

## Topic - Rotation Algorithms / Techniques

Rotation is some of the basic operations that we perform on array, There are multiple ways to perform rotation on array.

- One by One Rotation
- Reversal Algorithm
- Juggling Algorithm

### One By One Rotation Technique

#### Introduction

The method for rotating the elements of an array in a circular fashion. It shifts the elements of the array one position to the left or right, depending on the direction of rotation.

#### Rotation Direction

The rotation can be performed in two directions:

- **Left Rotation:** In this mode, the elements are shifted to the left. The last element of the array becomes the first, and all other elements are moved one position to the left.
- **Right Rotation:** In this mode, the elements are shifted to the right. The first element of the array becomes the last, and all other elements are moved one position to the right.

#### Implementation

**Left Rotation** To perform a left rotation on an array, follow these steps:

1. Store the first element in a temporary variable.
2. Shift all other elements one position to the left.
3. Set the last element of the array to the value stored in the temporary variable.

**Right Rotation** To perform a right rotation on an array, follow these steps:

1. Store the last element in a temporary variable.
2. Shift all other elements one position to the right.
3. Set the first element of the array to the value stored in the temporary variable.

```
void LeftRotation_by_one(vector<int> & nums, int k, string direction){
    int len = nums.size()-1;

    if(direction == "left"){
```

```

        int temp = arr[0]
        for (int i=1 ; i<len; i++){
            arr[i-1] =arr[i];
        }
        arr[size-1] =temp;
    }
    else{
        int temp = arr[len]
        for (int i=len ; i>=0; i--){
            arr[i] =arr[i-1];
        }
        arr[0] =temp;
    }
}

```

## Reversal Algorithm Technique

### Introduction

The reversal algorithm is a simple and efficient technique used to reverse the elements of an array or a list. It is a fundamental operation in data manipulation and can be applied to various scenarios, including reversing a string, array, or linked list.

### Algorithm Overview

The reversal algorithm for array rotation involves two main steps:

1. Divide the array into two subarrays, where the division point represents the rotation point.
2. Reverse both subarrays.
3. Reverse the entire array to obtain the desired rotated array.

### Implementation

To perform rotation using reversal algorithm, follow these steps:

1. Divide the array into two subarrays at the rotation point.
2. Reverse both subarrays.
3. Reverse the entire array.

```

void reverse(vector<int>& nums, int low, int high){
    while(low<high){
        int temp = nums[low];
        nums[low] = nums[high];
        nums[high] = temp;
        low++;
    }
}

```

```

        high--;
    }
}

void LeftRotation_by_one(vector<int> & nums, int k, string direction){
    int len = nums.size()-1;
    if (len <= 1 || k== 0) {
        return;
    }

    k = k % len;

    if (k == 0) {
        return;
    }

    if(direction == "left"){
        reverse(nums, 0, k-1);
        reverse(nums,k,len);
        reverse(nums,0,len);
    }
    else{
        reverse(nums, len-k+1, len);
        reverse(nums,0,len-k);
        reverse(nums,0,len);
    }
}

```

## Juggling Algorithm

### Introduction

- The Juggling Algorithm is an efficient method for rotating the elements of an array.
- It is particularly useful when you need to perform left or right rotations on an array by a fixed number of positions.
- This algorithm is known for its simplicity and speed in achieving array rotations.

### Algorithm Overview

The Juggling Algorithm for array rotation is based on the concept of GCD (Greatest Common Divisor) / HCF ( Highest Common Factor ). It involves three main steps:

1. Calculate the GCD of the array size  $n$  and the number of positions to be

- rotated  $d$ .
2. Divide the array into  $\text{gcd}(n, d)$  sets, where each set contains elements that need to be cycled within itself.
  3. Perform cyclic swaps within each set, moving the elements to their new positions.

## Implementation

To perform Juggling Algorithm, follow these steps:

1. Calculate the GCD of  $n$  and  $d$  (denoted as  $\text{gcd}$ ).
2. Divide the array into  $\text{gcd}$  sets.
3. Iterate over each set and perform cyclic swaps within the set.

```
int findGCD(int a, int b) {
    if (b == 0) {
        return a;
    }
    return findGCD(b, a % b);
}

void jugglingRotate(int arr[], int n, int d) {

    d = d % n; // Ensures that d is within the given array size.

    int gcd = findGCD(n, d); // Calculates gcd for size by rotation.

    for (int i = 0; i < gcd; i++) {
        // Stores the first element to temporary variable.
        int temp = arr[i];
        int j = i;
        // Looping to do swap elements from every block or we can say swap element after every
        while (1) {
            int k = (j + d) % n;
            if (k == i) {
                break;
            }
            arr[j] = arr[k];
            j = k;
        }
        // First element again gets stored at last swapped position.
        arr[j] = temp;
    }
}
```

### Lets Visualize juggling

- Suppose we have an array of size 6 and we have to perform 3 rotation ( $n = 6$  ,  $k = 3$ ).

## Topic - Rotation Algorithms / Techniques

Rotation is some of the basic operations that we perform on array, There are multiple ways to perform rotation on array.

- One by One Rotation
- Reversal Algorithm
- Juggling Algorithm

### One By One Rotation Technique

#### Introduction

The method for rotating the elements of an array in a circular fashion. It shifts the elements of the array one position to the left or right, depending on the direction of rotation.

#### Rotation Direction

The rotation can be performed in two directions:

- **Left Rotation:** In this mode, the elements are shifted to the left. The last element of the array becomes the first, and all other elements are moved one position to the left.
- **Right Rotation:** In this mode, the elements are shifted to the right. The first element of the array becomes the last, and all other elements are moved one position to the right.

#### Implementation

**Left Rotation** To perform a left rotation on an array, follow these steps:

1. Store the first element in a temporary variable.
2. Shift all other elements one position to the left.
3. Set the last element of the array to the value stored in the temporary variable.

**Right Rotation** To perform a right rotation on an array, follow these steps:

1. Store the last element in a temporary variable.
2. Shift all other elements one position to the right.
3. Set the first element of the array to the value stored in the temporary variable.

```

void LeftRotation_by_one(vector<int> & nums, int k, string direction){
    int len = nums.size()-1;

    if(direction == "left"){
        int temp = arr[0]
        for (int i=1 ; i<len; i++){
            arr[i-1] =arr[i];
        }
        arr[size-1] =temp;
    }
    else{
        int temp = arr[len]
        for (int i=len ; i>=0; i--){
            arr[i] =arr[i-1];
        }
        arr[0] =temp;
    }
}

```

## Reversal Algorithm Technique

### Introduction

The reversal algorithm is a simple and efficient technique used to reverse the elements of an array or a list. It is a fundamental operation in data manipulation and can be applied to various scenarios, including reversing a string, array, or linked list.

### Algorithm Overview

The reversal algorithm for array rotation involves two main steps:

1. Divide the array into two subarrays, where the division point represents the rotation point.
2. Reverse both subarrays.
3. Reverse the entire array to obtain the desired rotated array.

### Implementation

To perform rotation using reversal algorithm, follow these steps:

1. Divide the array into two subarrays at the rotation point.
2. Reverse both subarrays.
3. Reverse the entire array.

```

void reverse(vector<int>& nums, int low, int high){

```

```

        while(low<high){
            int temp = nums[low];
            nums[low] = nums[high];
            nums[high] = temp;
            low++;
            high--;
        }
    }

void LeftRotation_by_one(vector<int> & nums, int k, string direction){
    int len = nums.size()-1;
    if (len <= 1 || k== 0) {
        return;
    }

    k = k % len;

    if (k == 0) {
        return;
    }

    if(direction == "left"){
        reverse(nums, 0, k-1);
        reverse(nums,k,len);
        reverse(nums,0,len);
    }
    else{
        reverse(nums, len-k+1, len);
        reverse(nums,0,len-k);
        reverse(nums,0,len);
    }
}

```

## Juggling Algorithm

### Introduction

- The Juggling Algorithm is an efficient method for rotating the elements of an array.
- It is particularly useful when you need to perform left or right rotations on an array by a fixed number of positions.
- This algorithm is known for its simplicity and speed in achieving array rotations.

## Algorithm Overview

The Juggling Algorithm for array rotation is based on the concept of GCD (Greatest Common Divisor) / HCF ( Highest Common Factor ). It involves three main steps:

1. Calculate the GCD of the array size  $n$  and the number of positions to be rotated  $d$ .
2. Divide the array into  $\text{gcd}(n, d)$  sets, where each set contains elements that need to be cycled within itself.
3. Perform cyclic swaps within each set, moving the elements to their new positions.

## Implementation

To perform Juggling Algorithm, follow these steps:

1. Calculate the GCD of  $n$  and  $d$  (denoted as  $\text{gcd}$ ).
2. Divide the array into  $\text{gcd}$  sets.
3. Iterate over each set and perform cyclic swaps within the set.

```
int findGCD(int a, int b) {
    if (b == 0) {
        return a;
    }
    return findGCD(b, a % b);
}

void jugglingRotate(int arr[], int n, int d) {

    d = d % n; // Ensures that d is within the given array size.

    int gcd = findGCD(n, d); // Calculates gcd for size by rotation.

    for (int i = 0; i < gcd; i++) {
        // Stores the first element to temporary variable.
        int temp = arr[i];
        int j = i;
        // Looping to do swap elements from every block or we can say swap element after every
        while (1) {
            int k = (j + d) % n;
            if (k == i) {
                break;
            }
            arr[j] = arr[k];
            j = k;
        }
    }
}
```



```

        // First element again gets stored at last swapped position.
        arr[j] = temp;
    }
}

```

### Lets Visualize juggling

- Suppose we have an array of size 6 and we have to perform 3 rotation (  $n = 6$  ,  $k = 3$  ).

Index	0	1	2	3	4	5
Array	1	2	3	4	5	6

size /  $n = 6$  and rotation/ $k = 3$ , Therefore  $\text{gcd}(3,6) = 3$ .

- Sets based on gcd are : 1 | 2 and 3 | 4 and 5 | 6.

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**Left Rotation** To perform a left rotation on an array, follow these steps:

1. Store the first element in a temporary variable.
2. Shift all other elements one position to the left.
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**Right Rotation** To perform a right rotation on an array, follow these steps:

1. Store the last element in a temporary variable.
2. Shift all other elements one position to the right.
3. Set the first element of the array to the value stored in the temporary variable.

```
void LeftRotation_by_one(vector<int> & nums, int k, string direction){
    int len = nums.size()-1;

    if(direction == "left"){
        int temp = arr[0]
        for (int i=1 ; i<len; i++){
            arr[i-1] =arr[i];
        }
        arr[size-1] =temp;
    }
    else{
        int temp = arr[len]
        for (int i=len ; i>=0; i--){
            arr[i] =arr[i-1];
        }
        arr[0] =temp;
    }
}
```

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### Introduction

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1. Divide the array into two subarrays, where the division point represents the rotation point.
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### Implementation

To perform rotation using reversal algorithm, follow these steps:

1. Divide the array into two subarrays at the rotation point.
2. Reverse both subarrays.
3. Reverse the entire array.

```
void reverse(vector<int>& nums, int low, int high){
    while(low<high){
        int temp = nums[low];
        nums[low] = nums[high];
        nums[high] = temp;
        low++;
        high--;
    }
}

void LeftRotation_by_one(vector<int> & nums, int k, string direction){
    int len = nums.size()-1;
    if (len <= 1 || k== 0) {
        return;
    }

    k = k % len;

    if (k == 0) {
        return;
    }

    if(direction == "left"){
        reverse(nums, 0, k-1);
        reverse(nums,k,len);
        reverse(nums,0,len);
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        reverse(nums,0,len-k);
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}
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```
}
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1. Calculate the GCD of **n** and **d** (denoted as **gcd**).
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3. Iterate over each set and perform cyclic swaps within the set.

```
int findGCD(int a, int b) {
    if (b == 0) {
        return a;
    }
    return findGCD(b, a % b);
}

void jugglingRotate(int arr[], int n, int d) {

    d = d % n; // Ensures that d is within the given array size.

    int gcd = findGCD(n, d); // Calculates gcd for size by rotation.
```

```

for (int i = 0; i < gcd; i++) {
    // Stores the first element to temporary variable.
    int temp = arr[i];
    int j = i;
    // Looping to do swap elements from every block or we can say swap element after every
    while (1) {
        int k = (j + d) % n;
        if (k == i) {
            break;
        }
        arr[j] = arr[k];
        j = k;
    }
    // First element again gets stored at last swapped position.
    arr[j] = temp;
}
}

```

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1. Store the last element in a temporary variable.
2. Shift all other elements one position to the right.
3. Set the first element of the array to the value stored in the temporary variable.

```
void LeftRotation_by_one(vector<int> & nums, int k, string direction){
    int len = nums.size()-1;

    if(direction == "left"){
        int temp = arr[0]
        for (int i=1 ; i<len; i++){
            arr[i-1] =arr[i];
        }
        arr[size-1] =temp;
    }
    else{
        int temp = arr[len]
        for (int i=len ; i>=0; i--){
            arr[i] =arr[i-1];
        }
        arr[0] =temp;
    }
}
```

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3. Reverse the entire array to obtain the desired rotated array.

## Implementation

To perform rotation using reversal algorithm, follow these steps:

1. Divide the array into two subarrays at the rotation point.
2. Reverse both subarrays.
3. Reverse the entire array.

```
void reverse(vector<int>& nums, int low, int high){
    while(low<high){
        int temp = nums[low];
        nums[low] = nums[high];
        nums[high] = temp;
        low++;
        high--;
    }
}

void LeftRotation_by_one(vector<int> & nums, int k, string direction){
    int len = nums.size()-1;
    if (len <= 1 || k== 0) {
        return;
    }

    k = k % len;

    if (k == 0) {
        return;
    }

    if(direction == "left"){
        reverse(nums, 0, k-1);
        reverse(nums,k,len);
        reverse(nums,0,len);
    }
    else{
        reverse(nums, len-k+1, len);
    }
}
```

```

        reverse(nums, 0, len-k);
        reverse(nums, 0, len);
    }
}

```

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### Implementation

To perform Juggling Algorithm, follow these steps:

1. Calculate the GCD of **n** and **d** (denoted as **gcd**).
2. Divide the array into **gcd** sets.
3. Iterate over each set and perform cyclic swaps within the set.

```

int findGCD(int a, int b) {
    if (b == 0) {
        return a;
    }
    return findGCD(b, a % b);
}

void jugglingRotate(int arr[], int n, int d) {
    d = d % n; // Ensures that d is within the given array size.

```



```

int gcd = findGCD(n, d); // Calculates gcd for size by rotation.

for (int i = 0; i < gcd; i++) {
    // Stores the first element to temporary variable.
    int temp = arr[i];
    int j = i;
    // Looping to do swap elements from every block or we can say swap element after every
    while (1) {
        int k = (j + d) % n;
        if (k == i) {
            break;
        }
        arr[j] = arr[k];
        j = k;
    }
    // First element again gets stored at last swapped position.
    arr[j] = temp;
}
}

```

### Lets Visualize juggling

- Suppose we have an array of size 6 and we have to perform 3 rotation (  $n = 6$  ,  $k = 3$  ).

Index	0	1	2	3	4	5
Array	1	2	3	4	5	6

size /  $n = 6$  and rotation/ $k = 3$ , Therefore  $\text{gcd}(3, 6) = 3$ .

- Sets based on gcd are : 1 | 2 and 3 | 4 and 5 | 6.
- Perform a leftward cyclic rotation on the initial elements within each set .
- Similarly, subsequently iterate through the remaining elements applying cyclic rotations until the entire set is cycled.
- Finally we got

### FINALLY WE LEARNT HOW TO JUGGLE ARRAYS

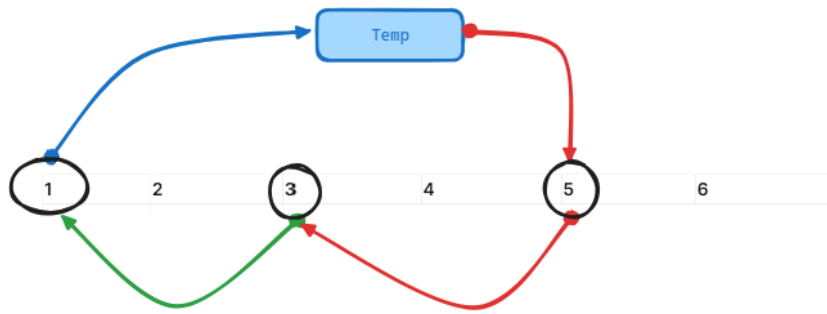


Figure 1: image

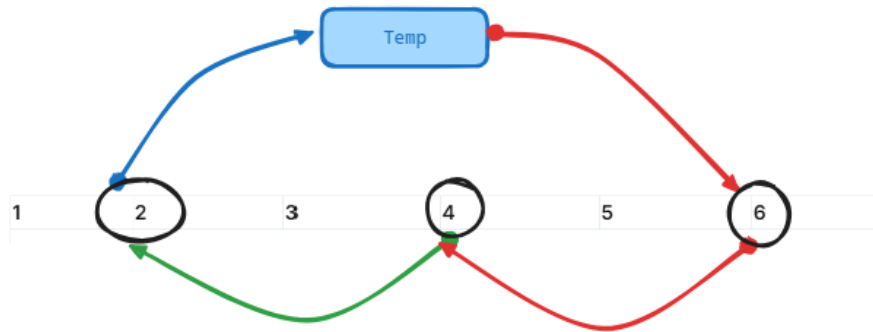


Figure 2: image



Figure 3: image



**SUPER**  
**SIMPLE**