

- Q1. The differential equation of the form  $Mdx + Ndy = 0$  is said to be exact if
- a)  $\frac{\partial M}{\partial x} = \frac{\partial N}{\partial y}$       b)  $\frac{\partial M}{\partial y} = \frac{\partial N}{\partial x}$       c)  $\frac{\partial M}{\partial y} + \frac{\partial N}{\partial x} = 0$       d)  $\frac{\partial M}{\partial y} - \frac{\partial N}{\partial x} = 0$
- Q2. If the non exact differential equation  $Mdx + Ndy = 0$  is of homogeneous type with  $Mx + Ny \neq 0$  then the integrating factor is
- a)  $\frac{1}{My-Nx}$       b)  $\frac{1}{Mx-Ny}$       c)  $\frac{1}{Mx+Ny}$       d)  $\frac{1}{My+Nx}$
- Q3. Solution of  $xdy + ydx = 0$  is
- a)  $xy = c$       b)  $x + y = c$       c)  $x - y = c$       d) none of these
- Q4. For the non-exact differential equation  $Mdx + Ndy = 0$ , if  $\frac{1}{N} \left( \frac{\partial M}{\partial y} - \frac{\partial N}{\partial x} \right) = f(x)$ , Then the integrating factor is
- a)  $e^{f(x)}$       b)  $\frac{1}{f(x)}$       c)  $e^{\int f(x)dx}$       d)  $\int f(x)dx$
- Q5. Integrating Factor of  $ydx - xdy + a(x^2 + y^2)dx = 0$  is
- a)  $\frac{1}{x^2}$       b)  $\frac{1}{y^2}$       c)  $\frac{1}{x^2y^2}$       d)  $\frac{1}{(x^2+y^2)}$
- Q6. The general solution of equation  $xp^2 - yp + a = 0$ , where  $p = \frac{dy}{dx}$ , is given by
- a)  $y = cx - e^c$       b)  $y = cx + \frac{a}{c}$       c)  $y = cx - \sin^{-1}c$       d)  $(y - cx)^2 = a^2c^2 + b^2$
- Q7. The equation having  $e^{2x}$  and  $xe^{2x}$  as independent solution is
- (a)  $y'' - 4y' + 4 = 0$       (b)  $y'' - 5y' + 4 = 0$       (c)  $y'' - 4y = 0$       (d)  $y'' - 3y' + 2 = 0$
- Q8. The solution of  $y'' - 4y' + 4y = 0$  is
- a)  $Ae^{-2x} + Be^{2x}$       b)  $Ae^{-2x} + Be^x$       c)  $(A + Bx)e^{2x}$       d)  $(A + Bx)e^{-2x}$
- Q9. The wronskian of the function 1,  $\sin x$ ,  $\cos x$  is
- a) -1      b) 1      c) 0      d) 2
- Q10. The set of linearly independent solution of  $\frac{d^4y}{dx^4} - \frac{d^2y}{dx^2} = 0$  is
- (a)  $\{1, x, e^x, e^{-x}\}$       (b)  $\{1, x, e^{-x}, xe^{-x}\}$       (c)  $\{1, x, e^x, xe^x\}$       (d)  $\{1, x, e^x, xe^{-x}\}$
- Q11. The general solution of the equation  $y'' - 6y' + 13y = 0$  is
- (a)  $e^x (c_1x^2 + c_2x + c_3)$       (b)  $e^{3x} (c_1\cos 2x + c_2\sin 2x)$       (c)  $e^x (c_1x^2 + (c_2 + c_3)x)$       (d)  $e^{2x} (c_1\sin^2 x + c_2\cos x + c_3)$
- Q12. The general solution of the equation  $\frac{d^5y}{dx^5} - \frac{d^3y}{dx^3} = 0$  is
- (a)  $c_1e^{2x} + c_2e^x + (c_3 + c_4x + c_5x^2)$       (b)  $c_1e^{-x} + c_2e^x$       (c)  $c_1e^{-x} + c_2e^x + (c_3 + c_4x + c_5x^2)e^{3x}$       (d)  $c_1e^{-x} + c_2e^x + (c_3 + c_4x + c_5x^2)$

Q13. The value of  $\frac{1}{f(D)} \cdot 1$  when  $f(D) = D^n$  is

- (a)  $\frac{x^n}{n}$  (b) 0 (c)  $\frac{x^n}{n!}$  (d) None of these

Q14. The particular integral of  $\frac{d^2y}{dx^2} + y = x^2$  is

- (a)  $x$  (b)  $x^3$  (c)  $x^2$  (d) None of these

Q15. The general solution of  $(D^2 + D - 2)y = e^x$  is

- (a)  $y = Ae^x + Be^{-2x} + \frac{1}{3}xe^x$  (b)  $y = Ae^x + Be^{-2x}$   
(c)  $y = Ae^x + Be^{-2x} + \frac{1}{6}(x^2e^x)$  (d)  $y = (A + Bx)e^{-2x} + \frac{1}{3}xe^x$

Q16. Particular integral of  $\frac{d^2y}{dx^2} + y = 1$  is

- (a) 0 (b)  $x$  (c) 1 (d)  $x^2$

Q17. The complementary function for the solution of the differential equation  $2x^2y'' + 3xy' - 3y = x^3$  is

- (a)  $Ax^2 + Bx$  (b)  $Ax^{\frac{3}{2}} + Bx^{\frac{3}{2}}$  (c)  $Ax + Bx^{\frac{3}{2}}$  (d)  $Ax + Bx^{\frac{3}{2}}$

Q18. On putting  $x = e^z$ , the transformed differential equation of  $x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + y = x$  is

- (a)  $\frac{d^2y}{dz^2} + y = e^z$  (b)  $\frac{d^2y}{dz^2} - y = e^z$  (c)  $\frac{dy}{dz} + y = e^z$  (d)  $\frac{dy}{dz} - y = e^{z^2}$

Q19. The initial solution taken by method of separation of variables for the differential equation

$$\frac{\partial u}{\partial t} = c^2 \left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) \text{ is}$$

- (a)  $u(x, t) = X(x)T(t)$  (b)  $u(y, t) = Y(y)T(t)$   
(c)  $u(x, y, t) = X(x)Y(y)T(t)$  (d)  $u(x, y, t) = X(y)Y(x)T(t)$

Q20. Which of the following represent one dimensional wave equation?

- (a)  $\left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) = 0$  (b)  $\left( \frac{\partial^2 u}{\partial x^2} - \frac{\partial^2 u}{\partial t^2} \right) = 0$  (c)  $\left( \frac{\partial^2 u}{\partial x^2} - \frac{\partial u}{\partial t} \right) = 0$  (d) None of these

Q21. Which of the following represent two dimensional Heat equation.

- (a)  $\left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) C^2 = \frac{\partial u}{\partial t}$  (b)  $\left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) C^2 = \frac{\partial^2 u}{\partial t^2}$   
(c)  $\left( \frac{\partial^2 u}{\partial x^2} - \frac{\partial u}{\partial t} \right) = 0$  (d) None of these

Q22. Which of the following is one dimensional Heat equations?;

- (a)  $\frac{\partial u}{\partial t} - \frac{\partial^2 u}{\partial x^2} = 0$  (b)  $\frac{\partial^2 u}{\partial t^2} - \frac{\partial^2 u}{\partial x^2} = 0$  (c)  $\frac{\partial^2 u}{\partial x^2} - \frac{\partial^2 u}{\partial y^2} = 0$  (d)  $\frac{\partial^2 u}{\partial t^2} + \frac{\partial^2 u}{\partial x^2} = 0$

Q23. Which of the following represents the solution of  $\frac{\partial^2 u}{\partial x^2} c^2 = \frac{\partial u}{\partial t}$ ;

$$u(0, t) = 0; u(L, t) = 0; u(x, 0) = f(x)$$

- (a)  $u(x, t) = \sum_n b_n \sin\left(\frac{n\pi x}{L}\right) e^{-\frac{n^2 \pi^2 c^2 t}{L^2}}$  (b)  $u(x, t) = \sum_n b_n \sin\left(\frac{n\pi x}{L}\right) \cos\left(\frac{n\pi ct}{L}\right)$   
(c)  $u(x, t) = \sum_n b_n \sin\left(\frac{n\pi ct}{L}\right) \cos\left(\frac{n\pi x}{L}\right)$  (d) Both (b) and (c)

Q24. The possible solution of  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$ ;

(a)  $u(x, t) = (C_1 \cos kx + C_2 \sin kx)(C_3 e^{ky} + C_4 e^{-ky})$

(b)  $u(x, t) = (C_1 + C_2 x)(C_3 + C_4 t)$

(c)  $u(x, t) = (C_1 \cos ky + C_2 \sin ky)(C_3 e^{kx} + C_4 e^{-kx})$

(d) All of the above

Q25. If The solution of  $\frac{\partial^2 u}{\partial x^2} C^2 = \frac{\partial^2 u}{\partial t^2}$ ;  $u(0, t) = 0$ ;  $u(L, t) = 0$ ;  $\left(\frac{\partial u}{\partial t}\right)_{t=0} = 0$ ;  $u(x, 0) = f(x)$

is  $u(x, t) = \sum_n b_n \sin\left(\frac{n\pi x}{L}\right) \cdot \cos\left(\frac{n\pi ct}{L}\right)$  then the value of  $b_n$  is given by

(a)  $b_n = \frac{1}{L} \int_0^L f(x) \sin\left(\frac{n\pi x}{L}\right) dx$

(b)  $b_n = \frac{1}{L} \int_0^L f(x) \sin\left(\frac{\pi x}{L}\right) dx$

(c)  $b_n = \frac{2}{L} \int_0^L f(x) \sin\left(\frac{\pi x}{L}\right) dx$

(d) None of these

Q26. The solution of  $2x \frac{\partial u}{\partial x} - 3y \frac{\partial u}{\partial y} = 0$  by separation of variable is

(a)  $u = cx^k y^k$

(b)  $u = cx^{k/2} y^k$

(c)  $u = cx^k y^{k/3}$

(d)  $u = cx^{k/2} y^{k/3}$

Q27. If The solution of  $\frac{\partial^2 u}{\partial x^2} c^2 = \frac{\partial^2 u}{\partial t^2}$ ;  $u(0, t) = 0$ ;  $u(L, t) = 0$ ;  $\left(\frac{\partial u}{\partial t}\right)_{t=0} = 0$ ;  $u(x, 0) = \sin^3\left(\frac{\pi x}{L}\right)$

is  $u(x, t) = \sum_n b_n \sin\left(\frac{n\pi x}{L}\right) \cdot \cos\left(\frac{n\pi ct}{L}\right)$  then the value of  $b_1, b_3$  is

(a)  $\frac{3}{4}, \frac{1}{4}$

(b)  $\frac{1}{4}, \frac{3}{4}$

(c)  $\frac{3}{4}, -\frac{1}{4}$

(d)  $-\frac{1}{4}, \frac{3}{4}$

Q28. If the following represents the solution of  $\frac{\partial^2 u}{\partial x^2} c^2 = \frac{\partial u}{\partial t}$ ;

$u(0, t) = 0$ ;  $u(2, t) = 0$ ;  $u(x, 0) = \sin\left(\frac{3\pi x}{2}\right) - 3\sin\left(\frac{2\pi x}{2}\right)$  is  $u(x, t) = \sum_n b_n \sin\left(\frac{n\pi x}{2}\right) \cdot e^{-\frac{n^2 \pi^2 c^2}{4} t}$  then the

value of  $b_1, b_2$  is

(a) 1, 3

(b) 3, 0

(c) 1, -3

(d) 0, -3

Q29. The solution of the equation

$\frac{\partial^2 u}{\partial x^2} C^2 = \frac{\partial^2 u}{\partial t^2}$ ;  $u(0, t) = 0$ ;  $u(l, t) = 0$ ;  $u(x, 0) = f(x)$ ;  $\left(\frac{\partial u}{\partial t}\right)_{t=0} = h(x)$  by D'Alembert's method is

(a)  $u(x, t) = \frac{1}{2} [f(x+ct) + f(x-ct)] + \frac{1}{2c} \int_{x-ct}^{x+ct} g(x) dx$

(b)  $u(x, t) = [f(x+ct) + f(x-ct)] + \frac{1}{2c} \int_{x-ct}^{x+ct} g(x) dx$

(c)  $u(x, t) = \frac{1}{2} [f(x+ct) + f(x-ct)] + \frac{1}{c} \int_{x-ct}^{x+ct} g(x) dx$

(d)  $u(x, t) = \frac{1}{2} [f(x+ct) + f(x-ct)] + \frac{1}{2} \int_{x-ct}^{x+ct} g(x) dx$



Q30. If The solution of  $\frac{\partial^2 u}{\partial x^2} c^2 = \frac{\partial^2 u}{\partial t^2}$ ;  $u(0, t) = 0$ ;  $u(\pi, t) = 0$ ;  $\left(\frac{\partial u}{\partial t}\right)_{t=0} = 0$ ;  $u(x, 0) = x$

Is  $u(x, t) = \sum_n b_n \sin nx \cos ncx t$  then the value of  $b_n$  is given by

- (a)  $\frac{(-1)^n}{n+1}$  (b)  $\frac{(-1)^{n+1}}{n}$  (c)  $2 \frac{(-1)^{n+1}}{n}$  (d) None of these

Q31. The partial differential equations obtained by eliminating the arbitrary constants a & b from  $z = (x-a)(y-b)$  is

- a)  $z = pq$  b)  $z = \frac{p}{q}$  c)  $z = p + q$  d) None of these

Q32. The partial differential equation  $u_{xx} + x^2 u_{xy} + u_y = 0$ ;  $x \neq 0$  is classified as

- (a) Parabolic (b) Elliptic (c) Hyperbolic (d) None of these

Q33. Which of the following is Laplace equation?

- a)  $\frac{\partial^2 u}{\partial x^2} = \frac{\partial u}{\partial t}$  b)  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$  c)  $\frac{\partial^2 y}{\partial t^2} = c^2 \frac{\partial^2 u}{\partial x^2}$  d) None of these

Q34. The Laplace equation is classified as

- (a) Parabolic (b) Elliptic (c) Hyperbolic (d) None of these

Q35. Laplace equation is a special case of

- (a) One dimensional Wave equation (b) One dimensional Heat equation  
(c) Two dimensional Wave equation (d) Two dimensional Heat equation

Q36. The parametric equation of the curve  $x + y + z = 8$ ,  $y - z = 0$  is

- (a)  $x = y = z = t$  (b)  $y = z = t, x = 8 - 2t$  (c)  $y = z = t, x = 8 - t$  (d) None of these

Q37. The tangent vector to the curve whose parametric representation is  $x = \cos t, y = \sin t, z = t, -\pi \leq t \leq \pi$ , is given by

- (a)  $\cos t \hat{i} + \sin t \hat{j} + t \hat{k}$  (b)  $-\sin t \hat{i} + \cos t \hat{j} + \hat{k}$   
(c)  $-\cos t \hat{i} - \sin t \hat{j} + t \hat{k}$  (d)  $\cos t \hat{i} + \sin t \hat{j} - t \hat{k}$

Q38. If  $\vec{V}(t) = (\cos t + t^2)(t\hat{i} + \hat{j} + 2\hat{k})$  then  $\vec{V}'(t)$  is

- (a)  $(3t^2 - t \sin t + \cos t)\hat{i} + (2t - \sin t)\hat{j}$  (b)  $(3t^2 - t \sin t + \cos t)\hat{i} + (2t - \sin t)\hat{k}$   
(c)  $(3t^2 - t \sin t + \cos t)\hat{i} + (2t - \sin t)(\hat{j} - 2\hat{k})$  (d)  $(3t^2 - t \sin t + \cos t)\hat{i} + (2t - \sin t)(\hat{j} + 2\hat{k})$

Q39. The length of the Helix traced by  $\vec{r}(t) = \cos t \hat{i} + \sin t \hat{j} + t \hat{k}$ ,  $0 \leq t \leq 2\pi$  is

- (a)  $2\pi$  (b)  $2\sqrt{2}\pi$  (c)  $\sqrt{2}\pi$  (d)  $2\sqrt{2}$

Q40. If the position vector of the moving particle is  $\vec{r}(t) = t^3 \hat{i} + t \hat{j} + t^2 \hat{k}$  then its speed is

- (a)  $(9t^4 + 4t^2 + 1)^{\frac{1}{2}}$  (b)  $(9t^4 - 4t^2 + 1)^{\frac{1}{2}}$  (c)  $(9t^4 + 4t^2 - 1)^{\frac{1}{2}}$  (d)  $(9t^4 - 4t^2 - 1)^{\frac{1}{2}}$

Q41. Normal vector to the curve  $x^2 + y^2 = 16$  at  $(3, 4)$  is

- (a)  $6\hat{i} - 8\hat{j}$  (b)  $6\hat{i} + 6\hat{j}$  (c)  $6\hat{i} + 8\hat{j}$  (d) None of these

Q42. The unit normal vector  $\hat{n}$  to the surface  $f(x, y, z) = k$  is given by

- (a)  $\frac{\text{grad } f}{|\text{grad } f|}$  (b)  $\frac{1}{|\text{grad } f|}$  (c)  $\frac{\text{grad } f^2}{|\text{grad } f|}$  (d) None of these

Q43. The angle between the surfaces  $f_1(x, y, z) = k_1$  and  $f_2(x, y, z) = k_2$  at any point  $(x_0, y_0, z_0)$  is given by

- (a)  $\cos \theta = \frac{(\nabla f_1)_{(x_0, y_0, z_0)} \cdot (\nabla f_2)_{(x_0, y_0, z_0)}}{\|(\nabla f_1)_{(x_0, y_0, z_0)}\| \|(\nabla f_2)_{(x_0, y_0, z_0)}\|}$  (b)  $\sin \theta = \frac{(\nabla f_1)_{(x_0, y_0, z_0)} \cdot (\nabla f_2)_{(x_0, y_0, z_0)}}{\|(\nabla f_1)_{(x_0, y_0, z_0)}\| \|(\nabla f_2)_{(x_0, y_0, z_0)}\|}$   
(c)  $\cos^{-1} \theta = \frac{(\nabla f_1)_{(x_0, y_0, z_0)} \cdot (\nabla f_2)_{(x_0, y_0, z_0)}}{\|(\nabla f_1)_{(x_0, y_0, z_0)}\| \|(\nabla f_2)_{(x_0, y_0, z_0)}\|}$  (d)  $\cos^2 \theta = \frac{(\nabla f_1)_{(x_0, y_0, z_0)} \cdot (\nabla f_2)_{(x_0, y_0, z_0)}}{\|(\nabla f_1)_{(x_0, y_0, z_0)}\| \|(\nabla f_2)_{(x_0, y_0, z_0)}\|}$

Q44. Directional derivative of  $f = xyz$  at  $(1, 4, 3)$  in the direction of line from  $(1, 2, 3)$  to  $(1, -1, -3)$  is  
 (a)  $\frac{11}{5}$  (b)  $-\frac{11}{\sqrt{5}}$  (c) 11 (d) None of these

Q45. If  $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$ , then the value of  $\text{div}(\vec{r})$  is  
 (a) 0 (b) 1 (c) 2 (d) 3

Q46. If divergence of a vector function  $\vec{F}$  is zero then it said to be  
 (a) Irrotational (b) Solenoidal (c) Conservative (d) None of these

Q47. If  $\vec{V} = x\hat{i} + y\hat{j} + z\hat{k}$ , then  $\text{curl}(\vec{V})$  is  
 (a)  $2x\hat{i} + 2y\hat{j} + 2z\hat{k}$  (b)  $x\hat{i} + y\hat{j} + z\hat{k}$  (c) 0 (d) None of these

Q48. If  $\vec{r} = x^2\hat{i} + y^2\hat{j} + z^2\hat{k}$ , then the value of  $\text{div}(\text{Curl } \vec{r})$  is  
 (a) 0 (b) 1 (c) 2 (d) 3

Q49. If  $\vec{V}$  be a differentiable vector field then the value of  $\text{div}(\text{curl } \vec{V})$  is  
 (a) -1 (b) 1 (c) 2 (d) 0

Q50. If  $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$  and  $\vec{a}$  is a constant vector then  $\text{div}(\vec{a} \times \vec{r})$  is  
 (a) 3 (b) 0 (c) 1 (d) None of these

Q51. If  $\vec{V} = (2x + 3y)\hat{i} + (x - y)\hat{j} - (x + y + z)\hat{k}$ , then  $\text{div}(\vec{V})$  is  
 (a)  $y\hat{i} + z\hat{j} + x\hat{k}$  (b) 0 (c)  $(2\hat{i} - \hat{k})$  (d) None of these

Q52. Let  $f$  be a differentiable scalar field then  $\text{curl}(\text{grad } f)$  is  
 a)  $\vec{0}$  b) 1 c) 2 d) None of these

Q53. The value of line integral  $\int_C (x^2 y dx + x^2 dy)$ , where C is the boundary described counter clockwise of the triangle with vertices  $(0, 0)$ ,  $(1, 0)$ ,  $(1, 1)$  {By using of green's theorem} is  
 a)  $-\frac{5}{12}$  b)  $\frac{12}{5}$  c)  $\frac{5}{12}$  d)  $-\frac{12}{5}$

Q54. The value of line integral  $\int_C (x^2 + xy)dx + (x^2 + y^2)dy$ , where C is the square formed by  $x = \pm 1$ ,  $y = \pm 1$  {By using of green's theorem} is  
 a) 0 b) -1 c) 1 d) None of these

Q55. The value of  $\iiint_V \text{Div } \vec{F} dv$ , where  $\vec{F} = 3x\hat{i} + 4y\hat{j} + 5z\hat{k}$  over the region bounded by the sphere  $x^2 + y^2 + z^2 = 1$  is  
 a)  $\frac{3584}{3}\pi$  b)  $\frac{3584}{4}\pi$  c)  $-\frac{3584}{3}\pi$  d) None of these

Q56. The value of  $\oint_C x^2 z dx + 3x dy - y^3 dz$ , where C is  $x^2 + y^2 = 1$   
 a)  $3\pi$  b)  $-3\pi$  c)  $\pi$  d) None of these

Q57. By using stock's theorem the value of the  $\int_C x^2 dx + y^2 dy + z^2 dz$  is, where C is  $x > 0, y > 0, x + y = 1$   
 a) 2 b) 1 c) -1 d) None of these.

(By green's theorem) is

- a) 2                  b) 1                  c) 0                  d) None of these

**Q59.** If  $\phi(x, y), \psi(x, y), \frac{\partial \phi}{\partial y}, \frac{\partial \psi}{\partial x}$  are continuous function over a region R bounded by simple closed curve C in x-y plane, then according to Greens theorem

- $$\begin{aligned} \text{a) } \oint_C (\psi dx + \phi dy) &= \iint_R \left( \frac{\partial \psi}{\partial x} - \frac{\partial \phi}{\partial y} \right) dx dy \\ \text{b) } \oint_C (\psi dx - \phi dy) &= \iint_R \left( \frac{\partial \psi}{\partial x} - \frac{\partial \phi}{\partial y} \right) dx dy \\ \text{c) } \oint_C (\phi dx + \psi dy) &= \iint_R \left( \frac{\partial \psi}{\partial x} - \frac{\partial \phi}{\partial y} \right) dx dy \\ \text{d) } \oint_C (\phi dx - \psi dy) &= \iint_R \left( \frac{\partial \psi}{\partial x} - \frac{\partial \phi}{\partial y} \right) dx dy \end{aligned}$$

**Q60.** By using stoke's theorem the value of the  $\int_C (2x - y)dx - yz^2 dy - y^2 z dz$  is, where c is

- $x^2 + y^2 = 1$
- a)  $-\pi$       b)  $\pi$       c)  $\pi/2$       d) None of these

Q61. If  $\iint_S (\vec{F} \cdot \hat{n}) dS = 0$  then  $\vec{F}$  is .....

- a) Irrotational vector  
b) Solenoidal vector  
c) Both solenoidal and irrotational  
d) None of these

**Q62.** By using stoke's theorem the value of the  $\int_C xdx + ydy + zdz$  is, where c is  $x^2 + y^2 = 1$

- a) 0                  b) 1                  c) -1                  d) None of these

**Q63.** The value of line integral  $\int_C (x dx + y dy)$ , where C is the region bounded by  $0 \leq x \leq 1, 0 \leq y \leq 1$  (By green's theorem) is

- a) 1                  b) -1                  c) 0                  d) None of these

**Q64.** Which of the following is the mathematical expression of stokes' theorem

- a)  $\oint \vec{F} \cdot d\vec{r} = \iint_S \text{Curl } \vec{F} \cdot d\vec{s}$       b)  $\oint \vec{F} \cdot d\vec{r} = \iint_S \text{Curl } \vec{F} \cdot \vec{n} \, ds$   
c)  $\oint \vec{F} \cdot \vec{n} \, d\vec{r} = \iint_S \text{Curl } \vec{F} \, ds$

**Q65.** The  $\iint \text{curl } \vec{v} \cdot \hat{n} \, ds$ , where  $\vec{v} = y\hat{i} + z\hat{j} + x\hat{k}$  and  $s$  is the surface  $z = 1 - x^2 - y^2, z \geq 0$ , is

- a)  $-\pi$   
b)  $\pi$   
c)  $\pi/2$   
d) None of these



Q66. Green's Theorem is a special case of ;

- a) Stoke's Theorem
- b) Gauss Theorem
- c) All of the above
- d) None of these

Q67. The mathematical form of Gauss divergence theorem is

- a)  $\oint \vec{F} \cdot d\vec{r} = \iint_S \text{Curl } \vec{F} \cdot d\vec{s}$
- b)  $\oint \vec{F} \cdot d\vec{r} = \iint_S \text{Curl } \vec{F} \cdot \hat{n} \, ds$
- c)  $\oint \vec{F} \cdot \hat{n} \, ds = \iiint_V \text{div } \vec{F} \, dv$
- d) None of these

Q68. The work done in moving a particle by the force field  $\vec{A} = 3x^2\hat{i} - y\hat{j} + z\hat{k}$  along (0,0,0) to (2,1,3) is

- a) 10
- b) 11
- c) 12
- d) 13

Q69. Stoke's Theorem gives the relationship between ;

- a) Surface and volume integral
- b) Line and volume integral
- c) Line and surface integral
- d) None of these

Q70. The value of  $\iiint_V \text{Div } \vec{A} \, dv$ , where  $\vec{A} = 3y^3\hat{i} + 4z^3\hat{j} + 5x^3\hat{k}$  over the region bounded by the

sphere  $x^2 + y^2 + z^2 = 1$  is

- a) 1
- b) 0
- c) -1
- d) None of these