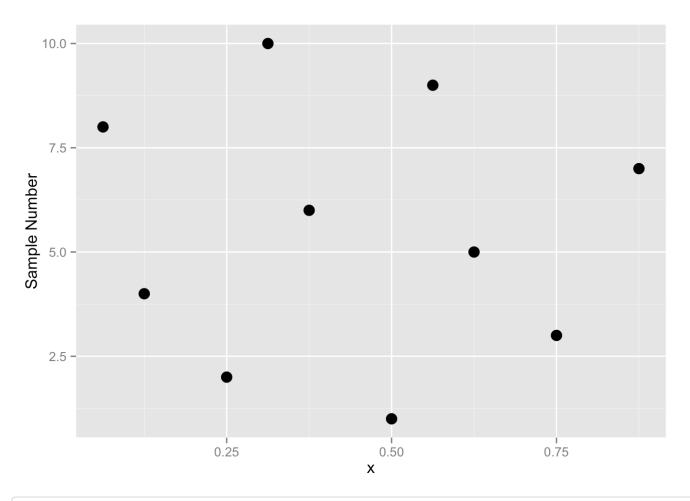
Quasi Monte Carlo

The first example of a QMC is the van Der corput sequence.

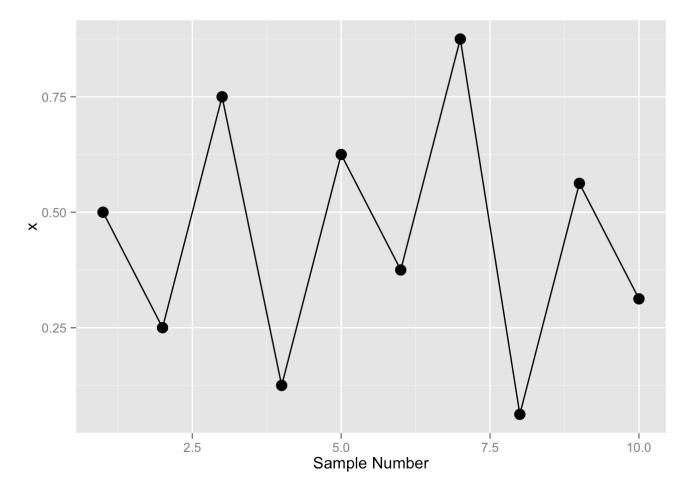
Van der Corput

Let's generate a 10 point van der Corput sequence.

```
npoints = 10
qmc <- data.frame(j = 1:npoints, x = halton(npoints))
ggplot(qmc,aes(x=x,y=j)) + geom_point(size=4) + scale_y_continuous('Sample Number')</pre>
```



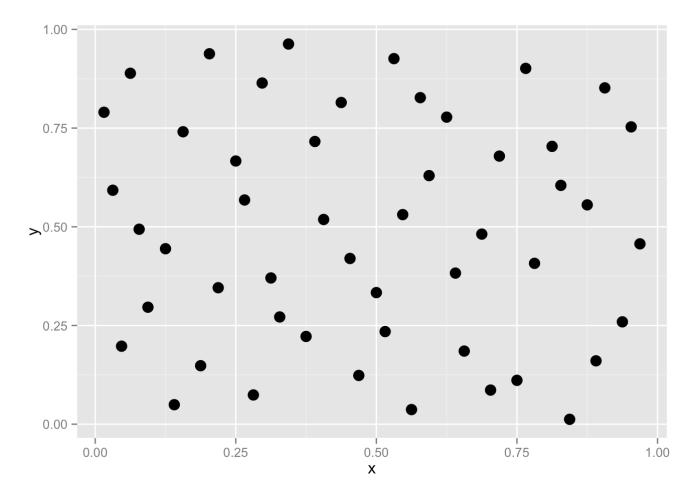
```
ggplot(qmc,aes(x=j,y=x)) + geom_line() + geom_point(size=4) + scale_x_continuous('Sample Number')
```



Halton Sequence

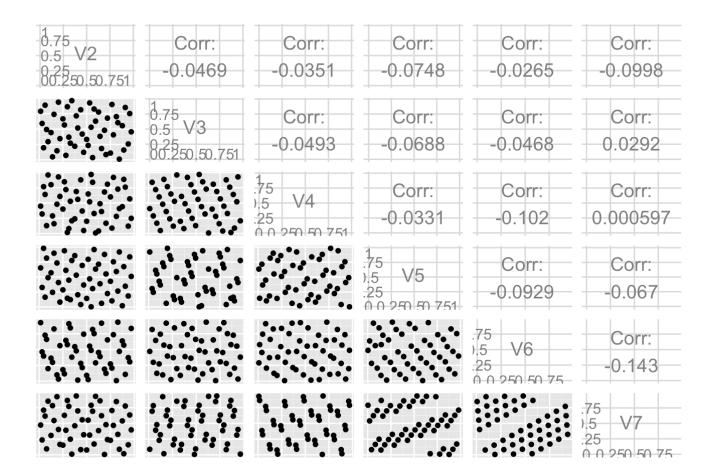
Now a Halton Sequence in 2-D

```
npoints = 50
xy = halton(npoints,dim=2)
qmc <- data.frame(j = 1:npoints)
qmc[,c("x","y")] = xy
ggplot(qmc,aes(x=x,y=y)) + geom_point(size=4)</pre>
```



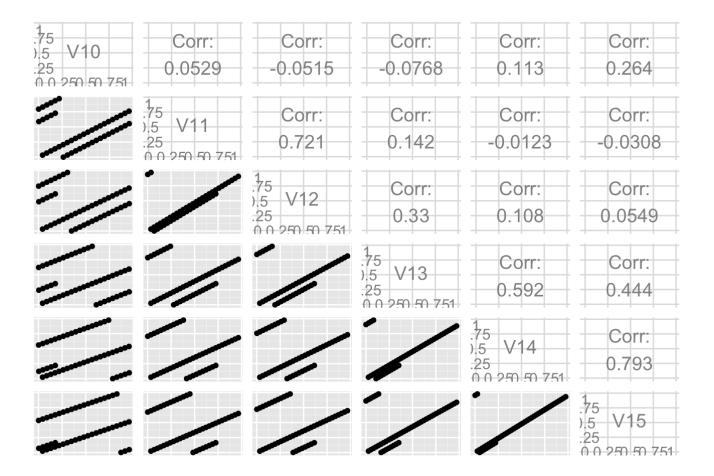
The warts begin to appear in a Halton Sequence in 6-D

```
npoints = 50
xy = halton(npoints,dim=6)
qmc <- data.frame(j = 1:npoints)
qmc[,2:7] = xy
ggpairs(qmc,columns=2:7)</pre>
```



15-D is just plain bad.

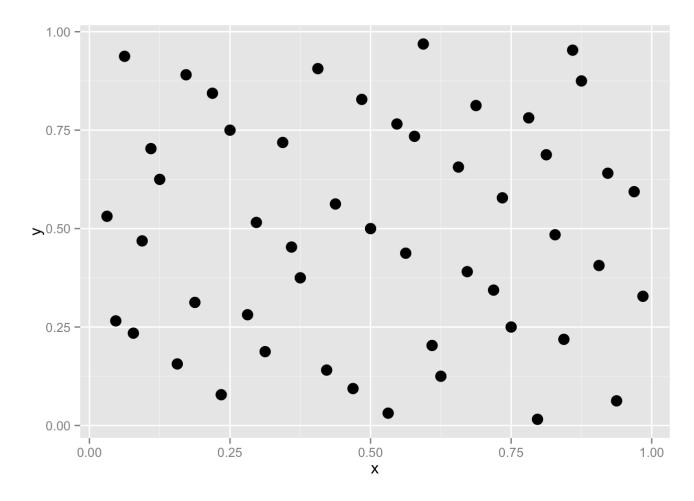
```
npoints = 50
xy = halton(npoints,dim=15)
qmc <- data.frame(j = 1:npoints)
qmc[,2:16] = xy
ggpairs(qmc,columns=10:15)</pre>
```



Sobol Sequnce

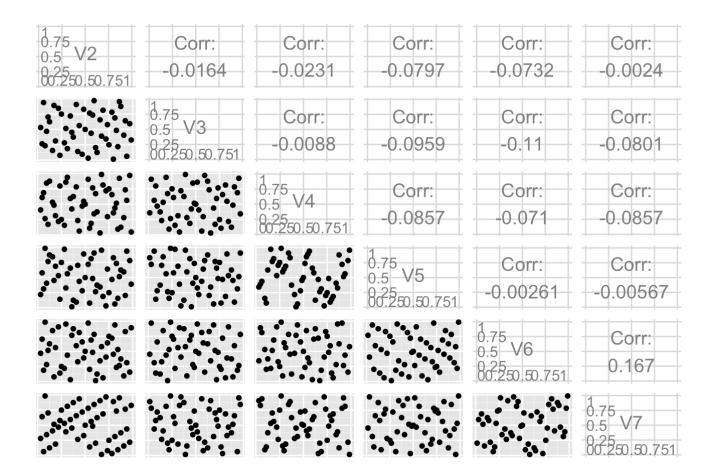
In 2-D the Sobol sequence is similar to Halton.

```
npoints = 50
xy = sobol(npoints,dim=2)
qmc <- data.frame(j = 1:npoints)
qmc[,c("x","y")] = xy
ggplot(qmc,aes(x=x,y=y)) + geom_point(size=4)</pre>
```



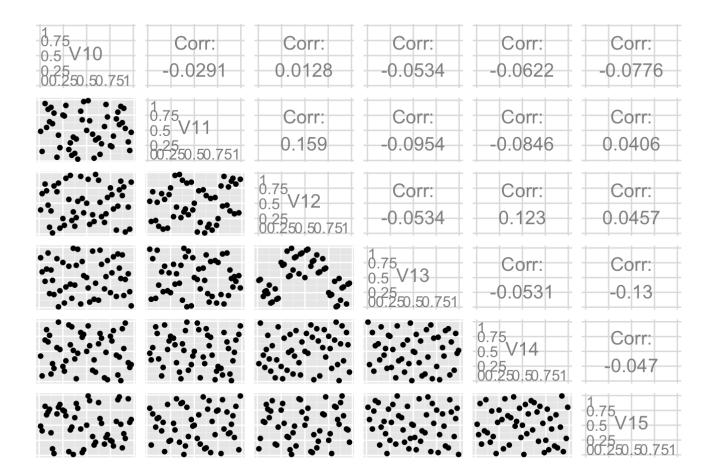
In 6-D the Sobol appears to be somewhat better than Halton, but still imperfect.

```
npoints = 50
xy = sobol(npoints,dim=6)
qmc <- data.frame(j = 1:npoints)
qmc[,2:7] = xy
ggpairs(qmc,columns=2:7)</pre>
```



15-D is much better than Halton.

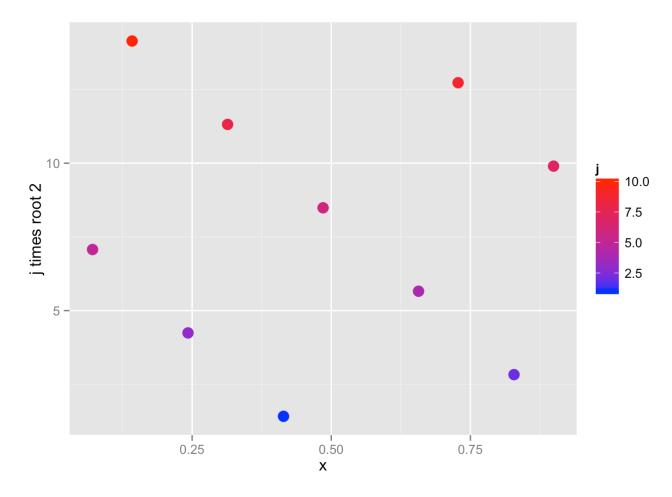
```
npoints = 50
xy = sobol(npoints,dim=15)
qmc <- data.frame(j = 1:npoints)
qmc[,2:16] = xy
ggpairs(qmc,columns=10:15)</pre>
```



Torus

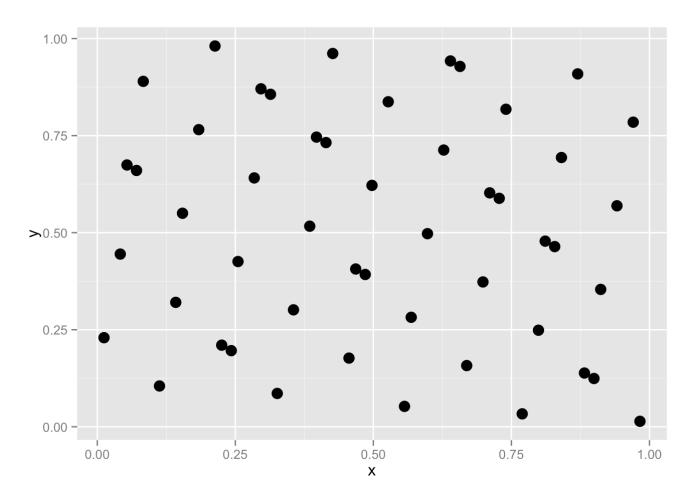
In 1-D the torus is the fractional part of $\sqrt{2}$:

```
npoints = 10
qmc <- data.frame(j = 1:npoints, x = torus(npoints), y = (1:npoints)*sqrt(2))
ggplot(qmc,aes(x=x,y=y,color=j)) + geom_point(size=4) + scale_y_continuous('j times root 2') + scale_colour_gradient(low="blue",high="red")</pre>
```



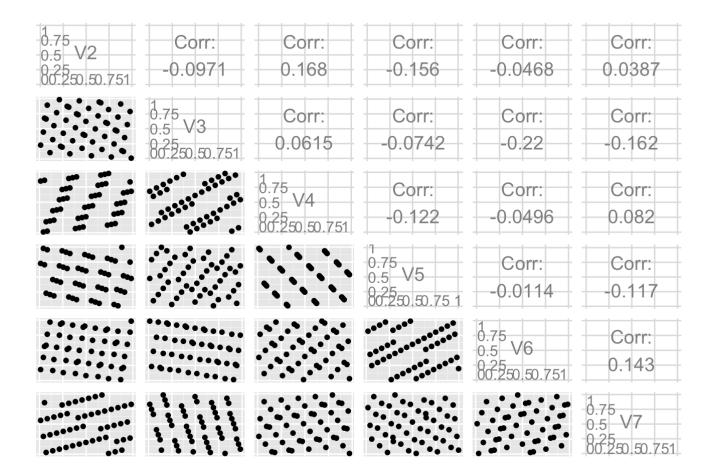
In 2-D the torus doesn't appear too random:

```
npoints = 50
xy = torus(npoints,dim=2)
qmc <- data.frame(j = 1:npoints)
qmc[,c("x","y")] = xy
ggplot(qmc,aes(x=x,y=y)) + geom_point(size=4)</pre>
```



In 6-D torus is probably the worst

```
npoints = 50
xy = torus(npoints,dim=6)
qmc <- data.frame(j = 1:npoints)
qmc[,2:7] = xy
ggpairs(qmc,columns=2:7)</pre>
```



15-D

```
npoints = 50
xy = torus(npoints,dim=15)
qmc <- data.frame(j = 1:npoints)
qmc[,2:16] = xy
ggpairs(qmc,columns=10:15)</pre>
```

0.75 0.5 V10 0.250,50.75 1	Corr: 0.239	Corr: 0.0357	Corr: -0.129	Corr: -0.444	Corr: -0.0148
///	.75 0.5 V11 .25 0.0 250 50 751	Corr: 0.069	Corr: 0.103	Corr: -0.209	Corr: -0.0707
		.75 V12 .25 .0.0 250 50 751	Corr: 0.0506	Corr: 0.026	Corr: 0.0128
			0.75 0.5 V13 0.250,50.75 1	Corr: 0.0578	Corr: -0.0596
	••••••			0.75 0.5 V14 80.250 50.751	Corr: -0.0774
		<i>////////</i>			0.75 0.5 V15 0.250 50.751