

NUEN 629
Numerical Methods in Reactor Analysis
Homework 4 & 5

Due on:
Thursday, November 19, 2015
&
Thursday, December 3, 2015

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Homework 4

Solve the following problem and submit a detailed report, including a justification of why a reader should believe your results and a description of your methods and iteration strategies.

1. (150 points + 50 points extra credit) In class we discussed the diamond-difference spatial discretization. Another discretization is the step discretization (this has several other names from other disciplines). It writes the discrete ordinates equations with isotropic scattering as, for $\mu_n > 0$ to

$$\mu_n \frac{\psi_{i,n} - \psi_{i-1,n}}{h_x} + \Sigma_t \psi_{i,n} = \frac{\Sigma_s}{2} \phi_i + \frac{Q}{2} \quad (1)$$

and for $\mu_n < 0$

$$\mu_n \frac{\psi_{i+1,n} - \psi_{i,n}}{h_x} + \Sigma_t \psi_{i,n} = \frac{\Sigma_s}{2} \phi_i + \frac{Q}{2} \quad (2)$$

The codes provided in class should be modified to implement this discretization.

- (a) (50 Points) Your task (should you choose to accept it) is to solve a problem with uniform source of $Q = 0.01$, $\Sigma_t = \Sigma_s = 100$ for a slab in vacuum of width 10 using step and diamond difference discretizations. Use, 10, 50, and 100 zones ($h_x = 1, 0.02, 0.01$) and your expert choice of angular quadratures. Discuss your results and how the two methods compare at each number of zones.
- (b) (10 points) Discuss why there is a different form of the discretization for the different signs of μ .
- (c) (40 points) Plot the error after each iteration using a 0 initial guess for the step discretization with source iteration and GMRES.
- (d) (50 points) Solve Reed's problem (see finite difference diffusion codes). Present convergence plots for the solution in space and angle to a "refined" solution in space and angle.
- (e) (50 points extra credit) Solve a time dependant problem for a slab surrounded by vacuum with $\Sigma_t = \Sigma_s = 1$ and initial condition given by $\phi(0) = 1/h_x$. Plot the solution at $t = 1$ s, using step and diamond difference. The particles have a speed of 1 cm/s. Which discretization is better with a small time step? What do you see with a small number of ordinates compared to a really large number (100s)?

Homework 5

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Project

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