

Module - IV (2023-24) syllabus

Database Design: Functional Dependencies - Normal forms; First Normal form, Second Normal Form, Third Normal Form, Boyce Codd Normal Form, Multivalued Dependencies & Fourth Normal Form, Join Dependencies & Fifth Normal form. Inference Rules for Functional Dependencies, Minimal sets of functional Dependencies, Prop: of Reln decomposition.

Functional Dependency

A f.d is a constraint b/w two sets of attributes from the db, denoted by,

$$x \rightarrow y$$

y is functionally dependent on x.

$$\begin{array}{l} x \rightarrow yz \\ x \rightarrow y \\ x \rightarrow z \\ A \rightarrow AB \\ A \rightarrow B \\ A \rightarrow C \end{array}$$

Inference Rules for Functional Dependency

- (1) Reflexive Rule :- If $y \subseteq x$, then $x \rightarrow y$
- (2) Augmentation Rule :- If $x \rightarrow y$, then $xz \rightarrow yz$
- (3) Transitive Rule :- If $x \rightarrow y \ \& \ y \rightarrow z$, then $x \rightarrow z$.
- (4) Decomposition or Projective Rule : If $x \rightarrow yz$, then $x \rightarrow y \ \& \ x \rightarrow z$.
- (5) Union or Additive Rule : If $x \rightarrow y \ \& \ x \rightarrow z$, then $x \rightarrow yz$.
- (6) Pseudo Transitive Rule :- If $x \rightarrow y \ \& \ wy \rightarrow z$, then $wy \rightarrow z$.

The 1st 3 rules are

- sound :- generate only f.d that actually hold.
- complete :- generate all f.d that hold. They are called Armstrong's axioms, the last 3 inference rules are inferred from Armstrong's axioms.

Examples

$$R = (A, B, C, G, H, I)$$

$$F = \{A \rightarrow B\} \\ \{A \rightarrow C\}$$

$$CG \rightarrow HI$$

$$CG \rightarrow I$$

$$B \rightarrow H$$

find f.d F^+ of F.

By transitivity from $A \rightarrow B$ & $B \rightarrow H$
we get $A \rightarrow H$.

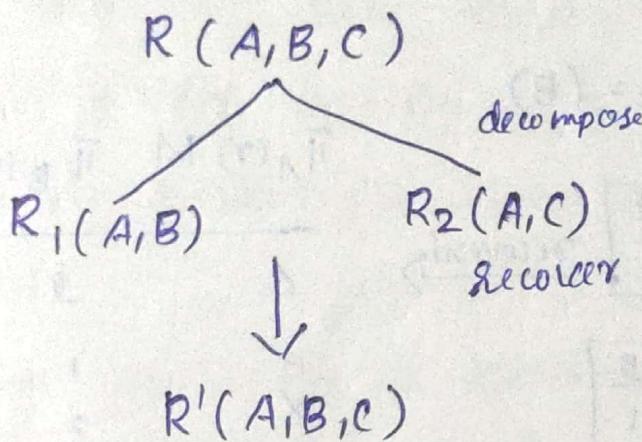
(2) $AG \rightarrow I$
by augmentation $A \rightarrow C$ with G , to get $AG \rightarrow CG$
& then transitivity with $CG \rightarrow I$

(3) $CG \rightarrow HI$
from $CG \rightarrow H$ & $CG \rightarrow I$ (union rule).

Decomposition

When we decompose a reln schema R with a set of fds F into R_1, R_2, \dots, R_n we want

i) lossless decomposition :- otherwise decompos^{tion} would result in information loss.



$$R(A, B, C) = R'(A, B, C) \rightarrow \text{lossless decmp.}$$

A decomposition of R into $R_1 \& R_2$ is lossless form iff atleast one of the following condtn is hold in F^+ .

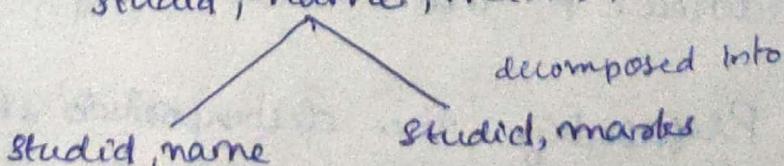
$$R_1 \cap R_2 \rightarrow R,$$

$$R_2 \cap R_1 \rightarrow R_2$$

Example

Table having fields

studid, name, marks.



There is a common attribute studid & original information can be retrieved without any information loss.

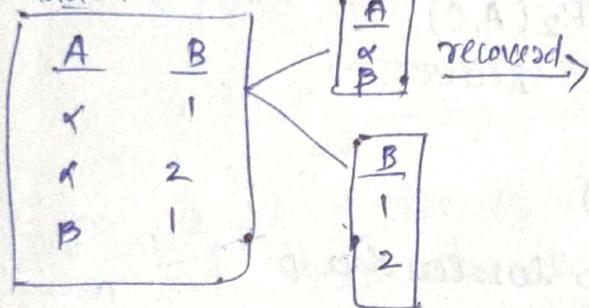
Illustration of lossy Decomposition

Given instances of the decomposed relns, if we are not able to reconstruct the corresponding instances of the original reln - there is information loss in lossy decomposition.

e.g:- $R = (A, B)$

$$R_1 = (A), R_2 = (B)$$

Table 1



$\pi_A(r)$	$\pi_B(r)$
A	B
x	1
x	2
B	1

The original reln is not retrieved after applying decomposition & retrieving data, so this comes under lossy decomposition.

- (2) No redundancy :- The reln R_i shld be either Boyce Codd Normal form or 3rd normal form.
- (3) Dependency Preserving :- Let F_i be the set of dependencies F^+ that include only attributes in R_i .

Prefarably, the decomposition shld be dependency preserving, that is

$$(F_1 \cup F_2 \cup \dots \cup F_n)^+ = F^+$$

Otherwise, checking updates for violation in functional dependencies may require computing joins, which is expensive.

Let $F^1 = F_1 \cup F_2 \cup \dots \cup F_n$. If F^1 is a set of f.ds on schema R, but in general $F^1 \neq F$, it may be $F^{1+} = F^+$. If the latter is true then every dependency in F is logically implemented in F^1 , & if we verify that F^1 is satisfied, we have verified that F is satisfied.

The conclusion is decomposition having the property $F^{1+} = F^+$ is a dependency - preserving decomposition.

Example

$$R = (A, B, C)$$

$$F = \{A \rightarrow B, B \rightarrow C\}$$

Normalization

The basic objectives of normalization is to reduce redundancy, which means that information is to be stored only once. Storing information several times leads to wastage of storage space & ↑ in the total size of the data stored. Relations are normalized so that when altns in the db

are to be altered, we do not loss information or introduce inconsistencies.

Functional Dependency

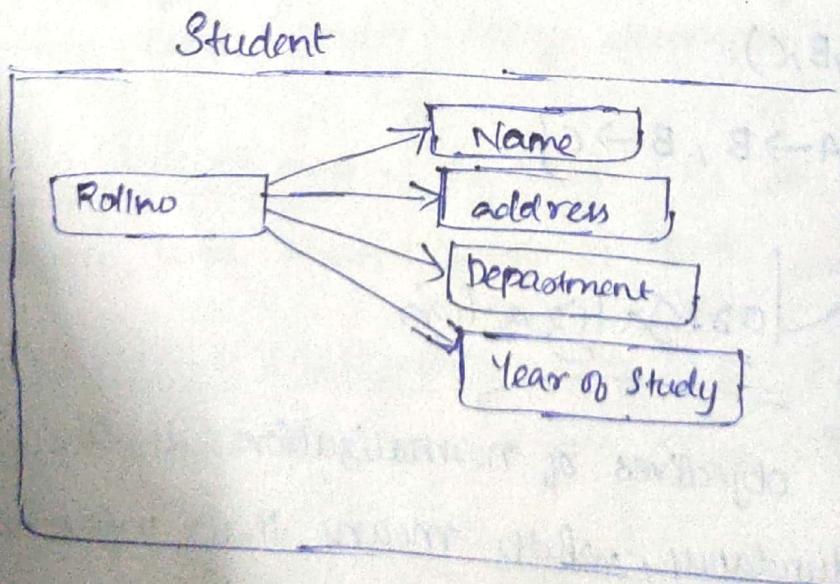
Let X & Y be two attributes of a reln.

Given the value of X , if there is only one value of Y corresponding to it, then Y is said to be functionally dependent on X . This is indicated by the notation.

$$X \rightarrow Y$$

If we write,

$X, Z \rightarrow Y$ — It means that there is only one value of Y corresponding to given values of X, Z .



In this reln named student, the values of all the attributes can be uniquely determined.

Thus all the attributes are f.d. on the attribute Rollno.

Anomalies in a db / Pitfalls in a Reltn Dd

Consider the reln

Name	Course	Phno	Major	Prof	Grade
Jones	353	237-46843	CS	Smith	A
Smith	329	431-53876	Phy	Turner	B
Martin	456	531-64789	Chem	Clark	B
Duke	293	444-75689	Math	James	A+
Jones	379	237-46843	Hstry	Lam.	B

The keys of the relns is Name & course.

Here the attribute grade is fully fd on the key, Name & course.

Name \leftarrow phone no

Name \leftarrow Major

Course \leftarrow Professor

Name, Course \leftarrow Grade

Thus, the determinants of these attr. is not the entire key, but only part of the key of the reln.

The anomalies forced here are.

- * Update Anomalies :- A change in the phno of Jones must be made, for consistency in all tuples pertaining to the student Jones.

- * Insertion Anomalies :- If this is the only attr in the db showing the association b/w a faculty member & the course, the fact that a given professor is teaching a given course cannot be entered in the db unless a student is registered in the course.
- * Deletion Anomalies :- If the only student registered in a given course discontinues the course the information as to which professor is offering the course will be lost, if this is the only attr in the db showing the association b/w a faculty member & the course.
It often leads to generation of ~~se~~ spurious tuples.

→ First Normal Form

- ① The domain of the attributes must include only atomic values
- ② It was designed to disallow multivalued, composite attributes & their combination.
- ③ It disallows nested attrs.

Converting a attr to 1NF is the 1st essential step of normalization. Each form is an improvement over the earlier form - 2NF is an improvement on 1NF, 3NF is an improvement on 2NF & so on.

Student Rlt

<u>Rollno</u>	<u>Name</u>	<u>Department</u>	<u>Year</u>	<u>Phnno</u>
1	Anju	MCA	1	234567
2	Mary	MBA	2	457892
3	Elaine	MCA	1	489435
4	Sist	MBA	2	498763
5	Katha	Btech	3	235865

The above Rlt is in INF, as it does not contain any non atomic value, or composite attribute or multivalued attribute.

Second Normal Form

- ① A Rlt is said to be in 2NF, if it is INF & non-key attributes are fully functionally dependent on the 1^o key attribute.
- ② If the key has more than one attribute then no non-key attributes shld be fd upon part of the key attribute.

Student Rlt

<u>studid</u>	<u>Name</u>	<u>CourseId</u>	<u>Coursename</u>	<u>Grade</u>
101	John	MS1250	Btech	A+
102	John	MS1415	MBA	A
103	Tennen	MS1331	HotMgt	B+
104	Chris	MS1455	MCA	B

Primary key — studid, courseId

studid \leftarrow Name \rightarrow Partial dependency

courseid \leftarrow coursename \rightarrow "

studid, courseId \leftarrow grade \rightarrow full "

To convert this into 2NF.

Student

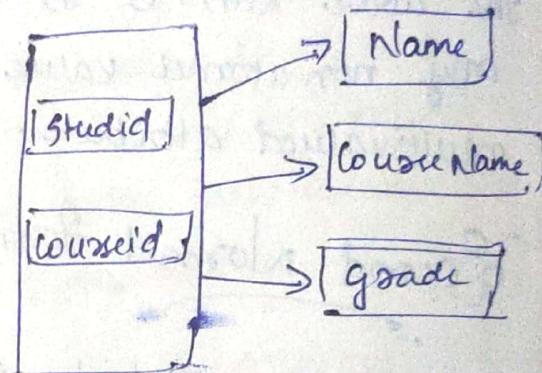
<u>Studid</u>	<u>Name</u>
101	Johns
102	Lennon
103	Chris

Course

<u>Courseid</u>	<u>Coursename</u>
MSI250	Btech
MSI415	MBA
MSI331	Honours
MSI455	MCA

Student-Grade

<u>Studid</u>	<u>Courseid</u>	<u>grade</u>
101	MSI250	A+
101	MSI415	A
103	MSI331	B+
103	MSI455	B



Third Normal Form

A table is in 3NF if

- (1) It is already in 2NF &
- (2) No two non-prime attributes should be f.d on each other i.e all the non-prime attributes should be non-transitively dependent on each other in the R.H.s.

<u>Rollno</u>	<u>Name</u>	<u>Dptmnt</u>	<u>year</u>	<u>hostel</u>
1784	Raman	Phy	1	Ganga
1896	Maya	Chem	1	Gang
1487	Singh	Maths	2	Icarus
1693	Rajan	CS	2	"
1847	Krishnan	CS	3	Krishna

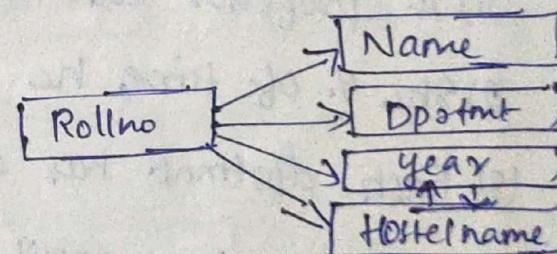
Observe that given the year of student, his hostel is known & vice versa.

Here, dependency is b/w the attributes yr & hostel names, which are both non key attributes. It leads to unnecessary duplication of data.

To convert this into 3NF,

<u>Rollno</u>	<u>Name</u>	<u>Dpmnt</u>	<u>year</u>
1784	Raman	Phy	1
1896	Maya	Chem	1
1487	Singh	Maths	2
1693	Rayan	CS	2
1847	Krishnan	CS	3

<u>year</u>	<u>Hostelname</u>
1	ganga
2	kaisevi
3	Krishna
4	godavari



① Boyce-Codd Normal Form (BCNF)

It arises when

- (1) The table is already in 3NF.
- (2) A attr has more than one possible key ✓
- (3) Further that the composite keys have a common attribute.
- (4) If an attribute of a composite key is dependent on the attribute of the other composite key, a normalization, BCNF is required.

Example - Professor

<u>Professor</u>	<u>Department</u>	<u>HOD</u>	<u>Percent</u>
P ₁	Phy	Rao	50
P ₁	Maths	Krishnan	30
P ₂	Chem	Ghosh	75
P ₂	Phy	Rao	duplicated 95
P ₃	Maths	Krishnan	25

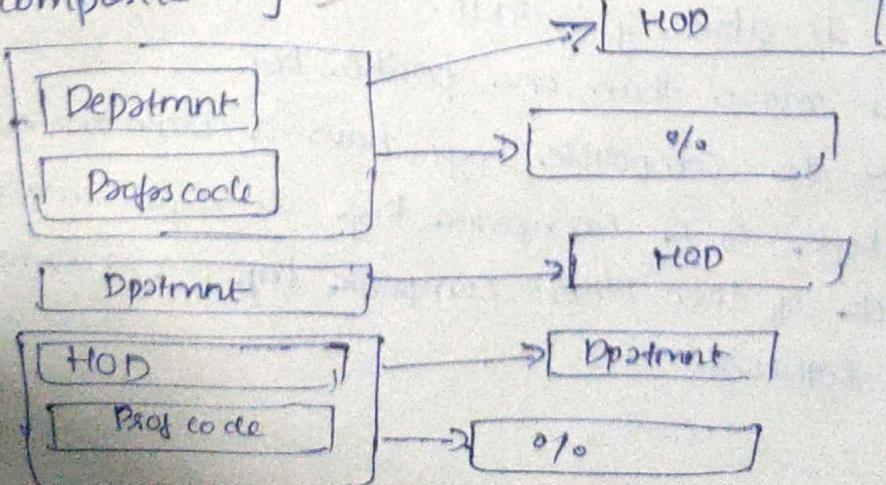
2. The relation is in 3NF, but the attribute dept & HOD is duplicated.

It is assumed that,

- (1) A professor can work in more than one dept.
- (2) The % of time he spends in each dept is given.
- (3) Each dept has only one HOD.

The two possible composite keys are HOD,

- Professor code & Prof code & Dept. ~~other~~
 Observe that HOD & department are not
 non-key attributes, they are part of the
 composite key.

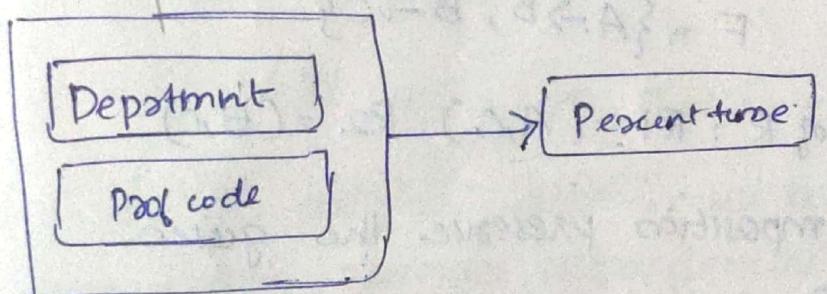


To convert to BCNF,

<u>Prof code</u>	<u>Department</u>	<u>% time</u>
P ₁	Phy	50
P ₁	Maths	30
P ₂	Chem	75
P ₂	Phy	75
P ₃	Maths	25

~~BCNF HOD~~

Phy Rao
Maths Kashman
Chem Ghosh



Thus, a table is in BCNF iff it is already in 3NF & every determinant shld be candidate key.

INF → Values shld be non-redundant & atomic

2NF → non-prime attributes shld be fully fundamentally dependent.

3NF → inter transitively dependent

4NF → No multivalued dependency

5NF → No join dependency

6NF → every determinant shld be a candidate key.

• (Read or replace by sqst. no / no number) (3)

* Dependency Preservation

~~M.d.IV~~ Getting lossless decomposition is necessary. But of course, we also want to keep dependencies, since losing a dependency means that the corresponding constraint can be checked only through natural join of the appropriate resultant relations in the decomposition. This would be very expensive, so, our aim is to get a lossless dependency preserving decomposition.

Example:

$$R = (A, B, C) \quad F = \{A \rightarrow B, B \rightarrow C\}$$

$$\text{Decomposition of } R: R_1 = (A, C) \quad R_2 = (B, C)$$

? Does this decomposition preserve the given dependencies?

Soln:- In R_1 the following dependencies hold:

$$F_1' = \{A \rightarrow A, C \rightarrow C, A \rightarrow C, AC \rightarrow AC\}$$

$$\text{In } R_2, " \quad F_2' = \{B \rightarrow B, C \rightarrow C, B \rightarrow C, BC \rightarrow BC\}$$

The set of nontrivial dependencies hold on $R_1 \& R_2$:

$$F' := \{B \rightarrow C, A \rightarrow C\}$$

$A \rightarrow B$ can not be derived from F' , so this decomposition is NOT dependency preserving.

Example

$$R = (A, B, C)$$

$$F = \{A \rightarrow B, B \rightarrow C\}$$

$$\text{Decomposition of } R : R_1 = (A, B)$$

$$R_2 = (B, C)$$

? Does this decomposition preserve the given dep?

soln

In R_1 the foll: dep holds :

$$F_1 = \{A \rightarrow B, A \rightarrow A, B \rightarrow B, AB \rightarrow AB\}$$

$$F_2 = \{B \rightarrow B, C \rightarrow C, B \rightarrow C, BC \rightarrow BC\}$$

$$F' = F_1 \cup F_2 = \{A \rightarrow B, B \rightarrow C, \text{trivial dependencies}\}$$

In F' all the original dependencies occur, so this decomposition preserves dependencies.

Module-IV

* Functional Dependencies

Let $x \in y$ be the two attributes of a reln. Given the value of x , if there is only one value for y corresponding to it, then y is said to be functionally dependent on x . Indicated by notation $x \rightarrow y$. y is fully dependent upon x .

* Inference Rules for Functional Dependencies / Armstrong's Axioms

A rule used to conclude Fd's on a reln db. If type is assertion, it can apply to a set of FD to derive other FD.

1. Reflexive Rule: If $y \subseteq x$, then $x \rightarrow y$

2. Augmentation Rule: If $x \rightarrow y$, then $xz \rightarrow yz$

3. Transitive Rule: If $x \rightarrow y$ & $y \rightarrow z$, then $x \rightarrow z$

4. Decomposition or Projective Rule: If $x \rightarrow yz$, then $x \rightarrow y$ & $x \rightarrow z$

5. Union or Additive Rule: If $x \rightarrow y$ & $x \rightarrow z$, then $x \rightarrow yz$.

6. Pseudo Transitive Rule: If $x \rightarrow y$ & $WY \rightarrow z$, then $Wx \rightarrow z$

e.g. $R = (A, B, C, G, H, I)$

$$F = \{ A \rightarrow B \}$$

$$A \rightarrow C$$

$$CG \rightarrow H$$

$$CG \rightarrow I$$

$$B \rightarrow H \}$$

Module-IV

* Functional Dependencies

Let $x \in y$ be the two attributes of a relation. Given the value of x , if there is only one value for y corresponding to it, then y is said to be functionally dependent on x . Indicated by notation $x \rightarrow y$. y is functionally dependent upon x .

* Inference Rules for Functional Dependencies / Armstrong's Axioms

Armstrong's axioms are used to conclude functional dependencies on a relational database. It consists of three axioms:

1. Reflexive Rule: If $y \subseteq x$, then $x \rightarrow y$

2. Augmentation Rule: If $x \rightarrow y$, then $xz \rightarrow yz$

3. Transitive Rule: If $x \rightarrow y$ & $y \rightarrow z$, then $x \rightarrow z$

4. Decomposition or Projective Rule: If $x \rightarrow yz$, then $x \rightarrow y$ & $x \rightarrow z$

5. Union or Additive Rule: If $x \rightarrow y$ & $x \rightarrow z$, then $x \rightarrow yz$

6. Pseudo Transitive Rule: If $x \rightarrow y$ & $y \rightarrow z$, then $wx \rightarrow z$

e.g. $R = (A, B, C, G, H, I)$

$$F = \{ A \rightarrow B \\ A \rightarrow C \\ CG \rightarrow H \\ CG \rightarrow I \\ B \rightarrow H \}$$

fund functional dependencies (F^+) $\subset F_B$

① $\rightarrow A \rightarrow B \quad A \rightarrow C$

Union: $A \rightarrow B, C$

② $\rightarrow CG \rightarrow H \quad CG \rightarrow I$

Union: $CG \rightarrow H, I$

③ $\rightarrow AG$

$AG \rightarrow CG \rightarrow$ Augment :- G

$CG \rightarrow H$

From $\Rightarrow AG \rightarrow H$: Redundant transitivity

④ $A \rightarrow B$ (given)

$B \rightarrow H$ (given)

$\Rightarrow A \rightarrow H$ (transitivity rule)

$A \rightarrow C = AG \rightarrow CG$ Augment

$CG \rightarrow H$ given

$\Rightarrow AG \rightarrow H$ Transitivity

• Minimal sets of functional dependencies /

Minimal canonical cover

A canonical cover of F (f³) a minimal set of functional dependencies equivalent to F , lacking no redundant dependencies (redundant parts) & dependences.

e.g. $\{A \rightarrow B, B \rightarrow C\}$, we informed from that $A \rightarrow C$.

A set of functional dependencies F to be minimal, it should satisfy the following condition -

- every dependency in F has a single attribute for its RHS.
- We cannot remove a dependency from F & have a set of dependencies that is equivalent to F .
- We can't replace any dependency $x \rightarrow A$ in F with a dependency $y \rightarrow A$ where $y \subseteq x$ & still have a set of dependencies that is equivalent to F .

$$x = \{A \rightarrow B, B \rightarrow C, A \rightarrow CD\}$$

$$y = \{A \rightarrow B, B \rightarrow C, A \rightarrow D\}$$

OR

$$x = \{A \rightarrow B, B \rightarrow C, A \rightarrow C\}$$

$$y = \{A \rightarrow B, B \rightarrow C\}$$

$y \subseteq x$

A ABC

B DEF

C GHI

D JKL

Remove, redundancy
transitivity rule
Redundant

* Normalization

Reduce redundancies & inconsistencies (data entries)

? First Normal Form:

The domains of the attribute must include only atomic values. It was designed to disallow multivalued, composite attributes & their combinations.
 $\text{shape} \rightarrow \text{Material}, \text{Title}$
(nested attr.)

eg:- Student

Rollno	Name	Dept	Year	phononumber
1	Anju	MCA	1	234567
2	Merry	MBA	2	467892
3	clairi	MCA	1	489435
4	sint	MBA	2	498763
5		Btech	3	

! Second Normal Form

A reln is said to be (fn) 2NF, if it is already in 1NF & the nonkey attributes are fully functionally dependent upon the primary key attribute.

eg:- Student Relation

studid	Name	courseid	coursename	Grade
101	Johnson	MSI250	Mtech	A+
101	Johnson	MSI415	MBA	A
102	Lennin	MSI331	Hotelman	B+
103	chris	MSI455	MCA	B+

Primary key - studid, courseid

studid \leftarrow Name

courseid \leftarrow coursename

studid, courseid \leftarrow grade

(depend on a primary key)

Sto

Solution

stud

studid	Name
101	Johnson
102	Lennier
103	Chris

course

courseid	coursename	grade
M51250	Mtech	A+
M51415	MBA	A
M51331	Hotel Mng	B+
M51455	MCA	B

studid → name

courseid ← coursename → grade

studid	courseid	grade
101	M51250	A+
101	M51415	A
102	M51331	B+
103	M51455	B

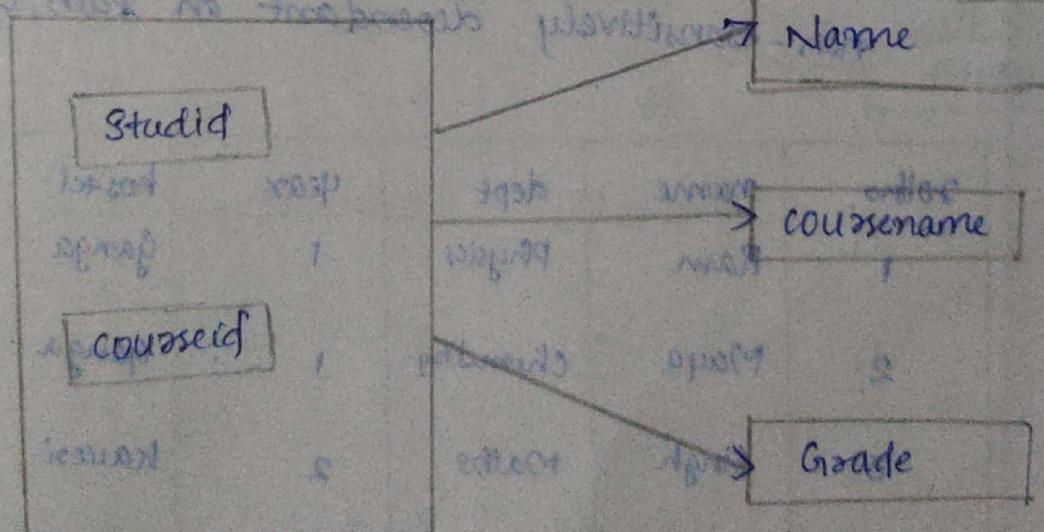
studgrade

studid, courseid → grade

studid, courseid → grade

studid, courseid → grade

studid, courseid → grade



book

foreign key bookid references tablenamel < author

bookid number (3)

bookname varchar(4)

foreign key bookid references author

* Third Normal Form

A table is in 3NF, iff :

(i) It is already in 2NF

(ii) No two non-prime attributes should be functionally dependent on each other.

i.e all the non-prime attributes should be non-transitively dependant on each other.

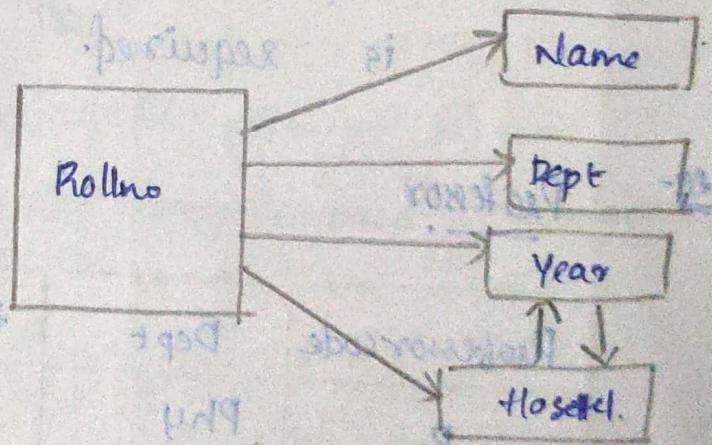
rollno	name	dept	year	hostel
1	Ram	Physics	1	Ganga
2	Maya	Chemistry	1	Ganga
3	Singh	Maths	2	Kaveri
4	Rajan	CS	2	Kaveri
5	Krishnan	CS	8	Krishna

(i) Student (2018) mat. letter No. 1908

rollno	name	dept	year
1	Ram	Phy	Ganga 1 2008
2	Maya	Chem	Ganga 1 2008
3	Singh	Math	Kaveri 2 2008
4	Rayan	2 CS	Kaveri 2 2008
5	Krishna	3 CS	Kaveri 3 2008

(ii) stud-hostel

Year	hostel
1	Ganga
2	Kaveri
3	Krishna
4	Kaveri
5	Kaveri
6	Kaveri
7	Kaveri
8	Kaveri



Boyce-Codd Normal Form (BCNF)

Non-key attr.
not key attr &
non-key

BCNF arises when:

- (a) the table is already in 3NF. non-prime attr/ no dependency
- (b) A attr has more than one possible key. Profcode & Dept OR Profcode & HOD
- (c) furthermore, the composite keys have a common attribute
more than 1 attr in key
- (d) If an attribute of a composite key is dependent on the attribute of the other composite key, a normalization BCNF is required.

Professor

Professorcode	Dept	Head of Dept	Percent
P ₁	Phy	Rao	50
P ₁	Maths	Krishnam	30
P ₂	Chem	Ghosh	60
P ₂	Phy	Rae	25
P ₂	Maths	Krishnam	30
P ₃			

Profcode	D.dept	Percent	Dept	Respective HOD
P ₁	Phy	50	Phy	Rao
P ₁	Maths	30	Maths	Krishnan
P ₂	Chem	60	Chem	Ghosh.
P ₂	Phy	25		
P ₃	Maths	30		

class of first normal form

* Fourth Normal Form

A reln is in fourth 4NF iff :

(i) It is already in BCNF

(ii) It contains non-trivial multivalued dependencies.

⇒ multivalued attribute

multivalued dependencies (MVD)

$A \rightarrow\!\!\! \rightarrow B$ MVD represents a dependency between attributes

$A \rightarrow\!\!\! \rightarrow C$ eg: A,B & C is an reln S, for each value of A, there is a set of values for B & a set of values for C. However the sets of values of B & C are independent of each other.

eg:- ModelNo

Manufacturing Year

colour

M101	2010	Red
M101	2010	Black
M102	2013	Red
M102	2014	Black
M103	2014	Red

ModelNo → Manufacturing yr

ModelNo → colour

Manufacturing yr & colour are independent to each other.

eg of 4NF

Vendor - Supply - Projects Rdbms in table: vendorSupply

VendorNode	ItemCode	ProjectCode	VendorNode	ItemCode
V1	I1	P1	V1	I1
V1	I2	(P1)	V1	I2
V2	I2	P2	V2	I2
V2	I3	P2	V2	I3
V3	I1	P3	V3	I4

table-2

VendorProject

Vendorcode	ProjectNo
V ₁	P ₁
V ₂	P ₂
V ₃	P ₃

A $\rightarrow\!\!\!\rightarrow$ Bstudname, address $\rightarrow\!\!\!\rightarrow$ address

A MVD can be classified as trivial & non-trivial.

An MVD A $\rightarrow\!\!\!\rightarrow$ B in a reltn is defined as being trivial,

if B is a subset of A's attributes initial or otherwise.

Fifth Normal Form

A reltn is said to be 5NF iff

1. It is already in 4NF

2. There should not be any join dependencies

e.g.: table vendor supply

table 1

Vendorcode	Itemcode
V ₁	I ₁
V ₁	I ₂
V ₂	I ₂
V ₂	I ₃
V ₃	I ₁

Vendorcode	Projectcode
V ₁	P ₁
V ₂	P ₂
V ₃	P ₃

Table 3.

Itemode	Projectcode
I ₁	P ₁
I ₂	P ₁
I ₂	P ₂
I ₃	P ₂
I ₁	P ₃

- Pitfalls in a RDBMS / Anomalies in db.

stud_grade

normal form

Name	Course	Phone no.	Major	Professor	Grade
Jones	353	23746843	CS	Smith	A
Smith	329	43153876	Physics	Tucker	B
Martin	456	531-64789	Chemistry	Davis	B
Pike	293	444-78689	Maths	James	A+
Jones	319	237-46883	History	Harris	A

- Update Anomalies
- Insertion Anomalies
- Deletion Anomalies

• Name \leftarrow Phn no

• Name \leftarrow Major

• Course \leftarrow Professor

• Name course \leftarrow grade

(C,B,A) \rightarrow

The anomalies freed here are

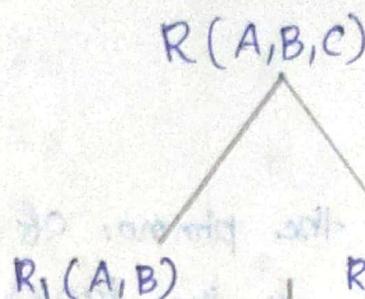
• Update Anomalies: - A change in the phn no. of jones must be need for consistency, in all the tuples pertaining to the student john.

• Insertion Anomalies: If this # is the only sltn in the db showing the association between the faculty member & the course, the fact that a given professor is teaching a given course cannot be entered to the db unless a student is registered in the course.

• Deletion Anomalies: If the only student registered in the given course discontinues the course the informts has to which professor is offering the course will be lost, if this is the only sltn in the db showing the Association b/w a faculty member & the course.

→ Properties of Relational Decomposition :- lossless & lossy

• Lossless join Decomposition:-



right → SW info. b
right → after getting data
from the decompos.
group → views easily,
eg:- studid, name, marks

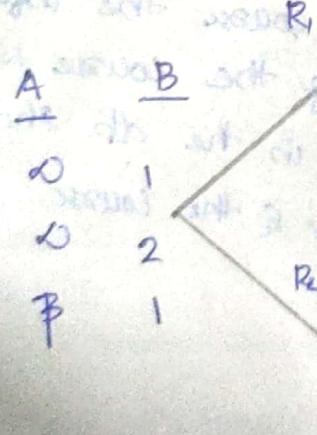
Recover

$$R'(A, B, C)$$

$$R(A, B, C) = R'(A, B, C)$$

• Lossy Decomposition:-

$$R = (A, B)$$



A	B
a	1
a	2
b	1
b	2

• Property 1

After decomposing & trying to retrieve original data, if the original information is lost it comes under lossy decomposition.

If we able to retrieve or reconstruct the original data that we had before applying decomposition even after decomposing & joining the table it comes under lossless decomposition.

The point here is that when we applying decomposition in a relational db compulsory it shld be lossless decompn.

• Property 2

+ No Redundancy

(see the sltn. shld be either in BCNF or in 3NF.

We want to keep dependencies since losing a dependency means the corresponding constraint can be checked only through natural join of the appropriate resultant relation in the decomposition. This could be very expensive, so our aim is to get a lossless dependency preserving decomposition.

Example: $R = (A, B, C)$, $F = (A \rightarrow B, B \rightarrow C)$

Decomposition of R : $R_1 = (A, C)$, $R_2 = (B, C)$

Solution: In R_1 the following dependencies hold: $F' = (A \rightarrow A, C \rightarrow C, A \rightarrow C, AC \rightarrow AC)$

augment $\rightarrow AC \rightarrow C$
suffix get $AC \rightarrow AC$

In R₂ the following dependencies hold : F² = {B → B, C → C, B → C, BC → BC}

The set of dependencies hold on R₁ ∪ R₂ : {B → C}, A → B cannot be

so decomposition is not desired so decomposition is not dependency preserving.

Example-1

R = (A, B, C) F² = {A → B, B → C}

Decomposition of R : R₁ = (A, B), R₂ = (B, C)

Does the decomposition preserve the given dependencies?

Ans:- In R₁ the following dependencies hold : F¹ = {A → A, B → B, B → A}

In R₂ the following dependencies hold : F² = {B → B, C → C, C → B}

The set of dependencies hold on R₁ ∪ R₂ = {A → B, B → C}

This decomposition preserves the functional dependencies given in the original reln.

(R₁, R₂)

(A, B) → A, (A, B) → B, (B, C) → C

(A → B, B → C)