Envelope Theorem

One choice variable and one constraint

Let F and G be econtinuously differentiable functions of x and θ . For any given θ , let $x^*(\theta)$ maximize $F(x,\theta)$ subject to $c \geq G(x,\theta)$, and let $\lambda^*(\theta)$ be the associated value of the Lagrange multipliesr. Suppose that $x^*(\theta)$ and $\lambda^*(\theta)$ are also continuously differentiable functions, and that the constraint qualification $G_1(x^*(\theta),\theta) \neq 0$ holds for all values of θ . Then, the maximum value function defined by

$$V(\theta) = \max_{x} F(x, \theta)$$
 subject to $c \ge G(x, \theta)$

satisfies

$$V'(\theta) = F_2(x^*(\theta), \theta) - \lambda^*(\theta)G_2(x^*(\theta), \theta).$$

itaic test