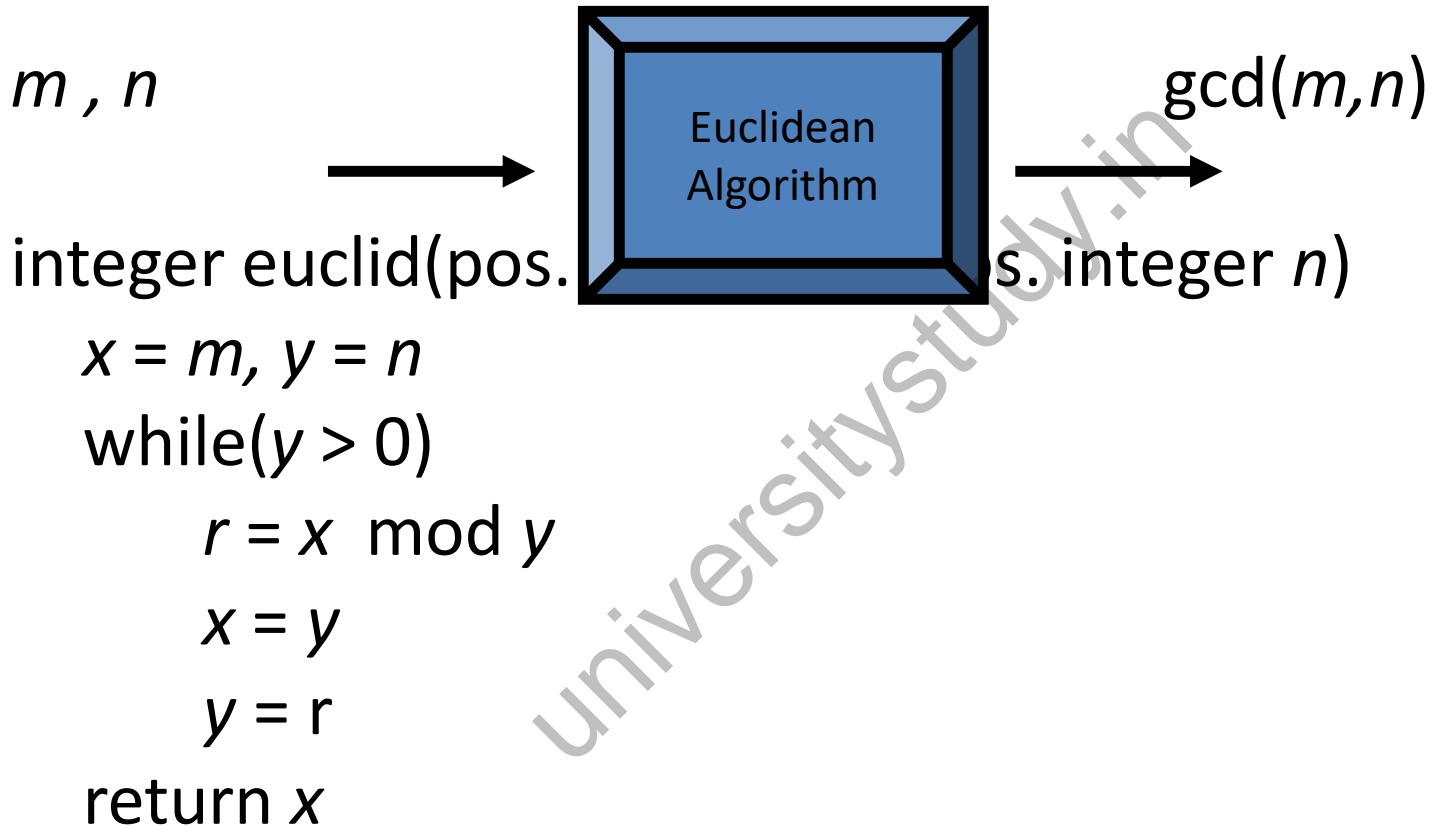




GCD and Optimization Problem

Euclidean Algorithm



Euclidean Algorithm. Example



$\text{gcd}(33, 77)$:

Step	$r = x \bmod y$	$x \leftarrow y$	$y \leftarrow r$
0	—	33	77

Euclidean Algorithm. Example



$\text{gcd}(33, 77)$:

Step	$r = x \bmod y$	$x \leftarrow y$	$y \leftarrow r$
0	–	33	77
1	$33 \bmod 77 = 33$	77	33

Euclidean Algorithm. Example



$\text{gcd}(33, 77)$:

Step	$r = x \bmod y$	$x \leftarrow y$	$y \leftarrow r$
0	–	33	77
1	$33 \bmod 77 = 33$	77	33
2	$77 \bmod 33 = 11$	33	11

Euclidean Algorithm. Example



$\text{gcd}(33, 77)$:

Step	$r = x \bmod y$	$x \leftarrow y$	$y \leftarrow r$
0	–	33	77
1	$33 \bmod 77 = 33$	77	33
2	$77 \bmod 33 = 11$	33	11
3	$33 \bmod 11 = 0$	11	0

Euclidean Algorithm. Example



$\text{gcd}(244, 117)$:

Step	$r = x \bmod y$	$x \leftarrow y$	$y \leftarrow r$
0	–	244	117

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Euclidean Algorithm. Example



$\gcd(244, 117)$:

Step	$r = x \bmod y$	$x \leftarrow y$	$y \leftarrow r$
0	–	244	117
1	$244 \bmod 117 = 10$	117	10

Euclidean Algorithm. Example



$\text{gcd}(244, 117)$:

Step	$r = x \bmod y$	$x \leftarrow y$	$y \leftarrow r$
0	–	244	117
1	$244 \bmod 117 = 10$	117	10
2	$117 \bmod 10 = 7$	10	7

Euclidean Algorithm. Example



$\text{gcd}(244, 117)$:

Step	$r = x \bmod y$	$x \leftarrow y$	$y \leftarrow r$
0	–	244	117
1	$244 \bmod 117 = 10$	117	10
2	$117 \bmod 10 = 7$	10	7
3	$10 \bmod 7 = 3$	7	3

Euclidean Algorithm. Example



$\text{gcd}(244, 117)$:

Step	$r = x \bmod y$	$x \leftarrow y$	$y \leftarrow r$
0	–	244	117
1	$244 \bmod 117 = 10$	117	10
2	$117 \bmod 10 = 7$	10	7
3	$10 \bmod 7 = 3$	7	3
4	$7 \bmod 3 = 1$	3	1

Euclidean Algorithm. Example



gcd(244,117):

Step	$r = x \bmod y$	$x \leftarrow y$	$y \leftarrow r$
0	-	244	117
1	$244 \bmod 117 = 10$	117	10
2	$117 \bmod 10 = 7$	10	7
3	$10 \bmod 7 = 3$	7	3
4	$7 \bmod 3 = 1$	3	1
5	$3 \bmod 1 = 0$	1	0

By definition \Rightarrow 244 and 117 are rel. prime.

Euclidean Algorithm Correctness



The reason that Euclidean algorithm works is $\gcd(x, y)$ is not changed from line to line. If x' , y' denote the next values of x , y then:

$$\begin{aligned}\gcd(x', y') &= \gcd(y, x \bmod y) \\ &= \gcd(y, x + qy) \quad (\text{the useful fact}) \\ &= \gcd(y, x) \quad (\text{subtract } y\text{-multiple}) \\ &= \gcd(x, y)\end{aligned}$$

Optimization Problem



- In mathematics and computer science, an **optimization problem** is the problem of finding the *best* solution from all feasible solutions. Optimization problems can be divided into two categories depending on whether the variables are continuous or discrete.
- An optimization problem with discrete variables is known as a **combinatorial optimization problem**. In a combinatorial optimization problem, we are looking for an object such as an integer, permutation or graph from a finite (or possibly countable infinite) set.



Thank You !!!

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