# Project 2 Report

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## 1 Language Decisions

Our group continued to use Python for the ease of expressing high level concepts and removal of memory management from the project. We also used Git for version control the collaboration tools. The repository can be found at Taylor's Github.

We continued our use of PyParsing to read in the grammar rules defined in external files.

### 2 Data Structures for a Context Free Grammar

The complete defintions for our data structures can be found in section 8.1. However, we will break them down in the order presented in the project specification and outline the reason they were created and the features implemented.

### 2.1 Productions

The first data structure we implemented is a structures for a grammar production. The implementation of the data structure is a decorator for a pair of symbols. It simply groups the symbols together into a left and right half. The right half is allowed to be a list of symbols whereas the left half must only be one symbol.

```
class Production:
    """ Represents a production. """

def __init__(self, lhs, rhs):
    """
    :param str lhs: Left-hand-side symbol.
    :param list[str] rhs: List of right-hand-side symbols.
    """
    self.lhs = lhs
    self.rhs = rhs

#... property functions excluded for brevity ...
```

#### 2.2 Grammar

A grammar object is the logical extension of having a single production. In our implementation, grammars are a dictionary of symbol to list of list of symbols. The nested list returned represents all productions that can come from the non-terminal on the left hand side of a production. Therefore if the set of productions looks like:

```
A -> aaa
A -> b
```

Then, the resulting dictionary lookup for A would return the list ['aaa', 'b'].

When constructing the grammar, the first left hand side of a production encountered is considered the start symbol. So upon parsing and reading that symbol an internal pointer to the start symbol is maintained by the grammar object. The definition for the constructor of a grammar is as follows:

```
class Grammar:
        """ Data structure for context-free grammar. """
2
3
       def __init__(self, grammar=None):
            self.productions = dict()
            self.nonTerminals = set()
            self.start = ""
            if grammar is not None:
10
                # Convert ParseResult objects into Productions.
                parse = pyp_Grammar.parseFile(grammar)
12
                productions = [Production(p.lhs, p.rhs.asList()) for p in parse]
14
                # First production's left-hand-side is start symbol.
                self.start = productions[0].lhs
16
17
                # Hygiene checks.
18
                productions = Generating(productions)
                if self.start not in set(p.lhs for p in productions):
20
                    raise Exception("Starting production is non-generating!")
                productions = Reachable(productions, self.start)
22
23
                # Add all of the productions to the grammar.
24
                for production in productions:
25
                    self.addProduction(production.lhs, production.rhs)
26
```

As you can see, on lines 19 and 22, there are grammar hygiene checks that are performed that remove non-generating and non-reachable productions. Otherwise, a grammar is constructed from the string parameter which points to a relative file location. Line 12 is the only location in which PyParsing is used in the project.

# 3 Context Free Grammar Representation

We chose to stick with the representation given in the project specification document. We found there were no changes need to be made to successfully represent a grammar. For completeness, the representation is below:

```
Grammar -> Grammar Production
Grammar ->
Production -> symbol Arrow List
Arrow -> '->
List -> symbol List
List ->
```

We note that a symbol in this context is any whitespace delimited string of printable ascii characters.

## 4 Parser for CFG Representation

Using PyParsing, the following is the representation for the representation given in section 3:

# 5 Grammar Hygiene Checks

After reading in a grammar, certain hygiene checks must be made. We must ensure that we can reach all non-terminals and we also must ensure that we can generate a terminal string with every production.

#### 5.1 Generating

We first check for non-generating productions as follows:

```
def Generating(productions):
    """

... comment excluded for brevity ...
    """

nonTerms = set(production.lhs for production in productions)
productive = set()

# Repeat until no new results are yielded.
```

```
previousSize = -1
        while previousSize < len(productive):</pre>
10
            previousSize = len(productive)
12
            for production in productions:
13
                # Don't bother with productions that are already marked.
                if production.lhs not in productive:
15
16
                     # Empty rhs is productive.
17
                     if not production.rhs:
                         productive.add(production.lhs)
19
                     # If every symbol in the RHS is productive, lhs is
21
                     # productive.
                     else:
23
                         isProductive = True
                         for symbol in production.rhs:
25
                             if symbol in nonTerms and symbol not in productive:
                                  isProductive = False
27
                                 break
28
29
                         if isProductive:
30
                             productive.add(production.lhs)
31
32
        # Build list of all productions with generating left-hand-sides,
33
        # but remove any that have non-generating variables in their
34
        # right-hand-side.
35
        unproductive = nonTerms - productive
36
        return [p for p in productions if
                p.lhs in productive
38
                and set(p.rhs).isdisjoint(unproductive)]
39
```

#### 5.2 Unreachables

We also remove any non-terminals that are unreachable and, consequently, any productions including those unreachable non-terminals.

```
def Reachable(productions, start):
    """

... comment ommited for brevity ...

"""

nonTerms = set(production.lhs for production in productions)
reachable = {start}

marked = set(filter((lambda p: p.lhs == start), productions))
unmarked = set(productions) - marked
```

```
# Repeat until no new results are yielded.
       previousSize = -1
11
       while previousSize < len(reachable):</pre>
12
           previousSize = len(reachable)
13
            # Find all new reachable non-terminals in current marked set. Generate
            # a new marked set from all newly reachable non-terminals.
16
           nextMarked = set()
           for production in marked:
                for symbol in production.rhs:
                    if symbol in nonTerms and symbol not in reachable:
20
                        nextMarked |= set(filter((lambda p: p.lhs == symbol), unmarked))
                        reachable.add(symbol)
22
           marked = nextMarked
24
           unmarked -= marked
26
        # Create new list of only reachable rules.
       return [p for p in productions if p.lhs in reachable]
28
```

### 6 Nullable, First and Follows

To construct the LL1 parse table, we first must be able to compute First and Follows. Both of those also use the set of all non-terminals that are nullable. We'll start with nullable since it is the stand alone computation.

#### 6.1 Nullable

The set of all non-terminals that are nullable (can be removed through a series of productions ending with the null character) are:

```
def nullable(grammar):
2
           ...excluded for brevity...
       nullable = set()
       productions = grammar.productions
        cardinality = -1
       while cardinality < len(nullable):</pre>
10
            cardinality = len(nullable)
11
            for non_term in productions:
13
                #if epsilon is in the rhs already,
                #the production is nullable
15
                if [] in productions[non_term]:
16
```

```
nullable.add(non_term)
                else:
18
                    isNullable = False
19
                    for N in productions[non_term]:
20
                        #check to see if this specific production is
21
                         # nullable by checking to see if the join set of
22
                         # all symbols in the production are nullable.
23
                         # If they are not, that production is not nullable
24
                        isProductionNullable = True
25
                        for symbol in N:
                             isProductionNullable &= symbol in nullable
27
                         # This is the disjoint set of all nullable
                         # productions the correspond to this lhs
29
                        isNullable |= isProductionNullable
31
                    # if any of the disjoint productions are nullable,
                    # then this is true. Therefore, add this production's
33
                    # lhs to the nullable set
                    if isNullable:
35
                        nullable.add(non_term)
       return nullable
37
```

#### 6.2 First

19

Now, to compute the set of terminals that could be the first terminals after a non-terminal is replaced with a production, we calculate the closure as:

```
def first(grammar):
        ,,,
2
           excluded for brevity
4
       productions = grammar.productions
       #define the nullables
6
       nullable_non_terms = nullable(grammar)
       #initially set our table to the empty set of terminals
       prev_table = {non_term : set() for non_term in grammar.nonTerminals}
10
       #add just the productions of the form:
           non_terminal -> terminal
12
       #to start the algorithm off
       for non_term in grammar.nonTerminals:
14
           for N in productions[non_term]:
                if [] == N: continue
                if N[0] not in grammar.nonTerminals:
17
                    prev_table[non_term].add(N[0])
18
```

```
has_changed = True
21
       while has_changed:
           has_changed = False
23
            #construct the new table so we don't interfere with the
24
            #previous one by adding things we wouldn't add this iteration
            new_table = prev_table.copy()
27
            for non_term in grammar.nonTerminals:
28
                for rhs in productions[non_term]:
                    # if we have an epsilon, ignore it. It is the
30
                    # equivalent of adding the empty set.
                    if [] == rhs or rhs[0] not in grammar.nonTerminals:
32
                        continue
34
                    first = rhs[0]
                    # Now, we need to check to see if adding anything from
36
                    # the first item in the rhs changes the current set of
                    # terminals we have for this non_term
38
39
                    # this is done by seeing if the rhs's first
40
                    # non-terminal's first set can add anything to the
41
                    # current set of terminals for non_term
42
                    if len(prev_table[first] - prev_table[non_term]) > 0:
43
                        new_additions = prev_table[first] - prev_table[non_term]
44
                         #skip past all the nullables until we hit the end
45
                        #or we find a non-terminal. Add all the first sets
46
                        #for the next item in the production as we come
47
                        #across them
                        i = 1
49
                        while i+1 < len(rhs) and rhs[i] in nullable_non_terms:
50
                             if rhs[i + 1] in grammar.nonTerminals:
51
                                 new_additions |= prev_table[rhs[i + 1]]
                            else:
53
                                 #must list-ify to match the rest in the
55
                                 new_additions |= set([rhs[i+1]])
56
                                 break
57
                             i += 1
58
59
                        new_table[non_term] |= new_additions
60
                        has_changed = True
61
62
            prev_table = new_table.copy()
       return prev_table
64
```

#### 6.3 Follows

To finally wrap up the closures needed to compute the LL1 parse table, we construct the set of terminals that follow any non-terminal by:

```
def follows(grammar):
2
           excluded for brevity
3
4
       nullable_non_terms = nullable(grammar)
       first_table = first(grammar)
6
       productions = grammar.productions
        #initalize the table to contain only the empty sets
       follow_table = {non_term : set() for non_term in grammar.nonTerminals}
10
        #add the EOF symbol for the start state
        #TODO: Correct symbol for eof? What should we do here?
12
       follow_table[grammar.start].add('$')
13
       has_changed = True
15
        #iterate until all sets have not changed
16
       while has_changed:
17
            has_changed = False
19
            #construct the new table for us to put additions into
            new_table = follow_table.copy()
21
            #construct all the follow sets for every non-terminal
23
            for non_term in grammar.nonTerminals:
                #qet the dictionary of all {lhs : 'beta' values} (lists of
25
                #expressions following the non-terminal)n
                betas_following_term = betas_following(non_term, productions)
27
28
                #Get the lhs of the production, call it M (like in the book)
29
                for M in betas_following_term.keys():
30
                    #For every beta, calculate the following...
31
                    for beta in betas_following_term[M]:
32
                        i = 0
                        while i < len(beta):
34
                             #iterating from the first to the last term in the list of
35
                             #symbols
36
                            beta_term = beta[i]
38
                             # Case where beta is a non-terminal:
                             # Follows(non_term) = first(beta) U follows(non_term)
40
                            if beta_term in grammar.nonTerminals:
41
                                 # if we see a value that's not in follows(non_term), add
42
```

```
# it and set the changed flag to True
43
                                 if not first_table[beta_term] <= follow_table[non_term]:</pre>
44
                                      has_changed = True
45
                                      new_table[non_term] |= first_table[beta_term]
46
                             # Case where beta term is a terminal and we
47
                             # haven't seen it before add the non-terminal
48
                             # to the follows set and set the changed
49
                             # flag to True
50
                             elif beta_term not in follow_table[non_term]:
51
                                 has_changed = True
                                 new_table[non_term] |= set([beta_term])
53
54
                             # if the beta_term is not nullable, we are
55
                             # done with this list of symbols
                             if beta_term not in nullable_non_terms:
57
                                 break
59
                             i += 1
60
61
                         # case where all of the symbol list is nullable, in which
62
                         # we need to say follows(M) = follows(M) U follows(non_term)
63
                         if i == len(beta):
64
                             if not follow_table[M] <= follow_table[non_term]:</pre>
65
                                 has_changed = True
66
                                 new_table[M] |= follows_table[non_term]
68
            #update our table to point to the new one
            follow_table = new_table.copy()
70
        return follow_table
```

Where the function betas\_following\_term can be found in the full code for ll1\_tools.py in section 8.2. With all three closures calculated, we can now construct the parse table (defined in the following section 7).

### 7 LL1 Parse Table

### 8 Full Code

#### 8.1 cfg.py

```
#!/usr/bin/env python
```

""" Data structures for representing context-free grammars over ASCII alphabets and parsing functions to read grammar descriptions in files. The grammars are specified formally by:

Grammar -> Grammar Production

```
Grammar -> Production
   Production -> Symbol Arrow List
   List -> List Symbol
   List ->
    Where any symbols appearing left of the arrow are non-terminals, and the
    non-terminal of the first production is starting production. Productions are
    separated by lines.
from pyparsing import *
# pyparsing definitions for above-specified context-free grammar.
pyp_Arrow = Keyword("->").suppress()
pyp_Symbol = Word(alphanums)
pyp_List = ZeroOrMore(~LineStart().leaveWhitespace() + Word(printables))
pyp_Production = Group(pyp_Symbol.setResultsName("lhs") +
                       pyp_Arrow.suppress() +
                       Group(pyp_List).setResultsName("rhs"))
pyp_Grammar = ZeroOrMore(pyp_Production)
class Production:
    """ Represents a production. """
   def __init__(self, lhs, rhs):
        :param str lhs: Left-hand-side symbol.
        :param list[str] rhs: List of right-hand-side symbols.
        self.lhs = lhs
       self.rhs = rhs
   def __str__(self):
       return str(self.lhs) + " -> " + str(self.rhs)
   def __repr__(self):
       return str(self)
   def __hash__(self):
       return hash(str(self))
   def __eq__(self, other):
        return isinstance(other, Production)\
               and self.lhs == other.lhs\
```

```
and self.rhs == other.rhs
```

```
class Grammar:
    """ Data structure for context-free grammar. """
   def __init__(self, grammar=None):
        self.productions = dict()
        self.nonTerminals = set()
        self.start = ""
        if grammar is not None:
            # Convert ParseResult objects into Productions.
            parse = pyp_Grammar.parseFile(grammar)
            productions = [Production(p.lhs, p.rhs.asList()) for p in parse]
            # First production's left-hand-side is start symbol.
            self.start = productions[0].lhs
            # Hygiene checks.
            productions = Generating(productions)
            if self.start not in set(p.lhs for p in productions):
                raise Exception("Starting production is non-generating!")
            productions = Reachable(productions, self.start)
            # Add all of the productions to the grammar.
            for production in productions:
                self.addProduction(production.lhs, production.rhs)
   def addProduction(self, lhs, rhs):
        """Adds a production to the grammar. If the production's LHS already
        exists in the dictionary, the RHS is appended to the value
        list. If the LHS is not in the dictionary, it is added, and
        the RHS is added as a list.
        :param str lhs: Left-hand-side of the production.
        :param list[str] rhs: Right-hand-side of the production.
        if lhs in self.productions:
            self.productions[lhs].append(rhs)
        else:
            self.productions[lhs] = [rhs]
        self.nonTerminals.add(lhs)
```

```
def Generating(productions):
    """Returns a list of generating rules from a list of productions.
    This algorithm first identifies all initially-productive rules: -
    Rules with only terminals on the right-hand-side. - Rules with
    the empty string (epsilon) on the right-hand-side. Productions
    are then marked productive if their right-hand-side consists of
    only terminals and non-terminals marked as productive. This
    process is repeated until no new results are yielded. Any
    productions not marked as productive at this point are
    unproductive.
    :param list[Production] productions: List of productions to examine.
    :rtype: list[Production]
    11 11 11
   nonTerms = set(production.lhs for production in productions)
   productive = set()
    # Repeat until no new results are yielded.
   previousSize = -1
   while previousSize < len(productive):</pre>
        previousSize = len(productive)
        for production in productions:
            # Don't bother with productions that are already marked.
            if production.lhs not in productive:
                # Empty rhs is productive.
                if not production.rhs:
                    productive.add(production.lhs)
                # If every symbol in the RHS is productive, lhs is
                # productive.
                else:
                    isProductive = True
                    for symbol in production.rhs:
                        if symbol in nonTerms and symbol not in productive:
                            isProductive = False
                            break
                    if isProductive:
                        productive.add(production.lhs)
```

```
# Build list of all productions with generating left-hand-sides,
    # but remove any that have non-generating variables in their
    # right-hand-side.
   unproductive = nonTerms - productive
   return [p for p in productions if
            p.lhs in productive
            and set(p.rhs).isdisjoint(unproductive)]
def Reachable(productions, start):
   Returns a list of reachable rules from a list of productions.
    This algorithm initially marks the start productions as reachable. For every
    reachable state, all non-terminals in the reachable states' right-hand-sides
    are then marked as reachable (with a bit of checking to make sure it doesn't
    repeatedly check the same rules). This process is repeated until no new
    reachable states are found.
    :param list[Production] productions: List of productions to examine.
    :param str start: The starting non-terminal.
    :rtype: list[Production]
    11 11 11
   nonTerms = set(production.lhs for production in productions)
   reachable = {start}
   marked = set(filter((lambda p: p.lhs == start), productions))
   unmarked = set(productions) - marked
    # Repeat until no new results are yielded.
   previousSize = -1
   while previousSize < len(reachable):</pre>
       previousSize = len(reachable)
        # Find all new reachable non-terminals in current marked set. Generate
        # a new marked set from all newly reachable non-terminals.
       nextMarked = set()
        for production in marked:
            for symbol in production.rhs:
                if symbol in nonTerms and symbol not in reachable:
                    nextMarked |= set(filter((lambda p: p.lhs == symbol), unmarked))
                    reachable.add(symbol)
        marked = nextMarked
        unmarked -= marked
    # Create new list of only reachable rules.
```

return [p for p in productions if p.lhs in reachable]

### 8.2 ll1\_tools.py

```
from cfg import Grammar
def nullable(grammar):
    ,,,
    Returns a list of the all non-terminals that are nullable
    in the given grammar. A nullable non-terminal is calculated
    as a closure using the following rules:
      nullable(A -> Epsilon) -> True
      nullable(A -> a) -> False
      nullable(A \rightarrow AB) \rightarrow nullable(A) AND nullable(B)
      nullable(A \rightarrow A1 \mid A2 \mid ... \mid AN) \rightarrow nullable(A1) OR .. OR nullable(A_n)
    :param Grammar grammar: the set of productions to use and
                             wrapped in the Grammar object
    :return a set of all non-terminals that can be nullable
    nullable = set()
    productions = grammar.productions
    cardinality = -1
    while cardinality < len(nullable):</pre>
        cardinality = len(nullable)
        for non_term in productions:
            #if epsilon is in the rhs already,
            #the production is nullable
            if [] in productions[non_term]:
                nullable.add(non_term)
            else:
                isNullable = False
                for N in productions[non_term]:
                     #check to see if this specific production is
                     # nullable by checking to see if the join set of
                     # all symbols in the production are nullable.
                     # If they are not, that production is not nullable
                     isProductionNullable = True
                     for symbol in N:
                         isProductionNullable &= symbol in nullable
                     # This is the disjoint set of all nullable
                     # productions the correspond to this lhs
                     isNullable |= isProductionNullable
                # if any of the disjoint productions are nullable,
```

```
# then this is true. Therefore, add this production's
                # lhs to the nullable set
                if isNullable:
                    nullable.add(non_term)
    return nullable
def first(grammar):
    '''A first set calucation for a grammar returns a dictionary of all
    the first terminals that can proceed the rest of a parse given a
    non-termial symbol. First is a closure that is calculated as
    follows:
      first(Epsilon) -> EmptySet
      first(A -> a) -> { a }
      first(A \rightarrow A B) \rightarrow \{ first(A) \ U \ first(B), \ if \ nullable(A) \}
                        \{ first(A), 
                                                 otherwise
      first(A -> A1 | A2 | ... | AN) -> first(A1) U first(A2 U ... U first(AN)
    :param Grammar grammar: the set of productions to use wrapped in a
                            Grammar object
    :return dict{Non-Terminal : set(Terminal)}: a table of all terminals that
                                                 could come from a given
                                                 non-terminal
    productions = grammar.productions
    #define the nullables
    nullable_non_terms = nullable(grammar)
    #initially set our table to the empty set of terminals
    prev_table = {non_term : set() for non_term in grammar.nonTerminals}
    #add just the productions of the form:
    # non_terminal -> terminal
    #to start the algorithm off
    for non_term in grammar.nonTerminals:
        for N in productions[non_term]:
            if [] == N: continue
            if N[0] not in grammar.nonTerminals:
                prev_table[non_term].add(N[0])
    has_changed = True
    while has_changed:
        has_changed = False
        #construct the new table so we don't interfere with the
```

```
new_table = prev_table.copy()
        for non_term in grammar.nonTerminals:
            for rhs in productions[non_term]:
                # if we have an epsilon, ignore it. It is the
                # equivalent of adding the empty set.
                if [] == rhs or rhs[0] not in grammar.nonTerminals:
                    continue
                first = rhs[0]
                # Now, we need to check to see if adding anything from
                # the first item in the rhs changes the current set of
                # terminals we have for this non_term
                # this is done by seeing if the rhs's first
                # non-terminal's first set can add anything to the
                # current set of terminals for non_term
                if len(prev_table[first] - prev_table[non_term]) > 0:
                    new_additions = prev_table[first] - prev_table[non_term]
                    #skip past all the nullables until we hit the end
                    #or we find a non-terminal. Add all the first sets
                    #for the next item in the production as we come
                    #across them
                    i = 1
                    while i+1 < len(rhs) and rhs[i] in nullable_non_terms:
                        if rhs[i + 1] in grammar.nonTerminals:
                            new_additions |= prev_table[rhs[i + 1]]
                        else:
                            #must list-ify to match the rest in the
                            new_additions |= set([rhs[i+1]])
                            break
                        i += 1
                    new_table[non_term] |= new_additions
                    has_changed = True
        prev_table = new_table.copy()
    return prev_table
def betas_following(non_terminal, productions):
   ret_set = {}
   for k,v in productions.iteritems():
```

#previous one by adding things we wouldn't add this iteration

```
for rhs in v:
            if non_terminal in rhs:
                symbol_list = rhs
                while non_terminal in symbol_list:
                    idx = symbol_list.index(non_terminal)
                    beta = []
                    if idx + 1 < len(symbol_list):</pre>
                        beta = symbol_list[idx + 1:]
                         if k in ret_set:
                             ret_set[k].append(beta)
                            ret_set[k] = [beta]
                    symbol_list = beta
    return ret_set
def follows(grammar):
    ''', 'Calculates all terminals that can follow a given non terminal.
    Follows is a closure calculated by the following rules:
      given [M \rightarrow AN B] \rightarrow follows(N) = follows(N) U first(B)
                           if nullable(B) then
                            follows(M) = follows(M) U follows(N)
      qiven [M -> A N B1...A N B2...A N BX]
                   -> follows(N) = first(B1) U first(B2) U ...
                                       U first(BX)
                                    if nullable(B_i) then
                                      follows(M) = follows(M) U follows(N)
    :param Grammar grammar: the set of productions to use as a Grammar
                             object
    :return dict{non-Terminal : set(terminals)}: the set of terminal characters
                                                   that can follow any given
                                                   non-terminal
    ,,,
    nullable_non_terms = nullable(grammar)
    first_table = first(grammar)
    productions = grammar.productions
    #initalize the table to contain only the empty sets
    follow_table = {non_term : set() for non_term in grammar.nonTerminals}
    #add the EOF symbol for the start state
    #TODO: Correct symbol for eof? What should we do here?
    follow_table[grammar.start].add('$')
```

```
has_changed = True
#iterate until all sets have not changed
while has_changed:
   has_changed = False
    #construct the new table for us to put additions into
    new_table = follow_table.copy()
    #construct all the follow sets for every non-terminal
    for non_term in grammar.nonTerminals:
        #get the dictionary of all {lhs : 'beta' values} (lists of
        #expressions following the non-terminal)n
        betas_following_term = betas_following(non_term, productions)
        #Get the lhs of the production, call it M (like in the book)
        for M in betas_following_term.keys():
            #For every beta, calculate the following...
            for beta in betas_following_term[M]:
                i = 0
                while i < len(beta):
                    #iterating from the first to the last term in the list of
                    #symbols
                    beta_term = beta[i]
                    # Case where beta is a non-terminal:
                    # Follows(non_term) = first(beta) U follows(non_term)
                    if beta_term in grammar.nonTerminals:
                        # if we see a value that's not in follows(non_term), add
                        # it and set the changed flag to True
                        if not first_table[beta_term] <= follow_table[non_term]:</pre>
                            has_changed = True
                            new_table[non_term] |= first_table[beta_term]
                    # Case where beta term is a terminal and we
                    # haven't seen it before add the non-terminal
                    # to the follows set and set the changed
                    # flag to True
                    elif beta_term not in follow_table[non_term]:
                        has_changed = True
                        new_table[non_term] |= set([beta_term])
                    # if the beta_term is not nullable, we are
                    # done with this list of symbols
                    if beta_term not in nullable_non_terms:
                        break
```

```
i += 1

# case where all of the symbol list is nullable, in which
# we need to say follows(M) = follows(M) U follows(non_term)
if i == len(beta):
    if not follow_table[M] <= follow_table[non_term]:
        has_changed = True
        new_table[M] |= follows_table[non_term]

#update our table to point to the new one
follow_table = new_table.copy()

return follow_table

if __name__ == '__main__':
    x = Grammar('./testdata/unreachable.txt')
    f = follows(x)
    for i in f:
        print i, ':', f[i]</pre>
```