

MCQ Practice sheet

Unit 5

Set1

1. $U=x+y$, $x=t$, $y=t^2$, find dU/dt
 - a. $1+2t$
 - b. $t+2$
 - c. T
 - d. $2-t$
2. If $z=x^3+y^3-3axy$, find $\frac{\partial z}{\partial x}$
 - a. $3x^2-3ay$
 - b. $3x^2+3ay$
 - c. x^2-3ay
 - d. none of these
3. If $u = \frac{x+y}{\sqrt{x}+\sqrt{y}}$, which of the following is correct
 - a. u is homogeneous function with degree $1/2$
 - b. u is not homogeneous function
 - c. u is homogeneous function with degree 1
 - d. u is homogeneous function with degree $-1/2$
4. If $\log u = \frac{x+y}{\sqrt{x}+\sqrt{y}}$, which of the following is correct
 - a. $\log u$ is homogeneous function with degree $1/2$
 - b. u is homogeneous function with degree $1/2$
 - c. u is homogeneous function with degree $-1/2$
 - d. u is not homogeneous function
5. To find extreme value of $x^2+y^2+z^2$ such that $Ax+By+Cz=D$, which of the following is correct
 - a. $\frac{\partial F}{\partial x} = 0, \frac{\partial F}{\partial y} = 0, \frac{\partial F}{\partial z} = 0$ where $F = x^2+y^2+z^2 + \lambda(Ax+By+Cz-D)$
 - b. $\frac{\partial F}{\partial x} = 0, \frac{\partial F}{\partial y} = 0, \frac{\partial F}{\partial z} = 0$ where $F = x^2+y^2+z^2 + \lambda(Ax+By+Cz=D)$
 - c. $\frac{\partial F}{\partial x} = 0, \frac{\partial F}{\partial y} = 0, \frac{\partial F}{\partial z} = 0$ where $F = x^2+y^2+z^2 + Ax+By+Cz-D$
 - d. $\frac{\partial F}{\partial x} = 0, \frac{\partial F}{\partial y} = 0, \frac{\partial F}{\partial z} = 0$ where $F = (x^2+y^2+z^2)(Ax+By+Cz=D)$
6. The minimum value of the function $x^2+y^2+z^2$ subject to the condition $xyz=a^3$ if $x^2 = y^2 = z^2$ is obtained by Lagrange's method is
 - a. $3a^2$
 - b. a^2
 - c. $6a^2$
 - d. none of these

SET 2

1.

If $u = \frac{y^3-x^3}{y^2+x^2}$ then $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2}$ is

- (a) $3u$ (b) $2u$ (c) u (d) 0

2.If $F(x,y)$ is a homogeneous function of degree n in x and y and has continuous first and second order partial derivatives then

a) $x^2 \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial x \partial y} + y^2 \frac{\partial^2 f}{\partial y^2} = n(n-1)f$

b) $x^2 \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial x \partial y} + y^2 \frac{\partial^2 f}{\partial y^2} = nf$

c) $x^2 \frac{\partial^2 f}{\partial x^2} + 2xy \frac{\partial^2 f}{\partial x \partial y} + y^2 \frac{\partial^2 f}{\partial y^2} = n(n-1)f$

d) $x^2 \frac{\partial^2 f}{\partial x^2} + 2xy \frac{\partial^2 f}{\partial x \partial y} + y^2 \frac{\partial^2 f}{\partial y^2} = n(n-1)f$

3.

If $r = \frac{\partial^2 f}{\partial x^2}(a, b)$, $s = \frac{\partial^2 f}{\partial x \partial y}(a, b)$, $t = \frac{\partial^2 f}{\partial y^2}(a, b)$, then $f(x, y)$ will have a maxima at (a, b) if

a) $rt > s^2$, and $r < 0$

b) $rt > s^2$, and $r > 0$

c) $rt = s^2$, and $r < 0$

d) $rt = s^2$, and $r > 0$

4.

For the function $f(x, y) = 2(x^2 - y^2) - x^4 + y^4$ the critical point $(1, 0)$ is a point of

a) Maxima

b) Minima

c) saddle point

d) None of these

5.

If $x = \cos \theta$, $y = \sin \theta$ then $\frac{\partial(x, y)}{\partial(r, \theta)}$ is

(a) 0 (b) 1 (c) 2 (d) 3

6.

If $f(x, y) = x^3 + y^3 + x$ then $\frac{\partial f}{\partial x}$ & $\frac{\partial f}{\partial y}$ is

a) $3x^2 + 3y^2 + 1, 3y^2 + 1$

b) $3x^2 + 1, 3y^2$

c) $x^2 + 1, y^2$

d) $3x^2, y^2$

7.

Total derivative of $z = \tan^{-1}\left(\frac{x}{y}\right)$, $(x, y) \neq (0, 0)$ is

a) $\frac{ydx + ydy}{x^2 + y^2}$

b) $\frac{ydx - xdy}{x^2 + y^2}$

c) $ydx - xdy$

d) $ydx + xdy$

8.

If $w = x^2 + y^2$, $x = \frac{t^2 - 1}{t}$, $y = \frac{t}{t^2 + 1}$ then $\frac{dw}{dt}$ at $t = 1$ is

(a) 0 (b) 1 (c) 2 (d) 3

9. If $F(x_1, x_2, x_3, \dots, x_n, \lambda_1, \lambda_2, \lambda_3, \dots, \lambda_k) =$

$f(x_1, x_2, x_3, \dots, x_n) + \sum_{i=1}^k \lambda_i \phi_i(x_1, x_2, x_3, \dots, x_n)$

The necessary conditions to determine the stationary points of F

(a) $\frac{\partial F}{\partial x_1} = 0 = \frac{\partial F}{\partial x_2} = \frac{\partial F}{\partial x_3} = \dots = \frac{\partial F}{\partial x_n}$

(b) $\frac{\partial F}{\partial x_1} = \frac{\partial F}{\partial x_2} = \frac{\partial F}{\partial x_3} = \dots = \frac{\partial F}{\partial x_n}$

(c) $\frac{\partial F}{\partial x_1} = 0 = -\frac{\partial F}{\partial x_2} = -\frac{\partial F}{\partial x_3} = \dots = -\frac{\partial F}{\partial x_n}$

(d) $\frac{\partial F}{\partial x_1} = 0 = \frac{\partial F}{\partial x_2} = \frac{\partial F}{\partial x_3} = \dots = -\frac{\partial F}{\partial x_n}$

10. If $f(x,y) = \sqrt{a^2 - x^2 - y^2}$, critical point (x,y) is $(0,0)$, this is a point of
 (a) relative minimum (b) relative maximum (c) neither maximum or minimum (d) saddle point

11. If $z = f(x,y)$ where $x = g(t)$, $y = h(t)$ then $\frac{dz}{dt}$ is equal to

- (a) $\frac{\partial z}{\partial x} \frac{dx}{dt} + \frac{\partial z}{\partial y} \frac{dy}{dt}$ (b) $\frac{\partial z}{\partial x} \frac{dx}{dt} - \frac{\partial z}{\partial y} \frac{dy}{dt}$ (c) $\frac{\partial z}{\partial x} \frac{dx}{dt} + \frac{\partial z}{\partial y} \frac{dy}{dt}$ (d) $\frac{\partial z}{\partial x} \frac{dx}{dt} + \frac{\partial z}{\partial y} \frac{dy}{dt}$

12. If $z = \sqrt{xy}$ then $\frac{\partial^2 z}{\partial x \partial y}$ is equal to

- (a) $4z$ (b) $\frac{4}{z}$ (c) $\frac{z}{4}$ (d) $\frac{1}{4z}$

13. The function $f(x,y) = \begin{cases} \frac{2x(x^2-y^2)}{x^2+y^2}, & (x,y) \neq (0,0) \\ 0, & (x,y) = (0,0) \end{cases}$

- (a) continuous at $(x,y) = (0,0)$ (b) not continuous at $(x,y) = (0,0)$
 (c) limit does not exist (d) none of these

14. The value of the $\lim_{(x,y) \rightarrow (0,0)} \frac{xy}{x^2+2y^2}$, $x \neq 0, y \neq 0$ is

- (a) 0 (b) 1 (c) limit does not exist (d) -1

15. If $u = x(1+y)$, $v = xy$ then value of Jacobian $\frac{\partial(u,v)}{\partial(x,y)}$ is

- (a) $-x$ (b) x (c) y (d) $-y$

SET3

1.

If $f(x,y) = x^4 - x^2y^2 + y^4$ then $\frac{\partial f}{\partial x}$ at $(-1,1)$ is

- (a) -2 (b) 2 (c) 1 (d) -1

2.

If $z = \log \left[\frac{x^2 - y^2}{x^2 + y^2} \right]$, then $x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y}$ is

- (a) 0 (b) z (c) $2z$ (d) $3z$

3.

If $\cot^{-1}\left(\frac{x}{y}\right) + y^3 + 1 = 0, x > 0, y > 0$ then $\frac{dy}{dx}$ is

- a) $\frac{y}{x+3y^2(x^2+y^2)}$ b) $\frac{x}{x+3y^2(x^2+y^2)}$ c) $\frac{1}{x+3y^2}$ d) $\frac{y}{x+3x^2(x^2+y^2)}$

4. If $r = f_{xx}(u, v)$, $s = f_{xy}(u, v)$, $t = f_{yy}(u, v)$ then if $rt - s^2 < 0$ then $f(x, y)$ has no Maximum or minimum at this point (u, v) , then the point is called

- (a) Saddle point (b) Maximum point (c) Minimum Point (d) none of these

5. If $x = r \cos \theta, y = r \sin \theta$ then $\frac{\partial(x, y)}{\partial(r, \theta)}$

- (a) 1 (b) r (c) 0 (d) $\frac{1}{r}$

6. If $z = f(x, y)$, $x = x(r, s)$, $y = y(r, s)$ then $\frac{\partial z}{\partial r}$ is equal to

- (a) $\frac{\partial z}{\partial x} \frac{\partial x}{\partial r} + \frac{\partial z}{\partial y} \frac{\partial y}{\partial r}$ (b) $\frac{\partial z}{\partial x} \frac{\partial x}{\partial s} + \frac{\partial z}{\partial y} \frac{\partial y}{\partial s}$ (c) $\frac{\partial z}{\partial x} \frac{\partial x}{\partial r} + \frac{\partial z}{\partial y} \frac{\partial y}{\partial s}$ (d) $\frac{\partial z}{\partial x} \frac{\partial x}{\partial s} + \frac{\partial z}{\partial y} \frac{\partial y}{\partial r}$

7. If $f(x, y) = x^2 + y^2 + 2bxy$, the critical point (x, y) is $(0, 0)$ is a point of minimum, so the minimum value at $(0, 0)$ is

- (a) 0 if $|b| = 1$ (b) 0 if $|b| < 1$ (c) 0 if $b > 1$ (d) 0 if $|b| > 1$

8. If $f(x, y) = 4x^2 + 9y^2 - 8x - 12y + 4$, the critical point (x, y) is $(1, \frac{2}{3})$, this is a point of

- (a) relative minimum (b) relative maximum (c) neither maximum or minimum (d) saddle point

9.

If $u = x^3 + y^3$, then $\frac{\partial^2 u}{\partial x^2}$ is

- a) $3x^2$ b) $6x$ c) 6 d) 0

10.

If $u = \frac{x^3 + y^3}{x + y}$, $(x, y) \neq (0, 0)$, then $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$ is

- (b) $3u$ (b) $2u$ (c) u (d) 0

11.

If $u = \cos^{-1}\left[\frac{x+y}{\sqrt{x}+\sqrt{y}}\right]$, $0 < x < 1$, then $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$ is

- a) 0 b) $2u$ c) $-\frac{1}{2} \cot u$ d) None of these

12. If $f(x,y) = 3x^2 + y^2 - x$ then the critical point (x,y) is

(a) $\left(-\frac{1}{6}, 0\right)$ (b) $\left(-\frac{1}{6}, 1\right)$

(c) $\left(\frac{1}{6}, 1\right)$ (d) $\left(\frac{1}{6}, 0\right)$

13. If $x = r \cos \theta, y = r \sin \theta$ then $\frac{\partial(r\theta)}{\partial(x,y)}$

(b) 1 (b) r (c) 0 (d) $\frac{1}{r}$

14. Which of the following is not homogeneous function

(a) $\tan^{-1} \left[\frac{x}{y} \right]$ (b) $\frac{x^3 + y^3}{x-y}$ (c) $\frac{y^3 - x^3}{x^2 + y^2}$ (d) $\cos^{-1} \left[\frac{x+y}{x^2 + y^2} \right]$

15. If $u = x^2y + 2y^2x$ then the value of $\frac{\partial^2 u}{\partial x \partial y}$ is equal to

(a) $2x + y$ (b) $2x + 2y$ (c) $2x + 4y$ (d) $x + 4y$

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$f(x,y) = \frac{\sqrt{x^2 + y^2}}{x}$ is a homogeneous function of degree

(b) 0 (b) 1 (c) 2 (d) -1

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If $u = \cos^{-1} \left[\frac{x}{y} \right]$ then $\frac{\partial u}{\partial x}$ equals to

(a) $\frac{1}{\sqrt{y^2 - x^2}}$ (b) $\frac{-1}{\sqrt{y^2 - x^2}}$ (c) $\frac{1}{\sqrt{x^2 - y^2}}$ (d) none of these

18. The function

$$f(x,y) = \begin{cases} \frac{xy}{x^2 + 2y^2}, & (x,y) \neq (0,0) \\ 0, & (x,y) = (0,0) \end{cases}$$

(a) continuous at $(x,y) = (0,0)$ (b) not continuous at $(x,y) = (0,0)$ (c) limit does not exist (d) none of these

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The function

$f(x,y) = \begin{cases} \frac{\sin^{-1}(x+2y)}{\tan^{-1}(2x+4y)}, & (x,y) \neq (0,0) \\ \end{cases}$ is continuous at $(x,y) = (0,0)$, the value of $f(x,y)$ at $(0,0)$ is

(a) 0 (b) -1 (c) $\frac{1}{2}$ (d) does not exist

Set4

1. The value of $\lim_{(x,y) \rightarrow (0,0)} \frac{x}{\sqrt{x^2 + y^2}}$ is

- (a) $\frac{1}{2}$ (b) does not exist (c) $\frac{1}{4}$ (d) none of these.

2. The value of $\lim_{(x,y) \rightarrow (0,0)} \frac{xy^2}{x^2 + y^4}$ is

- (a) $\frac{1}{2}$ (b) does not exist (c) $\frac{1}{4}$ (d) none of these.

3. The value of $\lim_{(x,y) \rightarrow (0,1)} \frac{(y-1)\sin x}{x \log y}$ is

- (a) 1 (b) $\frac{1}{2}$ (c) does not exist (d) none of these.

4. If $f(x, y) = \begin{cases} \frac{xy}{x^2 + y^2} & , (x, y) \neq (0, 0) \\ 0 & , (x, y) = (0, 0) \end{cases}$ then

- (a) $f(x, y)$ is not continuous at (0,0) (b) $f(x, y)$ is not defined at (0,0) (c) $f(x, y)$ is continuous at (0,0) (d) none of these

5. If $f(x, y) = x^y$ then $f_y(x, y)$ is

- (a) 0 (b) yx^{y-1} (c) $x^y \log x$ (d) xy^{x-1}

7. If $w = xyz$, $x = t$, $y = (t+1)$, $z = e^t$ then $\frac{dw}{dt}$ at $t = 0$ is

- (a) 1 (b) 2 (c) 3 (d) 0

8. If $f(x, y) = \frac{x}{\sqrt{x^2 + y^2}}$ then $f_x(1, 1)$

- (a) 4 (b) $\frac{1}{4}$ (c) 2 (d) $\frac{1}{2\sqrt{2}}$

9. If $u = \cos^{-1} \left(\frac{\sqrt{x^2 + y^2}}{x + y} \right)$ then $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$ is

- (a) 0 (b) $\frac{1}{2}$ (c) 1 (d) 2

10. If $r = f_{xx}(a, b)$, $s = f_{xy}(a, b)$, $t = f_{yy}(a, b)$ then $f(x, y)$ will have the minimum value at (a, b) if

- (a) $f_x = 0, f_y = 0, rt - s^2 < 0$ and $r < 0$
 (b) $f_x = 0, f_y = 0, rt - s^2 > 0$ and $r > 0$
 (c) $f_x = 0, f_y = 0, rt - s^2 > 0$ and $r < 0$
 (d) $f_x = 0, f_y = 0, rt - s^2 < 0$ and $r > 0$

11. If $f(x, y) = y^2 e^{\frac{x}{y}}$ then $f_y(1, 1)$ is
 (a) $2e^{1/2}$ (b) e (c) $\frac{2}{e}$ (d) $\frac{4}{\sqrt{e}}$
12. If $f(x, y) = x^2 \cot^{-1}\left(\frac{y}{x}\right)$ then it is homogeneous function of degree
 (a) 1 (b) 0 (c) 2 (d) none of these
13. If $f(x, y, z) = e^{\frac{y}{x^2}} + \log\left(\frac{y}{z}\right)$ then $f_x(1, 1, 1)$ is
 (a) $\frac{1}{2}$ (b) $\frac{1}{3}$ (c) 1 (d) none of these
14. If $x^3 + y^3 + 3xyz = 1$ then value of $\left(\frac{\partial y}{\partial x}\right)_z$ is
 (a) $\frac{x^2 + yz}{y^2 + xz}$ (b) $-\frac{x^2 + yz}{y^2 + xz}$ (c) $\frac{x^2}{xz}$ (d) none of these
15. Which of the following function is a homogeneous function of degree = -2
 (a) $\frac{1}{x^2 + y^2}$ (b) $x^2 + y^2$ (c) $\frac{1}{x - y^2}$ (d) $\frac{1}{xy + y}$

UNIT 6

Set1

1. Area enclosed by $y=f_1(x)$ and $f_2(x)$ and $b \leq x \leq a$ is given by
 a. $\int_{x=a}^{x=b} \int_{y=f_1(x)}^{y=f_2(x)} dx dy$
 b. $\int_{x=a}^{x=b} \int_{y=f_1(x)}^{y=f_2(x)} z dx dy$
 c. $\int_{x=a}^{x=b} \int_{y=a}^{y=b} dx dy$
 d. None of these
2. Evaluate $\int_{x=0}^{x=1} \int_{y=0}^{y=2} x dx dy$
 a. 1 b. 2 c. 3 d. 4
3. Evaluate $\int_{x=0}^{x=1} \int_{y=0}^{y=2} \int_{z=0}^3 dz dx dy$
 a. 6 b. 3 c. 2 d. 1
4. Find area enclosed by $x^2 + y^2 = 4, x \geq 0, y \geq 0$
 a. π b. 2π c. 3π d. 4π
5. Find volume of $x^2 + y^2 + z^2 = 1, x \geq 0, y \geq 0, z \geq 0$
 a. $\pi/3$ b. $2/3\pi$ c. $3\pi/2$ d. $4\pi/3$

6. Which of the following is correct

a. $\iint dxdy = \iint r dr d\theta$

b. $\iint dxdy = \iint 2r dr d\theta$

c. $\iint dxdy = \iint r^2 dr d\theta$

d. $\iint dxdy = \iint r \cos \theta dr d\theta$

7. Change the order of $\int_{x=0}^{x=u} \int_{y=\sqrt{ax}}^{y=u} dxdy$

a. $\int_{y=0}^{y=a} \int_{x=0}^{x=y^2/a} dxdy$

b. $\int_{y=0}^{y=a} \int_{x=a}^{x=y^2/a} dxdy$

c. $\int_{y=0}^{y=1} \int_{x=0}^{x=y^2/a} dxdy$

d. None of these

8. Volume bounded by $x^2+y^2=4$ and $y+z=4, z=0$ is given by

a. $\int_{y=-2}^{y=2} \int_{x=-\sqrt{4-y^2}}^{x=\sqrt{4-y^2}} \int_{z=0}^{4-y} dz dxdy$

b. $\int_{y=0}^{y=2} \int_{x=-\sqrt{4-y^2}}^{x=\sqrt{4-y^2}} \int_{z=0}^{4-y} dz dxdy$

c. $\int_{y=-2}^{y=2} \int_{x=0}^{x=\sqrt{4-y^2}} \int_{z=0}^{4-y} dz dxdy$

d. None of these

Set 2

1. The value of integral $\int_0^2 \int_1^3 xy dy dx$ is (a) 2 (b) 4 (c) 8 (d) 0

2. $\int_0^1 \int_0^y e^y dx dy$ is (a) 1 (b) 0 (c) 2 (d) -1

3. $\int_1^2 \int_0^1 2x e^{x^2} dx dy$ is (a) $e+1$ (b) e (c) $-e$ (d) $e-1$

4. $\int_0^1 \int_0^y e^{\frac{x}{y}} dx dy$ is (a) $\frac{1}{2}[e+1]$ (b) $\frac{1}{2}e$ (c) $-\frac{1}{2}e$ (d) $\frac{1}{2}[e-1]$

5. The value of integral $\int_0^{\frac{\pi}{2}} \int_a^{a(1+\cos\theta)} r dr d\theta$

(a) $(\pi+8)\frac{a^2}{4}$ (b) $(\pi+8)\frac{a^2}{2}$ (c) $-(\pi+8)\frac{a^2}{4}$ (d) $-(\pi+8)\frac{a^2}{2}$

6. $\int_0^1 \int_0^{x^2} x e^y dy dx$ is (a) $e-1$ (b) $\frac{1}{2}e-1$ (c) $1-e$ (d) $\frac{1}{2}e$

7. To change Cartesian coordinates (x,y,z) to cylindrical coordinates (r, θ , z) $dxdydz$ is replaced

(a) $r d\theta dz$ (b) $r dr d\theta dz$ (c) $r \sin \theta dr d\theta dz$ (d) $\sin \theta dr d\theta dz$

8. After changing the order of integration, the integral $\int_{-a}^a \int_0^{\sqrt{a^2-y^2}} f(x,y) dxdy$

(a) $\int_{-a}^a \int_{-\sqrt{a^2-x^2}}^{\sqrt{a^2-x^2}} f(x,y) dy dx$

(b) $\int_0^a \int_0^{\sqrt{a^2-x^2}} f(x,y) dy dx$

(c) $\int_{-a}^a \int_0^{\sqrt{a^2-x^2}} f(x,y) dy dx$

(d) $\int_0^a \int_{-\sqrt{a^2-x^2}}^{\sqrt{a^2-x^2}} f(x,y) dy dx$

9. After changing to polar coordinates, the integral $\int_0^{2a} \int_0^{\sqrt{2ax-x^2}} dxdy$

(a) $\int_0^{\frac{\pi}{2}} \int_0^{2a \cos \theta} r d\theta dr$

(b) $\int_0^{\pi} \int_0^a \cos \theta r d\theta dr$

(c) $\int_0^{\frac{\pi}{2}} \int_0^a \cos \theta \, r \, d\theta \, dr$ (d) $\int_0^{\pi} \int_0^{2a \cos \theta} r \, d\theta \, dr$

10. After changing the order of integration, the integral $\int_0^a \int_x^a f(x, y) \, dx \, dy$

(a) $\int_0^a \int_0^y f(x, y) \, dy \, dx$ (b) $\int_0^a \int_0^x f(x, y) \, dy \, dx$
 (c) $\int_0^a \int_0^y f(x, y) \, dy \, dx$ (d) $\int_{-a}^a \int_0^y f(x, y) \, dy \, dx$

11. The value of the integral $\int_0^a \int_0^b \int_0^c x^2 y^2 z^2 \, dz \, dy \, dx$ is (a) $\frac{abc}{9}$ (b) $\frac{a^2 b^2 c^2}{27}$ (c) $\frac{a^3 b^3 c^3}{27}$ (d) $\frac{a^2 b^2 c^2}{9}$

12. After changing the order of integration the integral $\int_0^1 \int_0^{\sqrt{1-x^2}} (x+y) \, dy \, dx$

$\int_0^1 \int_0^{\sqrt{1-y^2}} (x+y) \, dx \, dy$ (b) $\int_0^2 \int_0^{\sqrt{1-y^2}} (x+y) \, dx \, dy$
 (c) $\int_0^1 \int_0^{\sqrt{1+y^2}} (x+y) \, dx \, dy$ (d) $\int_0^{-1} \int_0^{\sqrt{1-y^2}} (x+y) \, dx \, dy$

13. Evaluate

$\int_0^{\infty} \int_0^{\infty} e^{-(x^2+y^2)} \, dx \, dy$ by changing to polar coordinates. (a) $\int_{\theta=0}^{\frac{\pi}{2}} \int_{r=0}^{\infty} e^{-(r^2)} r \, dr \, d\theta$ (b) $\int_{\theta=0}^{\frac{\pi}{2}} \int_{r=0}^{\infty} e^{-(r^2)} r$

(c) $\int_{\theta=0}^{\frac{\pi}{2}} \int_{r=0}^{\infty} e^{-(r^2)} \, dr \, d\theta$ (d) $\int_{\theta=0}^{\frac{\pi}{2}} \int_{r=0}^{\infty} e^{(r^2)} \, dr \, d\theta$

14. The area bounded by circle $x^2 + y^2 = 16$ is 16π (b) π (c) 8π (d) 4π

15. Evaluate the integral $\iiint dxdydz$ along R where R is hemisphere of radius a ,

$x^2 + y^2 + z^2 = a^2$ is (a) πa^3 (b) $\frac{\pi a^3}{6}$ (c) $\frac{2\pi a^3}{3}$ (d) $\frac{\pi a^3}{3}$

SET3

1. The value of integral $\int_1^0 \int_0^1 (x^2 + y^2) \, dx \, dy$ is (a) $\frac{2}{3}$ (b) $-\frac{2}{3}$ (c) $\frac{1}{3}$ (d) $-\frac{1}{3}$

2. The value of integral $\int_{-b}^b \int_0^{\sqrt{a^2-y^2}} dy \, dx$ is
 $-b\sqrt{a^2-y^2}$ (b) $-2b\sqrt{a^2-y^2}$ (c) $b\sqrt{a^2-y^2}$ (d) none of these

3. $\int_{-b}^b \int_0^y dx \, dy$ is (a) 1 (b) 0 (c) 2 (d) -1

4. The value of the integral $\int_0^{\pi} \int_{2 \sin \theta}^4 \sin \theta \, r^3 \, dr \, d\theta$ is (a) $-\frac{45}{2}\pi$ (b) $\frac{25}{2}\pi$ (c) $\frac{45}{2}\pi$ (d) $-\frac{25}{2}\pi$

5. The value of integral $\int_0^{\pi} \int_0^{a(1+\cos \theta)} dr \, d\theta$ is (a) $-a\pi$ (b) $a\pi$ (c) $\frac{\pi}{2}$ (d) $-\frac{\pi}{2}$

6. The value of the integral $\int_0^2 \int_1^3 \int_1^2 x y^2 z \, dz \, dy \, dx$ is (a) 23 (b) 26 (c) 22 (d) 21

7. To change Cartesian coordinates (x,y) to Polar coordinates (r,θ) $dxdy$ is replaced by

(a) $r \, dr \, d\theta$ (b) $dr \, d\theta$ (c) $r \sin \theta \, dr \, d\theta$ (d) $\sin \theta \, dr \, d\theta$

8. The value of $\int_0^1 \int_x^{\sqrt{x}} xy \, dx \, dy$ is (a) Zero (b) $-\frac{1}{24}$ (c) 24 (d) $\frac{1}{24}$

9. Area between the parabolas $y^2 = 4x$ and $x^2 = 4y$ is (a) $\frac{6}{3}$ (b) $\frac{26}{3}$ (c) $\frac{16}{3}$ (d) $\frac{6}{13}$

10. evaluate $\iint dxdy$ over the area bounded by $x = 0, y = 0, 5y = 3, x^2 + y^2 = 1$
 $\frac{6}{5} + \frac{1}{2} \sin \frac{3}{5}$ (b) $\frac{6}{25} + \frac{1}{2} \sin \frac{3}{15}$ (c) $\frac{6}{25} + \frac{1}{2} \sin \frac{3}{5}$ (d) $\frac{6}{25} - \frac{1}{2} \sin \frac{3}{5}$

11. The value of the integral $\int_{-1}^1 \int_0^z \int_{x-z}^{x+z} dy \, dx \, dz$ is (a) 0 (b) $\frac{4}{3}$ (c) $-\frac{4}{3}$ (d) $\frac{2}{3}$

12. The value of the integral $\int_0^a \int_0^b \int_0^c (x^2 + y^2 + z^2) \, dx \, dy \, dz$

(a) $\frac{abc}{3} [a^2 + b^2 + c^2]$ (b) $\frac{a^2 b^2 c^2}{27} [a^2 + b^2 + c^2]$ (c) $\frac{a^3 b^3 c^3}{27} [a^2 + b^2 + c^2]$ (d) $\frac{a^2 b^2 c^2}{9} [a^2 + b^2 + c^2]$

13. $\int_0^2 \int_0^x e^{x^2} dy dx$ is (a) $\frac{1}{4} [e^4 + 1]$ (b) $\frac{1}{2} [e^4 - 1]$ (c) $\frac{1}{4} [e^4 - 1]$ (d) none of these

14. The cylinder $x^2 + z^2 = 1$ is cut by planes $z = 0, y = 0, x = y$. the volume of the region in first octant is

(a) $\frac{1}{3}$ (b) $\frac{2}{3}$ (c) $-\frac{2}{6}$ (d) $\frac{2}{16}$

15. Volume of sphere $x^2 + y^2 + z^2 = 1$ is given as

(a) $8 \int_0^1 \int_0^{\frac{\pi}{2}} \int_0^{\frac{\pi}{2}} r^2 \sin \theta dr d\theta d\phi$ (b) $8 \int_0^a \int_0^{\frac{\pi}{2}} \int_0^{\frac{\pi}{2}} r^2 \sin \theta dr d\theta d\phi$

(c) $8 \int_{-1}^1 \int_0^{\frac{\pi}{2}} \int_0^{\frac{\pi}{2}} r^2 \sin \theta dr d\theta d\phi$ (d) none of these

U4 unit 4 Fourier series practice problems

For the function $f(x) = x^2, -2 \leq x \leq 2$ the value of b_n in Fourier series expansion will be

(a) $\frac{8}{3}$ (b) 0 (c) $\frac{16}{3}$ (d) none of these **Ans-b**

For the function $f(x) = x^3, -\pi \leq x \leq \pi$ the value of a_n in Fourier series expansion will be

(a) $\frac{2}{\pi}$ (b) 2π (c) 0 (d) none of these **Ans-c**

Fourier series what is the value of Fourier coefficient for a_0 on $[-l, l]$

(a) $\frac{2}{l} \int_0^l f(x) dx$ (b) $\frac{1}{l} \int_{-l}^l f(x) dx$ (c) $\frac{2}{l} \int_{-l}^l f(x) dx$ (d)

$\frac{2}{l} \int_0^l f(x) \cos\left(\frac{n\pi x}{l}\right) dx$ **Ans- b**