Computer Vision

Jacobs University Bremen

Fall 2021

Homework 4

This notebook includes both coding and written questions. Please hand in this notebook file with all the outputs and your answers to the written questions.

This assignment covers K-Means and HAC methods for clustering and image segmentation.

```
# Setup
from time import time
import numpy as np
import matplotlib.pyplot as plt
from matplotlib import rc
from skimage import io
from future import print function
%matplotlib inline
plt.rcParams['figure.figsize'] = (15.0, 12.0) # set default size of
plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'
# for auto-reloading extenrnal modules
%load ext autoreload
%autoreload 2
The autoreload extension is already loaded. To reload it, use:
 %reload ext autoreload
```

Introduction

In this assignment, you will use clustering algorithms to segment images. You will then use these segmentations to identify foreground and background objects.

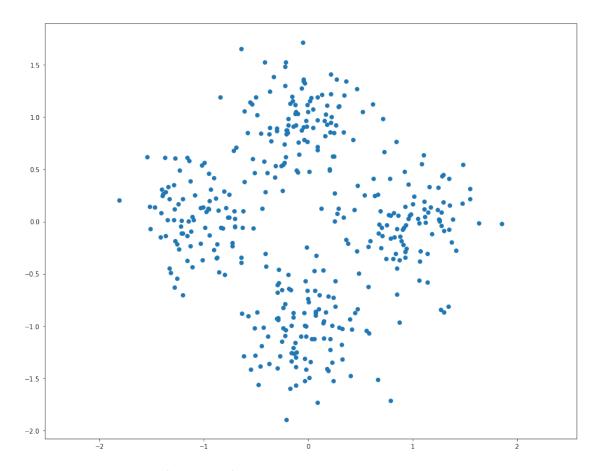
Your assignment will involve the following subtasks:

• **Clustering algorithms**: Implement K-Means clustering and Hierarchical Agglomerative Clustering.

- **Pixel-level features**: Implement a feature vector that combines color and position information and implement feature normalization.
- Quantitative Evaluation: Evaluate segmentation algorithms with a variety of parameter settings by comparing your computed segmentations against a dataset of ground-truth segmentations.

1 Clustering Algorithms (40 points)

```
# Generate random data points for clustering
# Set seed for consistency
np.random.seed(⊙)
# Cluster 1
mean1 = [-1, 0]
cov1 = [[0.1, 0], [0, 0.1]]
X1 = np.random.multivariate_normal(mean1, cov1, 100)
# Cluster 2
mean2 = [0, 1]
cov2 = [[0.1, 0], [0, 0.1]]
X2 = np.random.multivariate normal(mean2, cov2, 100)
# Cluster 3
mean3 = [1, 0]
cov3 = [[0.1, 0], [0, 0.1]]
X3 = np.random.multivariate normal(mean3, cov3, 100)
# Cluster 4
mean4 = [0, -1]
cov4 = [[0.1, 0], [0, 0.1]]
X4 = np.random.multivariate_normal(mean4, cov4, 100)
# Merge two sets of data points
X = np.concatenate((X1, X2, X3, X4))
# Plot data points
plt.scatter(X[:, 0], X[:, 1])
plt.axis('equal')
plt.show()
```



1.1 K-Means Clustering (20 points)

As discussed in class, K-Means is one of the most popular clustering algorithms. We have provided skeleton code for K-Means clustering in the file segmentation.py. Your first task is to finish implementing **kmeans** in segmentation.py. This version uses nested for loops to assign points to the closest centroid and compute a new mean for each cluster.

from segmentation import kmeans

```
np.random.seed(0)
start = time()
assignments = kmeans(X, 4)
end = time()

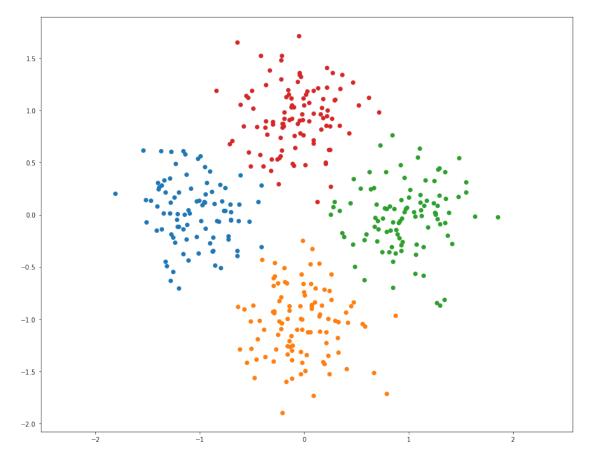
kmeans_runtime = end - start

print("kmeans running time: %f seconds." % kmeans_runtime)

for i in range(4):
    cluster_i = X[assignments==i]
    plt.scatter(cluster_i[:, 0], cluster_i[:, 1])

plt.axis('equal')
plt.show()
```

kmeans running time: 0.033740 seconds.



We can use numpy functions and broadcasting to make K-Means faster. Implement **kmeans_fast** in segmentation.py. This should run at least 10 times faster than the previous implementation.

```
from segmentation import kmeans_fast

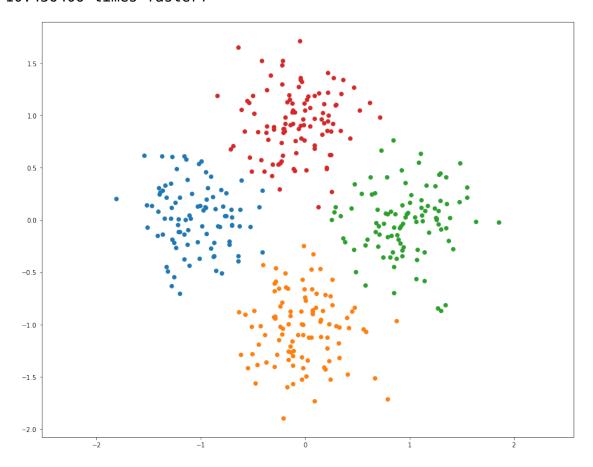
np.random.seed(0)
start = time()
assignments = kmeans_fast(X, 4)
end = time()

kmeans_fast_runtime = end - start
print("kmeans running time: %f seconds." % kmeans_fast_runtime)
print("%f times faster!" % (kmeans_runtime / kmeans_fast_runtime))

for i in range(4):
    cluster_i = X[assignments==i]
    plt.scatter(cluster_i[:, 0], cluster_i[:, 1])

plt.axis('equal')
plt.show()
```

kmeans running time: 0.003227 seconds. 10.456406 times faster!



1.2 K-Means Convergence (10 points)

Implementations of the K-Means algorithm will often have the parameter num_iters to define the maximum number of iterations the algorithm should run for. Consider that we opt to not include this upper bound on the number of iterations, and that we define the termination criterion of the algorithm to be when the cost L stops changing.

Recall that L is defined as the sum of squared distance between all points x and their nearest cluster center c:

$$L = \sum_{i \in clusters} \sum_{x \in cluster_i} (x - c_i)^2$$

Show that for any set of points D and any number of clusters k, the K-Means algorithm will terminate in a finite number of iterations.

Your answer here:

$$L = \sum_{i \in clusters} \sum_{x \in cluster_i} (x - c_i)^2$$

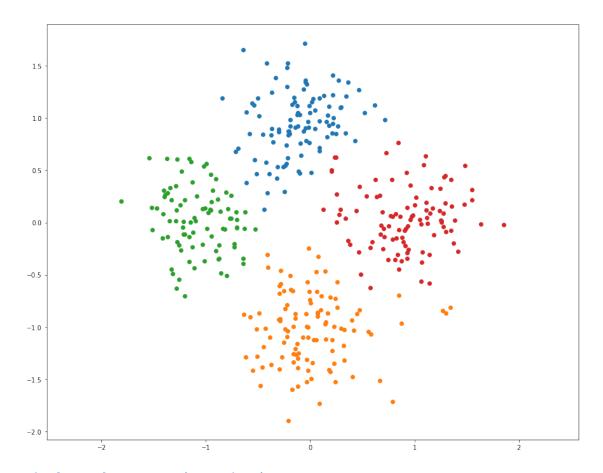
Here, we can reduce the distance w.r.t any set of points that five optimal solution instead of minimizing the distance to the centroid of clusters. i.e. minimizing locally Mathematically, v(X) - v(C), where v is variance

1.2 Hierarchical Agglomerative Clustering (10 points)

Another simple clustering algorithm is Hieararchical Agglomerative Clustering, which is somtimes abbreviated as HAC. In this algorithm, each point is initially assigned to its own cluster. Then cluster pairs are merged until we are left with the desired number of predetermined clusters (see Algorithm 1).

Implement hiererachical clustering in segmentation.py.

```
Algorithm 1 Hierarchical Agglomerative Clustering
  Require: Points x_1, \dots, x_m \in \mathbb{R}^n, desired number of clusters k \in \mathbb{Z}
    Assign each point to its own cluster
    while There are more than k clusters do
      Compute the distance between all pairs of clusters
      Merge the two closest clusters
   end while
from segmentation import hierarchical clustering
start = time()
assignments = hierarchical clustering(X, 4)
end = time()
print("hierarchical clustering running time: %f seconds." % (end -
start))
for i in range(4):
     cluster i = X[assignments==i]
     plt.scatter(cluster i[:, 0], cluster i[:, 1])
plt.axis('equal')
plt.show()
hierarchical clustering running time: 0.232761 seconds.
```



2 Pixel-Level Features (30 points)

Before we can use a clustering algorithm to segment an image, we must compute some *feature vector* for each pixel. The feature vector for each pixel should encode the qualities that we care about in a good segmentation. More concretely, for a pair of pixels p_i and p_j with corresponding feature vectors f_i and f_j , the distance between f_i and f_j should be small if we believe that p_i and p_j should be placed in the same segment and large otherwise.

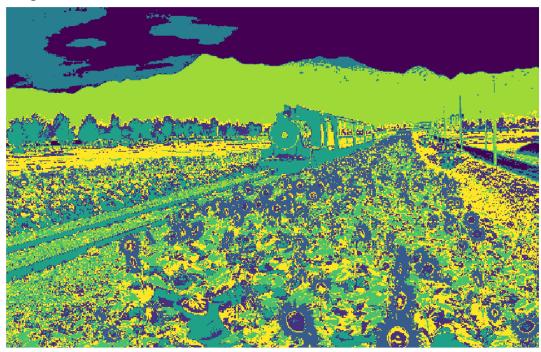
```
# Load and display image
img = io.imread('train.jpg')
H, W, C = img.shape

plt.imshow(img)
plt.axis('off')
plt.show()
```



2.1 Color Features (15 points)

One of the simplest possible feature vectors for a pixel is simply the vector of colors for that pixel. Implement **color_features** in segmentation.py. Output should look like the following:



```
from segmentation import color_features
np.random.seed(0)

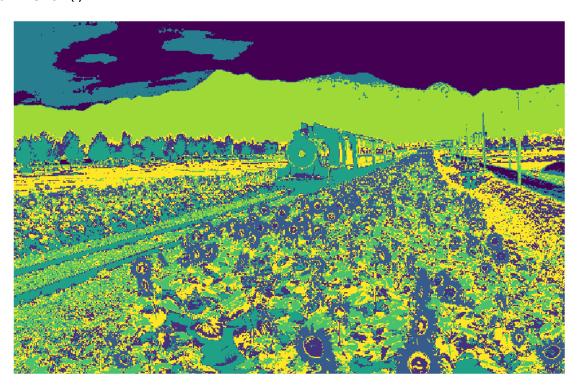
features = color_features(img)

# Sanity checks
assert features.shape == (H * W, C),\
    "Incorrect shape! Check your implementation."

assert features.dtype == float,\
    "dtype of color_features should be float."

assignments = kmeans_fast(features, 8)
segments = assignments.reshape((H, W))

# Display segmentation
plt.imshow(segments, cmap='viridis')
plt.axis('off')
plt.show()
```



In the cell below, we visualize each segment as the mean color of pixels in the segment.

```
from utils import visualize_mean_color_image
visualize_mean_color_image(img, segments)
```



2.2 Color and Position Features (15 points)

Another simple feature vector for a pixel is to concatenate its color and position within the image. In other words, for a pixel of $\operatorname{color}(r,g,b)$ located at $\operatorname{position}(x,y)$ in the image, its feature vector would be (r,g,b,x,y). However, the color and position features may have drastically different ranges; for example each color channel of an image may be in the range δ , while the position of each pixel may have a much wider range. Uneven scaling between different features in the feature vector may cause clustering algorithms to behave poorly.

One way to correct for uneven scaling between different features is to apply some sort of normalization to the feature vector. One of the simplest types of normalization is to force each feature to have zero mean and unit variance.

Implement color position features in segmentation.py.

Output segmentation should look like the following:



```
from segmentation import color_position_features
np.random.seed(0)

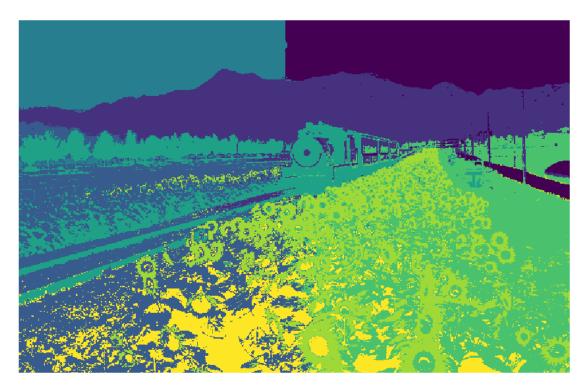
features = color_position_features(img)

# Sanity checks
assert features.shape == (H * W, C + 2),\
    "Incorrect shape! Check your implementation."

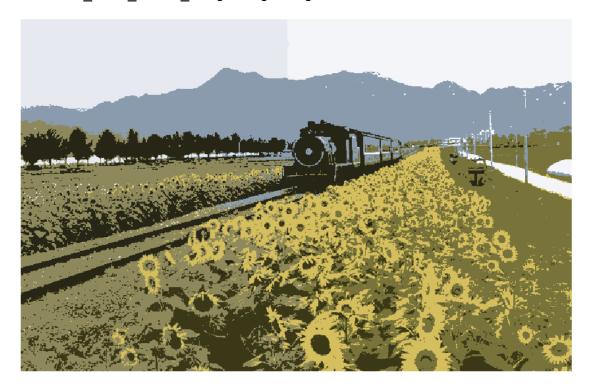
assert features.dtype == float,\
    "dtype of color_features should be float."

assignments = kmeans_fast(features, 8)
segments = assignments.reshape((H, W))

# Display segmentation
plt.imshow(segments, cmap='viridis')
plt.axis('off')
plt.show()
```



visualize_mean_color_image(img, segments)



Extra Credit: Implement Your Own Feature

For this programming assignment we have asked you to implement a very simple feature transform for each pixel. While it is not required, you should feel free to experiment with

other feature transforms. Could your final segmentations be improved by adding gradients, edges, SIFT descriptors, or other information to your feature vectors? Could a different type of normalization give better results?

Implement your feature extractor my_features in segmentation.py

Depending on the creativity of your approach and the quality of your writeup, implementing extra feature vectors can be worth extra credit (up to 1 point).

```
Describe your approach: (YOUR APPROACH)
from segmentation import my features
# Feel free to experiment with different images
# and varying number of segments
img = io.imread('train.jpg')
num segments = 8
H, W, C = img.shape
# Extract pixel-level features
features = my features(img)
# Run clustering algorithm
assignments = kmeans fast(features, num segments)
segments = assignments.reshape((H, W))
# Display segmentation
plt.imshow(segments, cmap='viridis')
plt.axis('off')
plt.show()
                                          Traceback (most recent call
AttributeError
last)
~/environments/hw4/ipykernel 915954/4244037440.py in <module>
     13 # Run clustering algorithm
---> 14 assignments = kmeans_fast(features, num_segments)
     16 segments = assignments.reshape((H, W))
~/environments/hw4/segmentation.py in kmeans fast(features, k,
num iters)
     71
     72
---> 73
            N, D = features.shape
```

75 assert N >= k, 'Number of clusters cannot be greater than number of points'

AttributeError: 'NoneType' object has no attribute 'shape'

3 Quantitative Evaluation (30 points)

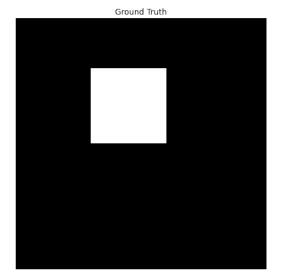
Looking at images is a good way to get an idea for how well an algorithm is working, but the best way to evaluate an algorithm is to have some quantitative measure of its performance.

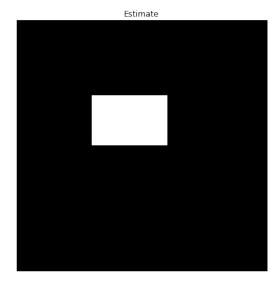
For this project we have supplied a small dataset of cat images and ground truth segmentations of these images into foreground (cats) and background (everything else). We will quantitatively evaluate different segmentation methods (features and clustering methods) on this dataset.

We can cast the segmentation task into a binary classification problem, where we need to classify each pixel in an image into either foreground (positive) or background (negative). Given the ground-truth labels, the accuracy of a segmentation is (TP+TN)/(P+N).

Implement compute_accuracy in segmentation.py.

```
from segmentation import compute accuracy
mask gt = np.zeros((100, 100))
mask = np.zeros((100, 100))
# Test compute accracy function
mask_gt[20:50, 30:60] = 1
mask[30:50, 30:60] = 1
accuracy = compute accuracy(mask gt, mask)
print('Accuracy: %0.2f' % (accuracy))
if accuracy != 0.97:
    print('Check your implementation!')
plt.subplot(121)
plt.imshow(mask gt)
plt.title('Ground Truth')
plt.axis('off')
plt.subplot(122)
plt.imshow(mask)
plt.title('Estimate')
plt.axis('off')
plt.show()
Accuracy: 0.97
```



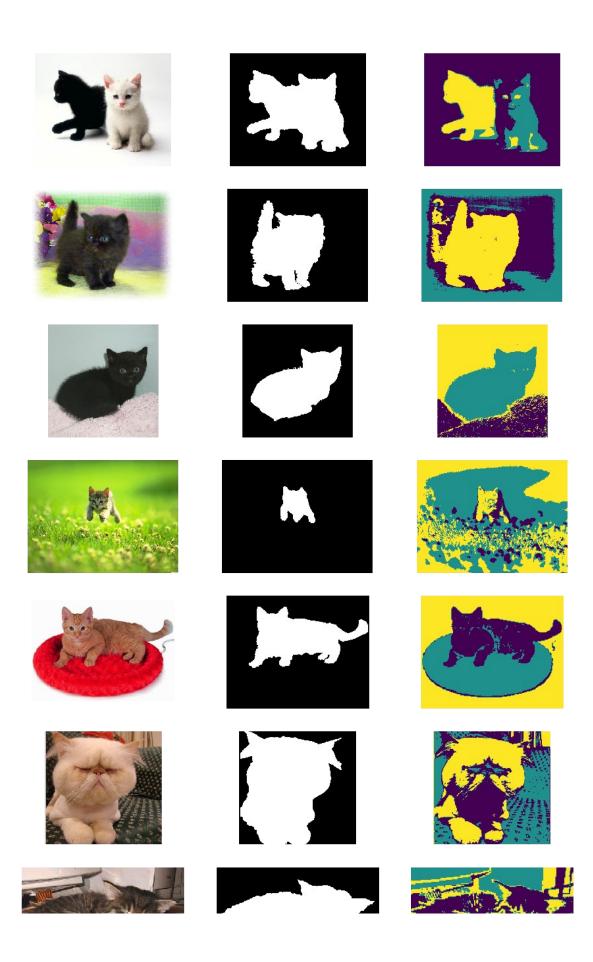


You can use the script below to evaluate a segmentation method's ability to separate foreground from background on the entire provided dataset. Use this script as a starting point to evaluate a variety of segmentation parameters.

from utils import load dataset, compute segmentation

```
from segmentation import evaluate segmentation
# Load a small segmentation dataset
imgs, gt masks = load dataset('./data')
# Set the parameters for segmentation.
num segments = 3
clustering fn = kmeans fast
feature fn = color features
scale = 0.5
mean accuracy = 0.0
segmentations = []
for i, (img, gt mask) in enumerate(zip(imgs, gt masks)):
    # Compute a segmentation for this image
    segments = compute segmentation(img, num segments,
                                    clustering fn=clustering fn,
                                    feature fn=feature fn,
                                    scale=scale)
    segmentations.append(segments)
    # Evaluate segmentation
    accuracy = evaluate segmentation(gt mask, segments)
    print('Accuracy for image %d: %0.4f' %(i, accuracy))
```

```
mean accuracy += accuracy
mean_accuracy = mean_accuracy / len(imgs)
print('Mean accuracy: %0.4f' % mean accuracy)
Accuracy for image 0: 0.8079
Accuracy for image 1: 0.9583
Accuracy for image 2: 0.9700
Accuracy for image 3: 0.9059
Accuracy for image 4: 0.9623
Accuracy for image 5: 0.6814
Accuracy for image 6: 0.6739
Accuracy for image 7: 0.6688
Accuracy for image 8: 0.8367
Accuracy for image 9: 0.9528
Accuracy for image 10: 0.8552
Accuracy for image 11: 0.8108
Accuracy for image 12: 0.7323
Accuracy for image 13: 0.6615
Accuracy for image 14: 0.7456
Accuracy for image 15: 0.4931
Mean accuracy: 0.7948
# Visualize segmentation results
N = len(imgs)
plt.figure(figsize=(15,60))
for i in range(N):
    plt.subplot(N, 3, (i * 3) + 1)
    plt.imshow(imgs[i])
    plt.axis('off')
    plt.subplot(N, 3, (i * 3) + 2)
    plt.imshow(gt masks[i])
    plt.axis('off')
    plt.subplot(N, 3, (i * 3) + 3)
    plt.imshow(segmentations[i], cmap='viridis')
    plt.axis('off')
plt.show()
```



Include a detailed evaluation of the effect of varying segmentation parameters (feature transform, clustering method, number of clusters, resize) on the mean accuracy of foreground-background segmentations on the provided dataset. You should test a minimum of 10 combinations of parameters. To present your results, add rows to the table below (you may delete the first row).

Feature Transform Clustering Method Number of segments Scale Mean Accuracy Color K-Means 3 0.5 0.79 Color and Position K-Means 3 0.5 0.79

Observe your results carefully and try to answer the following question:

- 1. Based on your quantitative experiments, how do each of the segmentation parameters affect the quality of the final foreground-background segmentation?
- 2. Are some images simply more difficult to segment correctly than others? If so, what are the qualities of these images that cause the segmentation algorithms to perform poorly?
- 3. Also feel free to point out or discuss any other interesting observations that you made.

Write your analysis in the cell below.

Your answer here:Here, we tested k-means clustering method having 'color' and 'color and position' as two vectors in feature space in order to get the resulting mean accuracy which is approximately similar. Since, the foreground and background color is similar and the clusteing is pretty closer as the vector distance between our feature transform vectors are minimum, we add pixel's 'position' factor as additional feature to have varied clusters.