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**B.E. V Semester Examination**

**BE-V/12 (A)**

**233904**

**COMP. ENGG.**

**Course No. COM-504**

**(Automata & Formal Languages)**

*Time Allowed-3Hours*

*Maximum Marks-100*

**Note :** Attempt five questions at least two questions from each section.  
Each question carries 20 marks.

**Section - A**

1. a) Why do we need to study NFA if we have less number of states in DFA? Justify. (7)  
b) Design the DFA for "Even number of a's and Odd number of b's". Design a machine to check the divisibility by 4. (13)
2. a) State the theorem on pumping Lemma for regular expressions (8)  
b) Prove by using pumping Lemma that the language L is not regular, such that:  
$$L = \{w \in \Sigma^* : \Sigma = \{a, b\} \text{ and } N_a(w) < N_b(w)\}$$
$$N_a(w)$$
 represents number of a's in w. (6)

- c) How do you define a PDA? What is the difference between FA and PDA? (6)

3. a) Find DFA and Regular Expression when the DFA accepts all strings corresponding to the regular expression  $(0^*10^*1)^*$ . Explain how to convert the DFA to Regular Expression by eliminating states? (10)

- b) Construct a FA that accepts  $\{0+1\}^*$ . Obtain a derivation tree for the string 001100 using grammar:  
 $S \rightarrow A0S / 0 / SS$   
 $A \rightarrow S / 1A / 10$  (10)

4. Prove or disprove each of the following statements, stating clearly any well-known results that you use.

- a) For any regular expressions  $r$  and  $s$ , the regular expressions  $(r^*s^*)^*$  and  $(r|s)^*$  always denote the same language. (10)

- b) Let  $L$  be a regular language over an alphabet  $\Sigma$ . Then the language consisting of those  $u \in \Sigma^*$  such that there is some  $v \in \Sigma^*$  with  $uv \in L$ , is also a regular language. (10)

**Section - B**

5. a) Explain optimization of grammars with examples and perform the optimization for grammar:
- $$S \rightarrow XY \quad X \rightarrow Zb \quad Y \rightarrow bW \quad Z \rightarrow AB \quad W \rightarrow Z$$
- $$A \rightarrow aA|bA| \epsilon \quad B \rightarrow Ba|Bb| \epsilon$$
- (10)
- b) Construct a PDA for following language:
- $$L = \{a^n b^{2n} | n \geq 1\}$$
- (10)
6. a) Design a Turing Machine to accept the set of all palindrome over  $\{0,1\}^*$ . Draw a transition diagram for the Turing Machine of the above.
- (10)
- b) Define pumping Lemma. How is it used in CFG? Explain with an example.
- (10)
7. Explain Halting problem of Turing Machine. What are the consequences of Halting Problem?
- (20)
8. Write short notes on:
- a) Decidability problem
- (10)
- b) Universal Turing Machine.
- (10)

