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# A Shift Cipher Cracking Algorithm

## The Shift Cipher

The shift cipher, also known as Caesar's cipher, takes a plaintext  $m$  and shifts each letter forward a set number of times  $k$ . If

$m = \text{"Stop: Hammer time!"}$  then its encryption with key  $k = 4$  produces the ciphertext  $Enc_k(m) = \text{"WXSTLEQQIVXMQI"}$ . Notice that all letters are capitalized and all spaces and punctuation are removed. My implementation of the shift cipher in Clojure uses the code below to psuedo-randomly generate a key.

```
(+ 1 (rand-int 25))
```

## The Cracking Algorithm

The cracking algorithm cycles through each possible value  $[1, 25]$  for  $k$  and finds the one that produces the text which has letter distribution that most closely matches the average letter distribution in English, as explained below. Let  $p_i$  represent the average frequency of the  $i$ th letter of the English alphabet (e.g.,  $p_1 = \text{"a"} = 0.08167$ ) and let  $q_i$  represent the frequency of occurrence of the  $i$ th letter in our ciphertext. To find which value  $k$  will shift the ciphertext such that it's letter frequency distribution most closely matches English it calculates

$$I_j = \sum_{i=1}^{26} p_i * q_{i+j} \text{ for all } j \text{ in } [1, 25].$$

Then it determines for which  $j$  the value  $I_j$  is closest to

$$\sum_{i=1}^{26} p_i^2 \approx 0.0655.$$

This is chosen as the value for  $k$  and then it reproduces the original text, albeit uniformly capitalized and sans punctuation and spacing.