

Initialisation code

Choose a and b as per choice

```
a = 1;
b = 1;
length = 10;
```

```
In[ ]:= getM[n_, gm_, a_, b_] := Module[{M, i, j}, M = Table[0, {n}, {n}];
  For[i = 1, i ≤ n, i++,
    {
      If[i == 1, For[j = 2, j ≤ b + 1, j++, M[[i, j]] = 1 - gm], Unevaluated[Sequence[]]];

      If[i == n, For[j = n - a, j ≤ n - 1, j++, M[[i, j]] = gm], Unevaluated[Sequence[]]];
      If[2 ≤ i ≤ n - b, M[[i, i + b]] = 1 - gm, Unevaluated[Sequence[]]];
      If[a + 1 ≤ i ≤ n, M[[i, i - a]] = gm, Unevaluated[Sequence[]]];
    }
  ];
  {M[[1, 1]] = 1 - gm, M[[n, n]] = gm};
  M]
```

```
In[ ]:= getM[length + 1, γ, a, b] // Transpose // MatrixForm
```

Out[]//MatrixForm=

$$\begin{pmatrix} 1-\gamma & \gamma & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1-\gamma & 0 & \gamma & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1-\gamma & 0 & \gamma & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1-\gamma & 0 & \gamma & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1-\gamma & 0 & \gamma & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1-\gamma & 0 & \gamma & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1-\gamma & 0 & \gamma & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1-\gamma & 0 & \gamma & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1-\gamma & 0 & \gamma & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1-\gamma & 0 & \gamma \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1-\gamma & \gamma \end{pmatrix}$$



```
In[ ]:= P[γ_] := DiscreteMarkovProcess[ReplacePart[ConstantArray[0, length + 1], 2 → 1],
  getM[length + 1, γ, a, b] // Transpose];
D = .;
D[γ_] := StationaryDistribution[P[γ]]
```

```

In[ ]:= K = length;
p = 0.4;
p1 = 0;
p2 = 0.8;
simply = Table[Simplify[PDF[ $\mathcal{D}[\gamma]$ , i + 1]], {i, 0, length, 1}];
th = .;
q[i_,  $\gamma$ _] :=  $\gamma p + (1 - \gamma) p_i$ ;
sols = Table[qs = Table[If[i ≤ th, q[1,  $\gamma$ ], q[2,  $\gamma$ ]], {i, 0, K, 1}] /. th → j;
temp = simply.qs;
{j,  $\gamma$  /. Solve[temp == 0.5 &&  $\gamma > 0$  &&  $\gamma < 1$ ,  $\gamma$ ] // Quiet} // Flatten,
{j, Range[0, K]}}];

In[ ]:= toplone = Select[sols, Length[#] == 3 &];

{covercol, cashcol} = ColorData[97, "ColorList"][[{1, 2}]];
col[x_] := Blend[{covercol, cashcol}, x]
gammastopl = Table[i, {i, 0, 1, 0.1}];
coltopl = Table[col[1 - gammastopl[[i]]], {i, Length[gammastopl]}}];

Out[ ]:= {, }

In[ ]:= q[i_,  $\gamma$ _] :=  $\gamma p + (1 - \gamma) p_i$ ;
Pwin[ $\gamma$ _, th_] :=  $q[1, \gamma] \times \sum_{i=0}^{th} \text{PDF}[\mathcal{D}[\gamma], i + 1] + q[2, \gamma] \times \sum_{i=th+1}^K \text{PDF}[\mathcal{D}[\gamma], i + 1]$ ;
extremes = {{0, Pwin[0, 1]}, {1, Pwin[1, 1]}};
explorethresh = Range[0, 5, 1];
pwinlist = Table[{ $\gamma$ , Pwin[ $\gamma$ , th]}, {th, explorethresh}, { $\gamma$ , 0, 1, 0.01}];

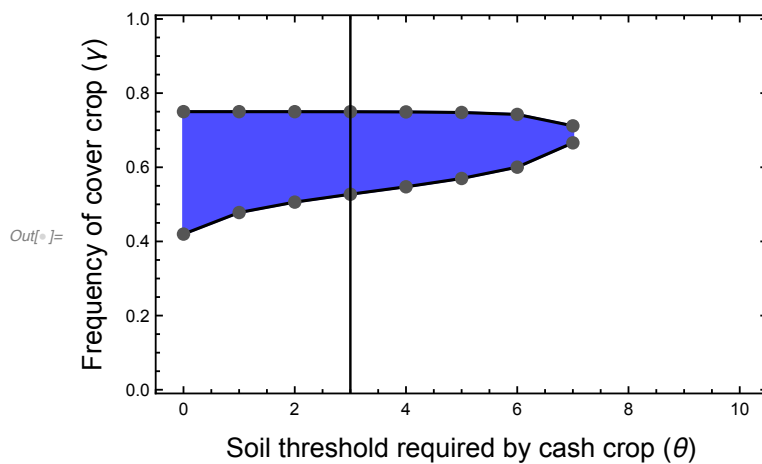
```

Plotting

```

In[ ]:= ListPlot[{toplone[[All, {1, 2}]], toplone[[All, {1, 3}]]},
  PlotStyle → {Black}, PlotRange → {{-0.5, K + 0.5}, {-0.01, 1.01}},
  Frame → True, FrameStyle → Directive[Black, Thickness[0.003]],
  FrameLabel → {Style["Soil threshold required by cash crop ( $\theta$ )", 14, Black],
    Style["Frequency of cover crop ( $\gamma$ )", 14, Black]}, Joined → True,
  Mesh → All, Filling → {1 → {2}}, FillingStyle → Lighter[Blue, 0.3],
  MeshStyle → {PointSize[Large], Darker[Gray]}, GridLines → {{3}, None},
  GridLinesStyle → Directive[{Black, Thickness[0.004]}],
  Method → {"GridLinesInFront" → True}]

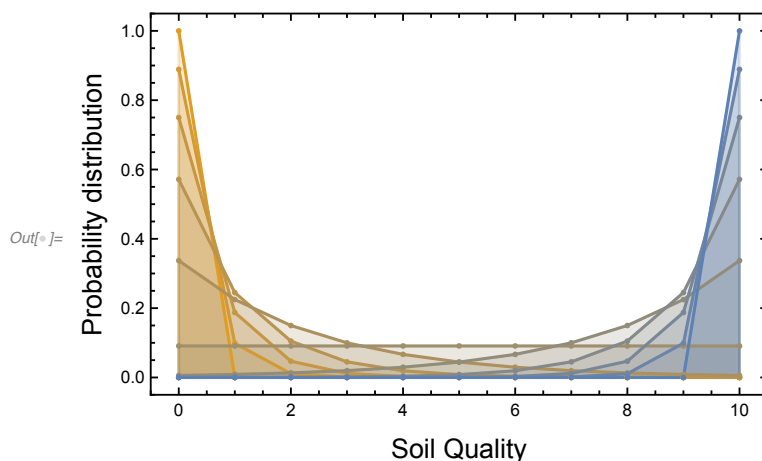
```



```

In[ ]:= ListPlot[Table[{k - 1, PDF[D[gamma], k]}, {gamma, gammastopl}, {k, 1, length + 1}],
  PlotStyle → coltopl, (*PlotLegends→gammastopl,*)Joined → True,
  Mesh → All, PlotRange → {{-0.5, length + 0.5}, {-0.05, 1.05}},
  Frame → True, FrameStyle → Directive[Black, Thickness[0.003]],
  FrameLabel → {Style["Soil Quality", 14, Black],
    Style["Probability distribution", 14, Black]}, Filling → Axis]

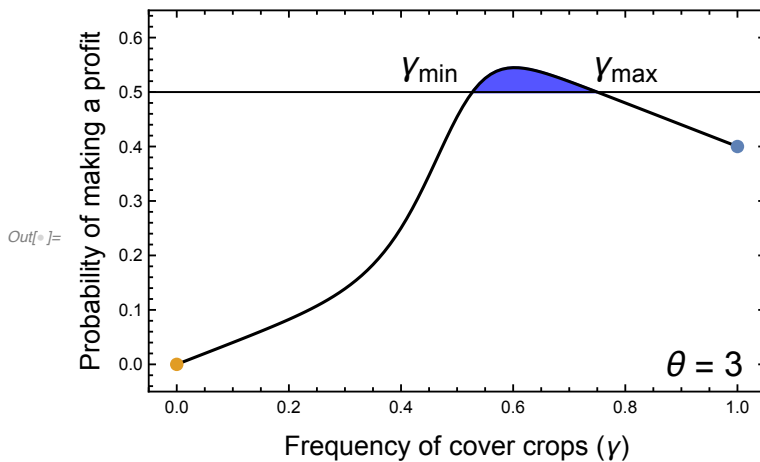
```



```

In[ ]:= ListPlot[pwinlist[[4]], Joined → True, Frame → True,
  FrameStyle → Directive[Black, Thickness[0.003]],
  FrameLabel → {Style["Frequency of cover crops ( $\gamma$ )", 14, Black],
    Style["Probability of making a profit", 14, Black]}, PlotStyle → Black,
  PlotRange → {{-0.05, 1.05}, {-0.05, 0.65}}, GridLines → {None, {0.5}},
  GridLinesStyle → Directive[{Black, Thickness[0.0032]}],
  Filling → {1 → {0.5, {None, Lighter[Blue]}},},
  Epilog → {PointSize[Large], cashcol, Point[extremes[[1]],
    PointSize[Large], covercol, Point[extremes[[2]], Black,
    Inset[Style[" $\gamma_{\min}$ ", 18], {0.45, 0.55}], Inset[Style[" $\gamma_{\max}$ ", 18], {0.8, 0.55}],
    Inset[Style[" $\theta = "$  <> ToString[explorethresh[[4]], 18], {0.94, 0}]}],
  Method → {"GridLinesInFront" → True}]

```



```

Manipulate[ListPlot[pwinlist[[j]], Joined → True,
  Frame → True, FrameStyle → Directive[Black, Thickness[0.003]],
  FrameLabel → {Style["Frequency of cover crops ( $\gamma$ )", 14, Black],
    Style["Probability of making a profit", 14, Black]}, PlotStyle → Black,
  PlotRange → {{-0.05, 1.05}, {-0.05, 0.65}}, GridLines → {None, {0.5}},
  GridLinesStyle → Black, Filling → {1 → {0.5, {None, Lighter[Blue]}},},
  Epilog → {PointSize[Large], cashcol, Point[extremes[[1]],
    PointSize[Large], covercol, Point[extremes[[2]], Black,
    Inset[Style[" $\gamma_{\min}$ ", 18], {0.45, 0.55}], Inset[Style[" $\gamma_{\max}$ ", 18], {0.8, 0.55}],
    Inset[Style[" $\theta = "$  <> ToString[explorethresh[[j]], 18], {0.94, 0}]}],
  {j, Range[Length[explorethresh]]}]

```