NUEN 647 Final Project

Uncertainty quantification of depletion calculations for specific isotopes using ORIGEN2.

I Introduction

Determing composition of irradiated fuel is of importance for a myriad of reasons. Whether for flux calculations, reprocessing, or irradiation history verification, calculating fuel composition requires a Bateman solver, and a means for building a sparse matrix.

Applications using these compositions rarely report the uncertainty associated with results, even when inputs, such as flux shape, fission yield, cross sections, and half-lives have varying degrees of uncertainty. Further sources of error in this calculation are due to the multi-group approximation, and single point approximation, but will not be explored here.

Several isotope concentrations, shown in Table 1, were calculated as a function of burnup with the depletion code ORIGEN2 for a PWR system with 3 Wt% enriched uranium. ORIGEN2 solves the bateman equations with the matrix expoential method and requires a library with decay and cross section information. Cross sections and fission product yields are reduced to single group through flux averaging before execution of the code, with the assumption that the flux has the same shape as a typical PWR.

The uncertainty of concentrations were determined by varying the absorption and fission cross sections for ²³⁵U, ²³⁸U ²³⁹Pu, ²⁴⁰Pu, and ²⁴¹Pu. Originally, absorption cross sections and yields for the fission products were to be varied, but variance information for the lighter nuclides is either difficult to acquire or not available.

The uncertainties on cross sections were determined by calculating the range of the single group cross section, taking the mid point as a mean, the range as a standard deviation, and assuming a Gamma distribution.

Table 1: Isotope solve list.

$^{133}\mathrm{Cs}$	$^{136}\mathrm{Ba}$	$^{153}\mathrm{Eu}$
$^{134}\mathrm{Cs}$	$^{138}\mathrm{Ba}$	$^{154}\mathrm{Eu}$
$^{135}\mathrm{Cs}$	$^{149}\mathrm{Sm}$	239 Pu
$^{137}\mathrm{Cs}$	$^{150}\mathrm{Sm}$	$^{242}\mathrm{Pu}$
$^{148}\mathrm{Nd}$	$^{106}\mathrm{Rh}$	$^{125}\mathrm{Sb}$

II Objectives

☑ Build ORIGEN2 model for thermal system which calculates concentrations of isotopes shown in Table 1.

Listing 1: PWR Input Deck

-1 -1 -1

```
RDA
          Irradiation of 1 MT of PWR fuel
     RDA
          Fuel enrichment is 3.0 w/o U-235
     RDA
         922350 922380 942390 942400 942410
     LPU
                    601 -602 603
             1 2 3
                                   9 50 0 1 38
     LIB
             101 102 103
                           10
     INP
                 -1
                     -1
                           1
                               1
10
     BUP
     IRP 100.0 37.5 1 2 4 2 BURNUP=3,750 MWD/MT
        200.0 37.5 2 3 4 0 BURNUP=7,500 MWD/MT
        300.0 37.5 3 4 4 0 BURNUP=11,250 MWD/MT
15
        400.0 37.5 4 5 4 0 BURNUP=15,000 MWD/MT
     DEC 500.0
                    5 6 4 0 DECAY FOR 100.0 DAYS
     DEC 4150.0
                     6 7 4 0 DECAY FOR 10 YEARS
                    7 8 4 0 DECAY FOR 200.0 YEARS
     DEC 73500.0
     BUP
     OPTL 24*8
     OPTA 4*8 5 19*8
     OPTF 4*8 5 19*8
             8
                 1
     OUT
     END
  2 922340 270. 922350 30000. 922380 969730. 0 0.0
   0
```

The model irradiates 1 metric ton of US PWR fuel for a single cycle (15,000 MWd/Mt). The calculations use a constant power assumption of 37.5 W/g. The model does not include the oxygen because we are not interested in the activation of oxygen. Cross section modification throughout the calculation use the changing flux associated with a US PWR.

Initial verification of the model analyzed the end concentration of 137 Cs and calculated the burn-up from that value. This calculation does not have an exact value for the yield of 137 Cs and is used qualitatively as a sanity check.

$$\frac{552.8 \text{ g}^{137}\text{Cs}}{Mt} \cdot \frac{6.022E23 \text{ atoms}}{137 \text{ g}^{137}\text{Cs}} \cdot \frac{\text{Fission}}{0.06 \text{ atoms}} \cdot \frac{200 \text{ MeV}}{\text{Fission}} \cdot \frac{1.602E - 19 \text{ MJ}}{1 \text{ MeV}} \cdot \frac{1 \text{ day}}{86400 \text{ s}} = 15,018 \frac{\text{MWd}}{Mt}$$

 \square Determine how to vary cross section and or flux spectrum inputs for calculation

ORIGEN2 reads in cross section information through a file named "TAPE9.inp", specified by the 8th input on the LIB card. "TAPE9.inp" needs at least 3 cross section libraries. These are specified by the 5th 6th and 7th inputs on the LIB card as 601, 602, and 603 for the activation products, actinides, and fission products, respectively. The input for ²³⁵U from library 601 is shown in the listing below, with a corresponding key shown in Table 2 [1].

Listing 2: ²³⁵U cross section library 602 input

602	922350 1.068E+01	2.338E-03	8.049E-07	4.752E+01	0.0	0.0	-1.0
-----	------------------	-----------	-----------	-----------	-----	-----	------

Table 2: Key to parameters in cross section library

LIB	NUCLID	(n,γ)	(n,2n)	(n,3n)	(n,f)	(n,γ^*)	(n,2n*)	YYN
-----	--------	--------------	--------	--------	-------	----------------	---------	-----

The cross sections, σ_{γ} and σ_{f} will be modified based on the locations in the cross section libraries shown above. Half-life information is contained in the decay libraries 1, 2, and 3 for activation products, actinides, and fission products, respectively. These values will not be modified to reduce the scope of the project.

Modifying the cross section libraries seems to have no bearing on the output of the code. This will be shown in the results section.

A program was writen to modify σ_{γ} , yield, or half-life based on lines from a text file. The project was simplified to only modify cross section input for the actuides, and therefore a modified version of is provided below. The code below is used to modify σ_{γ} and σ_{f} .

Listing 3: Script for modifying ORIGEN2 input.

```
#!/usr/bin/env python3
 #Please note, might have to run command
 # sed -i 's/E /E\+/g' TAPE9_BANK.inp
 # on file to make sure there are no spaces after E's
 ########################## Import Packages ####################
 import time
 start_time = time.time()
 import numpy as np
 import Functions as Fun
 from subprocess import call
 import os
 #As opposed to high class
 class ToPull:
    def init (self):
      self.Isotope = ""
25
      self.Type
 ListToPull=[]
 with open ('LISTTOPULL') as f:
    Lines=f.readlines()
 for i in Lines:
    i=i.split()
    ListToPull.append(ToPull())
    ListToPull[-1].Isotope =i[0]
    ListToPull[-1].Type
 ######################### Load all samples ##################
 with open ('SAMPLES/94Pu239a') as f:
    Pu239a=f.readlines()
```

```
Pu239a=Fun.StripNL(Pu239a)
 with open ('SAMPLES/94Pu240a') as f:
    Pu240a=f.readlines()
 Pu240a=Fun.StripNL(Pu240a)
 with open ('SAMPLES/94Pu241a') as f:
    Pu241a=f.readlines()
 Pu241a=Fun.StripNL(Pu241a)
 with open ('SAMPLES/94Pu239f') as f:
    Pu239f=f.readlines()
 Pu239f=Fun.StripNL(Pu239f)
 with open ('SAMPLES/94Pu240f') as f:
    Pu240f=f.readlines()
 Pu240f=Fun.StripNL(Pu240f)
 with open ('SAMPLES/94Pu241f') as f:
    Pu241f=f.readlines()
 Pu241f=Fun.StripNL(Pu241f)
60
 with open ('SAMPLES/92U235a') as f:
    U235a=f.readlines()
 U235a=Fun.StripNL(U235a)
 with open ('SAMPLES/92U238a') as f:
    U238a=f.readlines()
 U238a=Fun.StripNL(U238a)
 with open ('SAMPLES/92U235f') as f:
    U235f=f.readlines()
 U235f=Fun.StripNL(U235f)
 with open ('SAMPLES/92U238f') as f:
    U238f=f.readlines()
 U238f=Fun.StripNL(U238f)
 with open ('ORIGENBACKUP/TAPE9 BANK.inp') as f:
    TAPE9content=f.readlines()
80
 for k in range(0,len(U238f)):
 #for k in range(0,1):
    \#k = 2
    #Open output file
    output=open("TAPE50.inp","w")
    #output=open("tape9.inp","w")
    START=False #To print everything (True), otherwise print somethings...
    PRINTFIRSTLINE=True #Print first line of actinides lib
```

```
PRINTLASTLINE=True #Print the minus 1 at the end of act lib
      REMOVEM1=False #If you want to remove all the -1s after each line
100
                   #Be careful if you are moding the first lib
      #Loop through the TAPE9 template file, make changes,
      #and write to new TAPE9 (output)
      for i in TAPE9content:
          hold=i.split()
105
          toprint=START
          if '602' in hold[0] and "-" not in hold[0]:
              if "942390" in hold[1]:
                 #Replace the gamma x-section
110
                  i=i.replace(hold[2],Pu239a[k])
                  #Replace the fission x-section
                  i=i.replace(hold[5],Pu239f[k])
                  toprint=True
              if "942400" in hold[1]:
                  #Replace the gamma x-section
115
                  i=i.replace(hold[2],Pu240a[k])
                  #Replace the fission x-section
                  i=i.replace(hold[5],Pu240f[k])
                  toprint=True
              if "942410" in hold[1]:
120
                  #Replace the gamma x-section
                  i=i.replace(hold[2],Pu241a[k])
                  #Replace the fission x-section
                 i=i.replace(hold[5],Pu241f[k])
                 toprint=True
125
              if "922350" in hold[1]:
                  #Replace the gamma x-section
                  i=i.replace(hold[2],U235a[k])
                  #Replace the fission x-section
                  i=i.replace(hold[5],U235f[k])
130
                 toprint=True
              if "922380" in hold[1]:
                  #Replace the gamma x-section
                  i=i.replace(hold[2],U238a[k])
                  #Replace the fission x-section
135
                  i=i.replace(hold[5],U238f[k])
                  toprint=True
              if "ACTINIDE+AND" in i and PRINTFIRSTLINE:
                 toprint=True
          if REMOVEM1:
140
              i=i.replace("-1","")
          if toprint:
              i=i.replace("\n","")
              print(i, file=output)
      if not START and PRINTLASTLINE:
145
          print ("
                  -1", file=output)
      output.close() #important or ORIGEN2 wont run
       #endfile record being detected otherwise
       150
       #I think tape9 needs to be executable?
```

```
#os.system("chmod +x tape9.inp")
155
       #os.system("chmod +x TAPE50.inp")
      #Run with new TAPE9, also deletes old files
      print("Run number :"+str(k+1))
      call(["./r"])
160
       165
      #Open output file and save contents
      with open ('TAPE6.OUT') as f:
          content=f.readlines()
      #Work on Page by Page Basis for output
170
      #Also grab time steps
      Pages=[];Page=""
      TimeDays=[]; AD="ACTINIDES+DAUGHTERS" #For space
      for i in content:
          if "PAGE" in i:
175
              #Save the Page if it has useful information
              if AD in Page or "FISSION PRODUCTS" in Page:
                 Pages.append(Page)
              Page=""
          else:
180
              Page=Page+i
          #If we have located the time steps pull the info
          if "TIME, SEC" in i:
              i=i.replace("TIME, SEC","")
              i=i.split()
185
              for j in i:
                 TimeDays.append(str(round(float(j)/86400,2)))
       #Pages has a list of strings, each with a page on it
      #from the output
190
      #The only pages saved in Pages are ones with text:
      #"ACTINIDES+DAUGHTERS" or "FISSION PRODUCTS" the rest
      #of the output is trashed
      #Loop through all isotopes and grab info
195
      for item in ListToPull:
          Isotope=item.Isotope
          Type=item.Type
          Info=Fun.Graboutput(Isotope, Pages, Type)
          if k==0:
200
              SaveFile=open("OUTPUTDATA/"+Isotope+'.out','w')
              print('D,'.join(TimeDays)+'D',file=SaveFile)
              print(','.join(Info),file=SaveFile)
              SaveFile.close()
          else:
205
              SaveFile=open("OUTPUTDATA/"+Isotope+'.out','a')
              print(','.join(Info),file=SaveFile)
              SaveFile.close()
210
```

✓ Determine variance of Cross-sections

Both σ_{γ} and σ_{f} were determined by flux averaging via:

$$\sigma = \frac{\int \sigma(E)\phi(E)dE}{\int \phi(E)dE}$$

where:

$$\phi(E) = C_1 \cdot \frac{E}{E_0^2} \cdot exp\left(-\frac{E}{E_0}\right) \qquad E < E_{max,th}$$

$$= \frac{C_2}{E} \qquad E_{max,th} < E < E_{max,epi}$$

$$= C_3 \cdot \frac{\sqrt{\frac{E}{E_f}}}{E_f} \cdot exp\left(-\frac{E}{E_f}\right) \qquad E > E_{max,epi}$$

and:

$$C_1 = \frac{E_0^2}{E_{max,th}^2} e^{E_{max,th}/E_0}$$

$$C_2 = 1$$

$$C_3 = \frac{E_f}{E_{max,epi}} \cdot e^{\frac{E_{max,epi}}{E_f}} \frac{1}{\sqrt{\frac{E_{max,epi}}{E_f}}}$$

Where: $E_{max,th} = 0.50 \text{ eV}$, $E_{max,epi} = 1E5 \text{ eV}$, $\theta_{th} = 0.09 \text{ eV}$ (764 K), and $\theta_{fis} = 1.35E6 \text{ eV}$. These values were picked because they minimized the difference between the cross-sections in the TAPE9 file, and those calculated with ENDF-VII and the above method. This is highlighted in figure 1. Most of this error is from ^{238}U and ^{240}Pu .

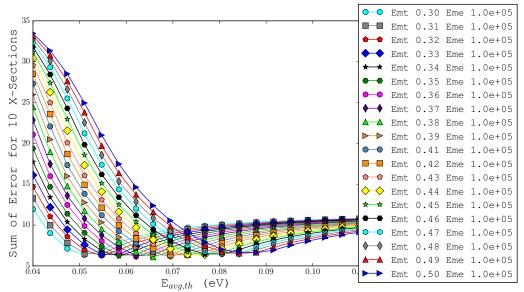


Figure 1: Minimized error for 10 cross section calculations

The flux spectrum is shown as below:

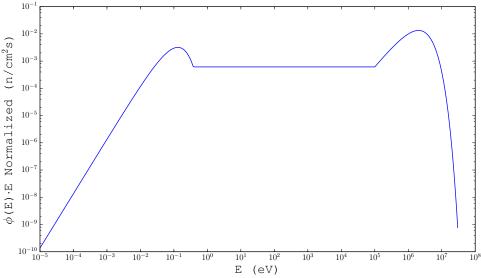


Figure 2: Flux Spectra used for weighting x-sections and yields

Table 3 shows the difference between my calculated cross section and the cross sections provided in ORIGEN2. The ratios will be used as a correction factor for the cross sections so that the input to ORIGEN2 will be constant. Differences have been attributed to the fact that the flux spectrum used does not capture reasonances. The cross sections were calculated with ENDF VII, and ORIGEN2 could have been processed with ENDF V, which would further account for differences, but has not been verified. The reason ENDF VII is being used for the current analysis is because the variance information is included in ENDF VII and not ENDF V.

Table 3: Comparison of one-group cross sections

ENDF VII	ORIGEN2	Ratio
6.544e + 01	6.909E+01	1.06
1.521e + 02	2.228E+02	1.46
4.518e + 01	4.202E+01	0.93
9.387e + 00	1.068E+01	1.14
4.098e + 00	8.872 E-01	0.22
1.179e + 02	1.211E+02	1.03
9.609 e-01	5.787E-01	0.60
1.253e + 02	1.259E + 02	1.01
4.621e + 01	4.752E + 01	1.03
2.091e-01	9.281E-02	0.44
	6.544e+01 1.521e+02 4.518e+01 9.387e+00 4.098e+00 1.179e+02 9.609e-01 1.253e+02 4.621e+01	6.544e+01 6.909E+01 1.521e+02 2.228E+02 4.518e+01 4.202E+01 9.387e+00 1.068E+01 4.098e+00 8.872E-01 1.179e+02 1.211E+02 9.609e-01 5.787E-01 1.253e+02 1.259E+02 4.621e+01 4.752E+01

Both σ_{γ}^{error} and σ_{f}^{error} were determined by calculating the single group cross section with error subtracted, and then added. These values will constitue a mean with error. This was done with the following code:

Listing 4: Script calculating average x-sections

```
#!/usr/bin/env python3
This program will compute 1-group cross sections with a weighted
flux. Parameters for the flux were
determined in a subdirectory called Reduce Err.
import time
start_time = time.time()
import Functions as f
from scipy import interpolate
from scipy import integrate
from scipy.integrate import trapz
#To fix X-section data to ORIGEN values
Ratios=[1.05578868993,1.46437937788,0.929974069639,1.13769098926,
    0.216470218472,1.02697467277,0.602248684356,1.0049132997,
    1.02836592353,0.443767334257]
#Get list of csv files with X-section information
```

```
Names=f.GETcsvFiles("X Sections")
  Names=["Pu_239_94_a.csv",
          "Pu_240_94_a.csv",
          "Pu_241_94_a.csv",
          "U_235_92_a.csv",
          "U_238_92_a.csv",
          "Pu_239_94_f.csv",
          "Pu_240_94_f.csv",
40
          "Pu_241_94_f.csv",
          "U_235_92_f.csv",
          "U_238_92_f.csv"]
  #Flux Parameters
  Emt=0.38
                 #Max thermal energy in ev
  Eme=1e5
                  #Max epithermal energy in ev
  E0=0.0658
                   #Thermal average in ev (1045 K)
                  #Fission average in ev
  Ef=1.35e6
  #Loop through all the X-sections I got
  index=0
  for Name in Names:
       Element=Name.split('_')[0]
55
       Isotope=Name.split('_')[1]
       Protons=Name.split('_')[2]
       Reaction=Name.split('_')[3].split('.')[0]
       #Do not do Averaging of variances
60
       if 'V' in Reaction:
           continue
       Xsec = f.np.genfromtxt('X_Sections/'+Name, delimiter=',')
       #Modify Xsections to match with ORIGEN2
65
       Xsec[:,1]=Xsec[:,1]*Ratios[index]
       index=index+1
       #Set energy, and convert from MeV to ev
       E=f.copy.copy(Xsec[:,0])*10**6
70
       #Gather Variance and make function for it
      VarName=Name.split(".")[0]+"V.csv"
       Var=f.np.genfromtxt('X_Sections/'+VarName, delimiter=',')
      Var_int=interpolate.interp1d(Var[:,0],Var[:,1],
75
                                     fill_value=0,bounds_error=False)
       #Determine the absolute err from the variance
       ErrAb = (Var_int(E)/100) *Xsec[:,1]
       #Find minimum X-section
80
       Xmin=Xsec[:,1]-ErrAb
       #Find Max X-section
       Xmax=Xsec[:,1]+ErrAb
       #Calculate flux (yes we need E)
85
       F=f.flux(E,Emt,Eme,E0,Ef)
       #Make function for Min-X-Section(E) * Flux(E)
```

```
X_phimin=interpolate.interpld(E,F*Xmin,
                             fill_value=0,bounds_error=False)
      #Make function for Max-X-Section(E) * Flux(E)
      X_phimax=interpolate.interp1d(E,F*Xmax,
                             fill value=0, bounds error=False)
      #Perform the integral for Max-X-Section(E) * Flux(E)
      X_int_max=integrate.trapz(X_phimax(E),E)
95
      #Perform the integral for Min-X-Section(E) * Flux(E)
      X_int_min=integrate.trapz(X_phimin(E),E)
      #Perform the integral for Flux(E)
      Phi_int=integrate.trapz(F,E)
100
      #Average X-section value
      Avgmin=X_int_min/Phi_int
      Avgmax=X int max/Phi int
      Avg=(Avgmin+Avgmax)/2
105
      print (Protons+Element+Isotope+Reaction+' '+str(Avg) +
           '+/-'+str(Avg-Avgmin))
      #With the ratio fixes, Ratio should be one
      #Find TAPE9's X-section value for comparison
110
      #TAPE9_X=f.LoopTAPE(Protons, Isotope, Reaction)
      #Ratio=str(float(TAPE9_X)/Avg)
      #print(Protons+Element+Isotope+Reaction+' Average: %.3e' % Avg
            +', TAPE Value: '+TAPE9_X+
            ", Their Ratio: "+Ratio)
115
   print("--- %s seconds ---" % (time.time() - start time))
```

With results in Table 4

Table 4: Errors in single group cross sections

σ with 1STD Error
69.09 ± 8.15
222.8 ± 50.9
42.02 ± 10.92
10.68 ± 3.23
0.887 ± 0.175
121.1 ± 1.2
0.579 ± 0.003
125.9 ± 2.3
47.52 ± 0.71
$0.093 \pm 8.2 e-7$

Cross section versus flux for several isotopes are shown in the following figures.

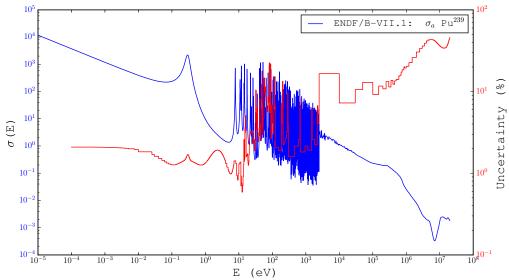
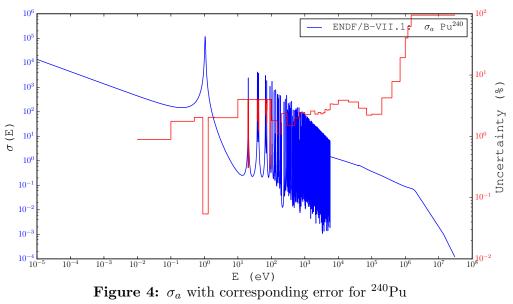


Figure 3: σ_a with corresponding error for ²³⁹Pu



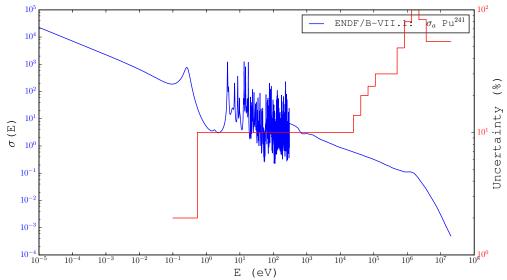
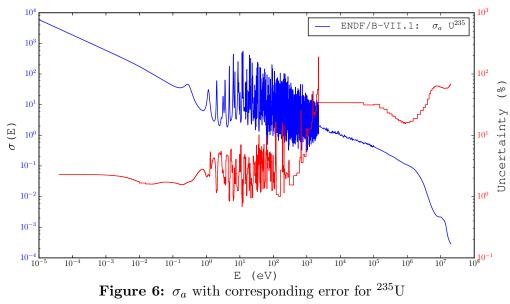
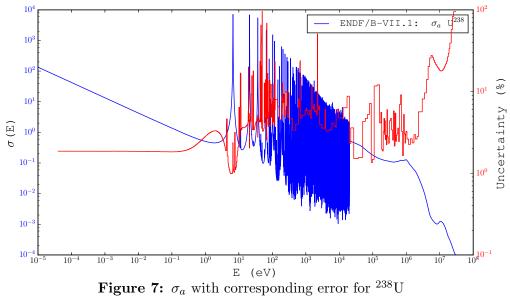
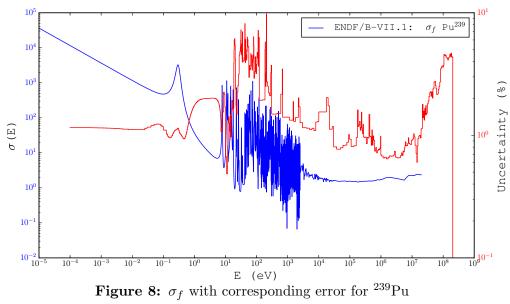


Figure 5: σ_a with corresponding error for ²⁴¹Pu







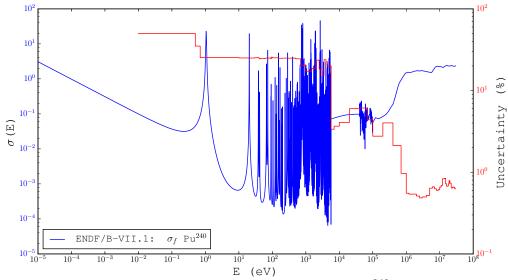
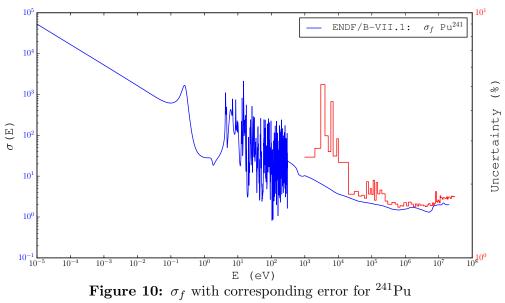


Figure 9: σ_f with corresponding error for $^{240}\mathrm{Pu}$



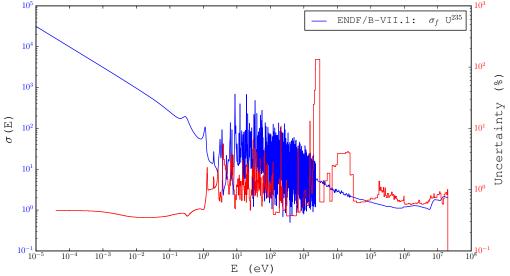


Figure 11: σ_f with corresponding error for $^{235}\mathrm{U}$

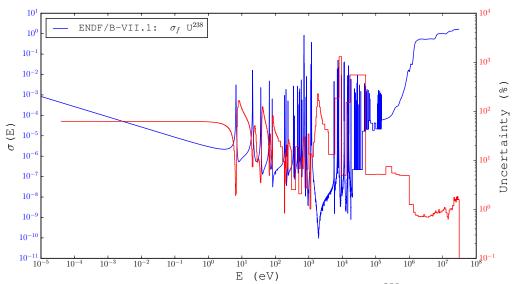


Figure 12: σ_f with corresponding error for ²³⁸U

The distribution for all 10 of the above cross sections are assumed as Gamma distributions to avoid negative cross section values.

$$\pi(\theta) = \frac{\theta^{\alpha - 1} e^{-\theta/\beta}}{\Gamma(\alpha)\beta^{\alpha}}, \qquad \theta, \alpha, \beta > 0.$$

Therefore, we say that $\theta \sim G(\alpha, \beta)$. Where the mean and errors determined above fit into α and β via

$$\alpha = \frac{\mathrm{Mean^2}}{\mathrm{Error^2}}$$

and

$$\beta = \frac{\text{Error}^2}{\text{Mean}}$$

With the following codes the sampling space was determined.

Listing 5: Sample Generation code

```
#!/usr/bin/env python3
 11 11 11
 Will make N random samples and store in files with same
 names as isotopes
 10
 import time
 start time = time.time()
 import numpy as np
 import Functions as Fun
 class OneGroupwError:
   def ___init___(self):
     self.Element
     self.XSec
            = 0
                #X Section
     self.Err
            = 0
                #Error
25
 N=Fun.N
 Nbins=Fun.Nbins
 0=[]
 with open ('OneGroupXSections') as f:
   Lines=f.readlines()
 for i in Lines:
   i=i.split()
40
   O.append(OneGroupwError())
   O[-1].Element = i[0]
   O[-1].XSec = float(i[1].split('+/-')[0])
   O[-1].Err
         = float(i[1].split('+/-')[1])
 for i in 0:
   #Make Samples
   alpha=(i.XSec**2)/(i.Err**2)
```

Below are histograms of the sampling space, most of the others look the same, with samples surrounding the mean.

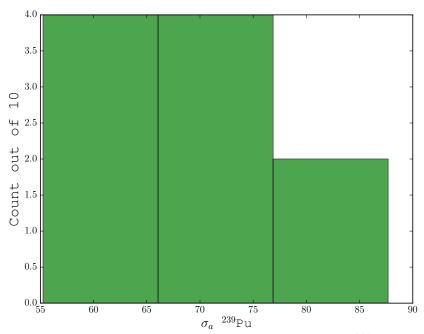


Figure 13: Histogram of sample space for σ_a ²³⁹Pu

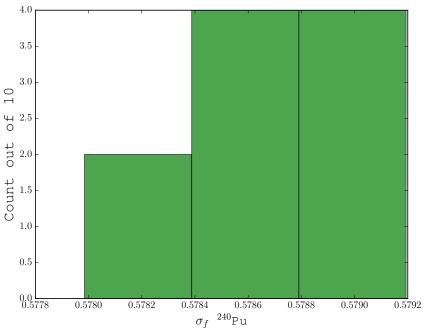


Figure 14: Histogram of sample space for σ_f ²⁴⁰Pu

The sampling spaces were run through ORIGEN with the code shown in the first section.

☑ Plot Results

The function for plotting results are shown below.

Listing 6: Code for plots

```
25
  #For histogram plots
 TimeIndex=3
  #Below should be the same as in 'Sample Gen' file (I know its lame)
 N=Fun.N
 Nbins=Fun.Nbins
 #Which Time Steps for range...
 T1 = 0
 Tf=5
  #15 Elements, cant do all at once Do 8 at a time (lame again)
  \#E1 = 9
  \#Ef = 1.5
 E1=0
40 Ef=9
  45 #As opposed to high class
  class ToPull:
    def __init__(self):
       self.File = ""
 #Gather all output file names
 ListToPull=[]
 with open ('LISTTOPULL') as f:
    Lines=f.readlines()
  for i in Lines:
    i=i.split()
55
    ListToPull.append(ToPull())
    ListToPull[-1].File =i[0]+'.out'
  #Loop through output file names
  for index in range(E1,Ef):
    fileparse=ListToPull[index].File
    #Save output file information
    with open("OUTPUTDATA/"+fileparse) as f:
       Lines=f.readlines()
70
    #Get time information from first row
    TimeList=Lines[0].replace(' \ ' ' ').replace(' \ ' ' ').split(',')
    Time=[]
    for times in TimeList:
       Time.append(float(times))
75
    #Make matrix of data for rest
    Data=[]
    del Data
```

```
for i in range(1,len(Lines)):
80
         line=Lines[i].replace('\n','')
         line=line.split(',')
         line=[float(i) for i in line]
         trv:
            Data=np.vstack((Data, line))
85
         except NameError:
            Data=copy.copy(line)
      #Plot Time vs grams for all different runs
      HISTSamples=[]
90
      fig=Fun.plt.figure(figsize=Fun.FigureSize)
      ax=fig.add_subplot(111)
      label=''
      for run in Data:
         HISTSamples.append(run[TimeIndex])
95
         #print(run) Plot
         (fig,ax) = Fun.plot(Time[T1:Tf], run[T1:Tf],
                       ax,'black',label,fig,fileparse)
      Element=fileparse.split('.')[0]
100
      Fun.plt.savefig("PLOTS/"+Element+'Post_XY.pdf')
      #Make histogram for specified time for all different runs
      Fun.PlotHistSave2(HISTSamples, N, fileparse, Nbins)
  print("--- %s seconds ---" % (time.time() - start_time))
```

III Results

Quantities of interest are shown in Table 1 above. The uncertain parameters were the absorption and fission cross-sections for ²³⁵U, ²³⁸U, ²³⁹Pu, ²⁴⁰Pu, and ²⁴¹Pu.

Results are graphically represented below.

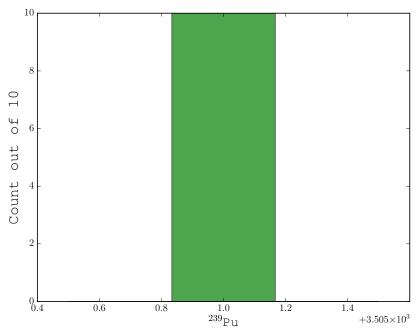
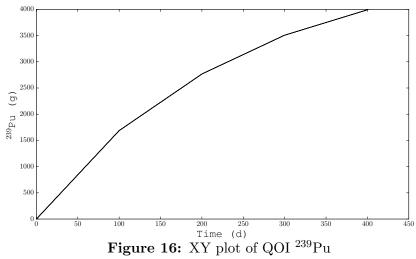
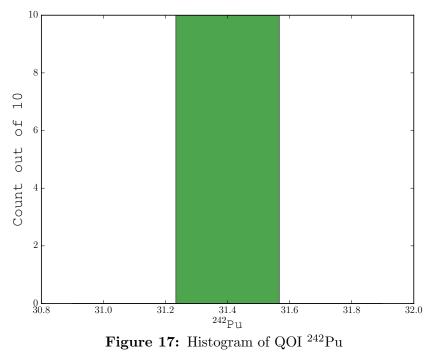
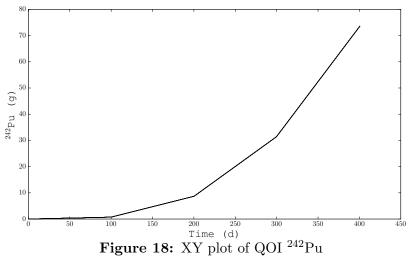


Figure 15: Histogram of QOI 239 Pu







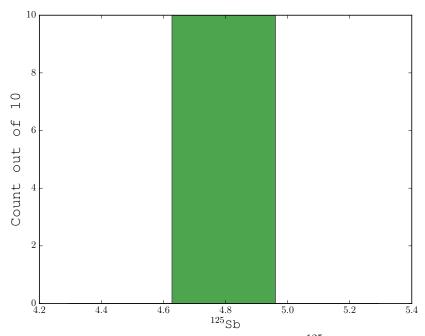
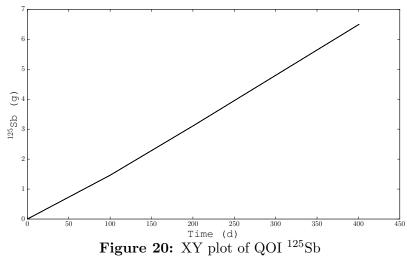


Figure 19: Histogram of QOI $^{125}\mathrm{Sb}$



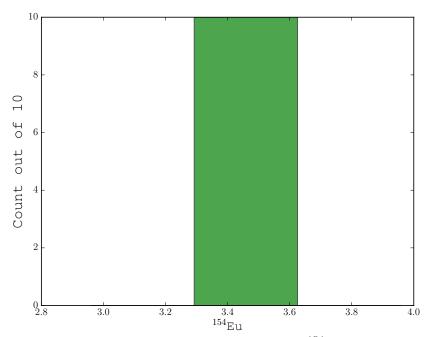
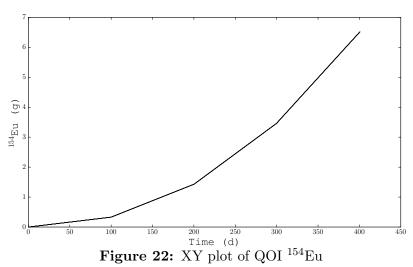


Figure 21: Histogram of QOI 154 Eu



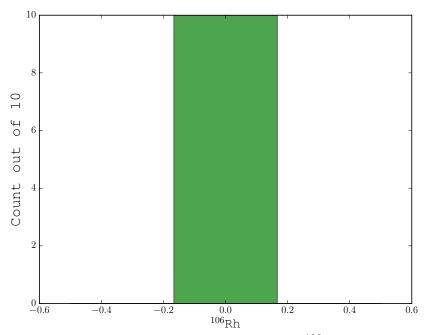
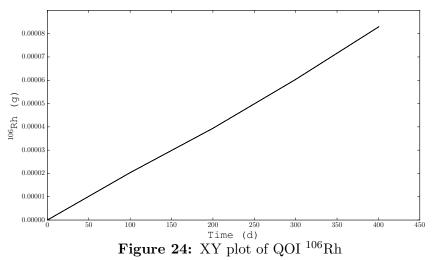


Figure 23: Histogram of QOI $^{106}\mathrm{Rh}$



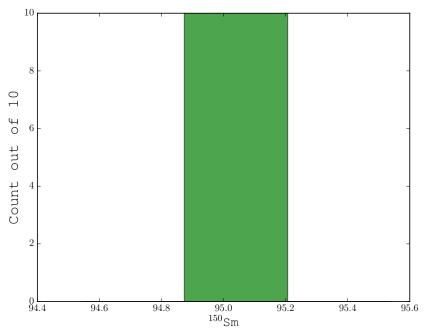
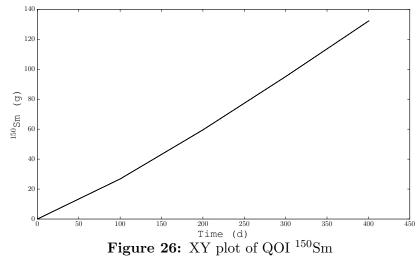


Figure 25: Histogram of QOI $^{150}\mathrm{Sm}$



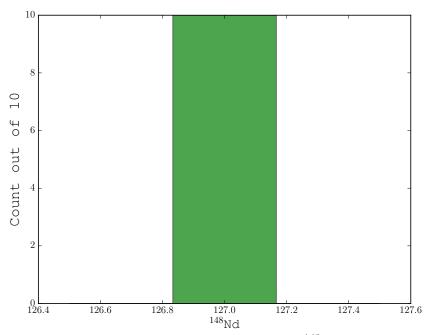
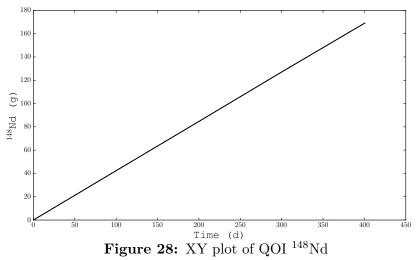


Figure 27: Histogram of QOI $^{148}\mathrm{Nd}$



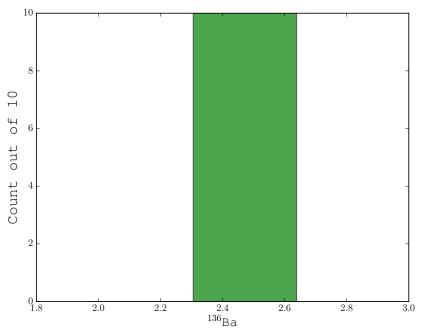
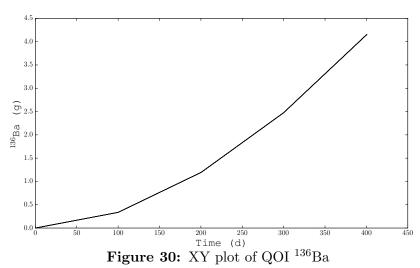


Figure 29: Histogram of QOI 136 Ba



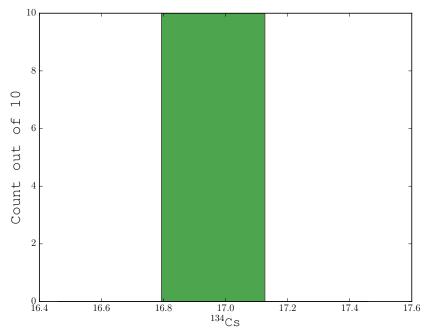
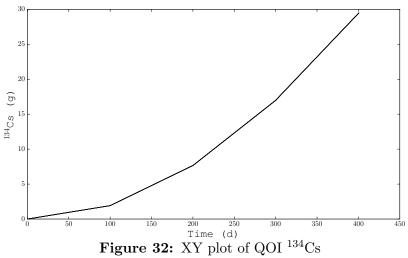


Figure 31: Histogram of QOI ¹³⁴Cs



I apologize for the wall of graphs. I left some out.

Conclusions IV

There was an unexpectedly large amount of error in the one group cross sections, but this is due to improperly sampling the cross sections. There is no variation in the output, even when a cross section is changed by a factor of over 1000, ORIGEN is not taking up what I am laying down.

References

[1] Allen G Croff. User's manual for the origen2 computer code. Technical report, Oak Ridge National Lab., 1980.