

Assignment 2

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April 21, 2018

1 Task 1

main function (sth here)

```
proc EMIRP(value  $n : \mathbb{N}$ , result  $r : \mathbb{N}$ )..  
   $\sqsubseteq n, r : \left[ \begin{array}{l} n > 0, \\ \sum_{i=1}^r \text{emirp}(i) = n \wedge \sum_{i=1}^{r-1} \text{emirp}(i) = n - 1 \end{array} \right] \neg(1)$ 
```

where (sth here)

$$\text{emirpVal}(i) = \begin{cases} 1 & \text{if } \text{isPrime}(i) \wedge \text{isPrime}(\text{reverse}(i)) \wedge i \neq \text{reverse}(i) \\ 0 & \text{else} \end{cases}$$

2 Task 2

```
(1)  $\sqsubseteq$        $\langle \text{c-frame} \rangle$   
   $r : \left[ \begin{array}{l} n > 0, \\ \sum_{i=1}^r \text{emirp}(i) = n \wedge \sum_{i=1}^{r-1} \text{emirp}(i) = n - 1 \end{array} \right]$   
   $\sqsubseteq$        $\langle \text{i-loc} \rangle$   
   $\sqsubseteq \text{var } j : r, j : \left[ \begin{array}{l} n > 0, \\ \sum_{i=1}^r \text{emirp}(i) = n \wedge \sum_{i=1}^{r-1} \text{emirp}(i) = n - 1 \end{array} \right] \neg(2)$ 
```

We construct the loop to verify the prime

$$\begin{aligned}
(2) \sqsubseteq & \quad \langle \mathbf{c\text{-}frame} \rangle \\
& \sqcup \mathbf{var} j : r, j : \left[\begin{array}{l} n > 0, \\ Inv \end{array} \right] \neg(3); \\
& \sqcup \mathbf{var} j : r, j : \left[\begin{array}{l} Inv, \\ \sum_{i=1}^r emirp(i) = n \wedge \sum_{i=1}^{r-1} emirp(i) = n - 1 \end{array} \right] \neg(4);
\end{aligned}$$

where the loop invariant is defined by

$$Inv = \left(\sum_{i=1}^j emirp(i) = n \wedge \sum_{i=1}^{j-1} emirp(i) = n - 1 \wedge \right)$$