

Uncertainty quantification of depletion calculations for specific isotopes using ORIGEN2

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Future Work

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Introduction

- Determing composition of irradiated fuel importance
 - Flux calculations
 - Reprocessing
 - Irradiation history verification
- Usually determined with a type of Bateman solver
- Uncertainties rarely reported
 - Flux Shape
 - > Fission yield
 - Cross Sections
 - Half-lives

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Current Problem

- Use of depletion code ORIGEN2
 - Solves with exponential method
 - Requires library
 - Decay information
 - Fission yield data
 - Single group cross sections
- PWR system with 3 wt% enriched uranium
- Varied ²³⁵U, ²³⁸U ²³⁹Pu, ²⁴⁰Pu, and ²⁴¹Pu
 - ightharpoonup Originally, σ_{γ} and γ for the FP were considered

Isotope solve list

¹³³ Cs	¹³⁶ Ba	¹⁵³ Eu
¹³⁴ Cs	¹³⁸ Ba	¹⁵⁴ Eu
¹³⁵ Cs	¹⁴⁹ Sm	²³⁹ Pu
¹³⁷ Cs	¹⁵⁰ Sm	²⁴² Pu
¹⁴⁸ Nd	¹⁰⁶ Rh	¹²⁵ Sb

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What is PUREX - A type of laundry detergent?

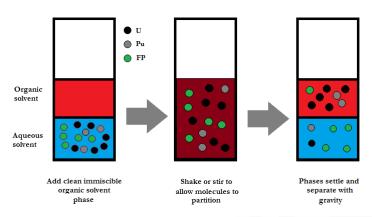
- Plutonium Uranium Redox EXtraction
 - Liquid-liquid solvent extraction
 - Many stages:
 - 1. Preparation for Dissolution
 - 2. Dissolution
 - 3. Preparation of Dissolved Feed
 - 4. Primary Decontamination Extraction to organic*
 - 5. Scrubbing
 - 6. Plutonium Partition Back-Extraction to aqueous*
 - 7. Plutonium Purification

* - Discussing Next

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Extraction

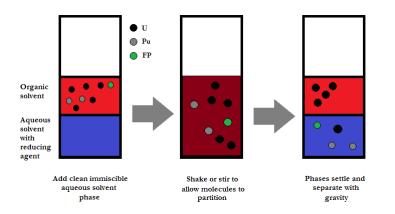
$$\begin{array}{l} UO_{2(aq)}^{2+} + 2NO_{3(aq)}^{-} + 2TBP_{(o)} \leftrightarrow UO_{2}(NO_{3})_{2} \cdot 2TBP_{(o)}^{[1]} \\ Pu_{(aq)}^{4+} + 4NO_{3(aq)}^{-} + 2TBP_{(o)} \leftrightarrow Pu(NO_{3})_{4} \cdot 2TBP_{(o)} \end{array}$$



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Back-Extraction

$$Pu(NO_3)_4(TBP)_{2(o)} + Fe^{2+}_{(aq)} \leftrightarrow Pu^{3+}_{(aq)} + 4NO^-_{3(aq)} + 2TBP_{(o)}^{[5]}$$



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Distribution Coefficients - The Missing link

 Distribution Coefficient (D): The ratio between the organic and aqueous phases (aka: D-values)

$$D = \frac{c_o}{c_{aq}}$$

- Specific element to element
- Vary widely with:^[7]
 - Composition of phases
 - Solution saturation
 - Temperature of the solvent
- * The fraction of mass, f_o deposited in the organic phase, assuming a volume ratio between the aqueous and organic phases, V_R , is:

$$f_o = (1 + D^{-1}V_R^{-1})^{-1}$$

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Decontamination Factors - The Pot of gold

 After several cycles of Pu extraction/scrubbing/back-extraction are completed, the effectiveness of a PUREX cycle is described by the decontamination factor (DF):

$$DF_{j} = \frac{\left|\frac{c_{j}}{c_{Pu}}\right|_{initial}}{\left|\frac{c_{j}}{c_{Pu}}\right|_{final}}$$

- DFs are characteristic of different process cycles
- Larger values (10⁷) for industrial scale PUREX (compared to benchtop)^[7, 1]

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Previous Work

Irradiation

- * $12.9 \pm 0.1 \text{ mg of DUO}_2$ was irradiated
 - High Flux Isotope Reactor at Oak Ridge National Laboratory
- * Burnup was 4.43 \pm 0.31 GWd/tHM^[8]
- * $0.196 \pm \text{mg}$ of total Pu was produced as measured by ICP-MS



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Dissolution of the spent fuel pellet



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Glovebox









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- Single stage extraction and back-extraction
 - Purpose: quantify product recovery, D-values and DF values for single stage extraction and back extraction
 - Conditions:

Starting Solution	Extraction Solution	Back extraction solution		
4 M nitric acid	30% vol.% TBP, 70 vol.% kerosene	0.024 M ferrous sulfamate in 0.75 M nitric acid		

- Multi-contact extraction and back-extraction
 - Purpose: Maximize recovery of Pu with 4 extractions, 3 back extractions
 - Conditions:

Starting Solution Extraction Solution		Back extraction solution		
4 M nitric acid	30% vol.% TBP, 70 vol.% kerosene	0.024 M ferrous sulfamate in 4 M nitric acid		

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Previous Experiment Results

Recoveries of U and Pu					
		Pu Recovery	U Recovery		
	Single stage	(83.4±9.5)%	(11.2±1.3)%		
	Multi-contact Cycle 1	$(99.7 \pm 4.2)\%$	$(6.8\pm0.3)\%$		
	Multi-contact Cycle 2	$(93.0\pm4.6)\%$	$(6.6\pm0.3)\%$		
	Overall Experiment 2	$(92.7\pm6.0)\%$	$(0.45\pm0.03)\%$		

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Previous Experiment Results

Decontamination Factors

Element (Z)	SS	Error	MC Cycle 1	Error	Isotopes Used
Rb(37)	39.0	5.9	11.8	0.8	⁸⁵ Rb
Sr(38)	283	43	84.6	5.9	⁹⁰ Sr
Mo(42)	5.7	0.8	1.9	0.2	^{97,98,100} Mo
Ru(44)	59.2	6.4	16.6	2.5	^{101,102,104} Ru
Pd(46)	65	14	8.9	1.2	¹¹⁰ Pd
Cd(48)	74	17	22.1	2.5	¹¹² Cd
Cs(55)	177	28	52.9	3.9	¹³³ Cs
Ce(58)	43	16	11.5	4.9	^{140,142} Ce
Nd(60)	19.2	2.1	5.9	0.4	¹⁴³ Nd
Pm(61)	12.8	1.9	3.9	0.3	¹⁴⁷ Pm
Sm(62)	11.5	1.5	3.6	0.3	¹⁵¹ Sm
Eu(63)	10.0	1.4	3.6	0.3	¹⁵⁴ Eu
U(92)	7.4	1.2	14.7	0.9	²³⁸ U

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- Two PUREX experiments were conducted
 - Single stage: Determined DC values for Pu, U and several FP
 - ➤ Multi-contact: Utilized Experiment 1 to recover over 92% of Pu while leaving less than 1% of the U
- ❖ DF values were measured for 12 FP elements
- DF values were lower than those typically found in industrial scale PUREX plants due to multiple extraction and back-extraction steps without an intermittent scrubbing step.
- This work provide DF data that will be built upon for nuclear forensic investigations of interdicted Pu.

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Future Work

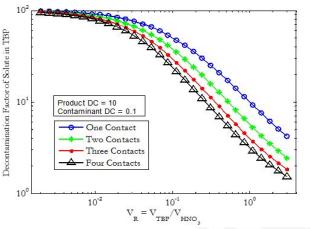
Future Work

- Modify Multi-contact extraction, to recover a larger fraction of Pu
- Investigation of how D-values for (Cs, Sb, Eu, Rb, Sr, Nd, Pm, and Sm) change as a function of nitric acid concentration
- Determine statistical uncertainty of D and DF values.
 - Repeat above experiments 3-5 times
- Connect D-values with process information to DF values

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Questions?

Previous Experiment Results



Decontamination Factors for multi-contact extraction.

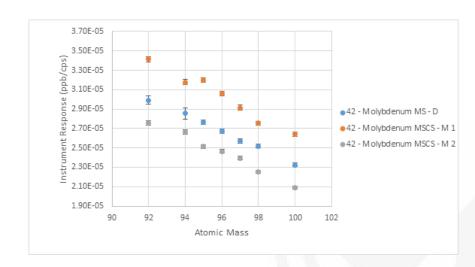
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Mass Spec



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