
Automating it

simp and auto

simp rewriting and a bit of arithmetic

auto rewriting and a bit of arithmetic, logic & sets

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- Show you where they got stuck

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auto rewriting and a bit of arithmetic, logic & sets

- Show you where they got stuck
- highly incomplete wrt logic

blast

- A **complete** (for FOL) tableaux calculus implementation

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- Covers logic, sets, relations, ...

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- Extensible with intro/elim rules
- **Almost no “=”**

Demo: blast

blast: A 2-stage implementation

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Isabelle follows the LCF architecture

fast and friends

fast slow and incomplete version of *blast*

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fastsimp rewriting and logic

fast and friends

fast slow and incomplete version of *blast*

fastsimp rewriting and logic

force slower but completer version of *fastsimp*

metis

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metis

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- Can deal with bidirectional “=”
- Knows only pure logic, not sets etc

Demo: beyond blast

Problems

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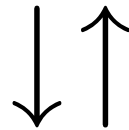
- Most proofs require additional lemmas.
- Adding arbitrary lemmas slows *blast* down significantly; *metis* copes better.
- Finding the right lemmas in a library of thousands of lemmas is light years beyond *blast* and *metis*.
- There are highly optimized *ATPs* (automatic theorem provers) for FOL that can deal with large libraries ...

Sledgehammer



Architecture

Isabelle

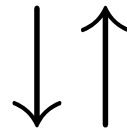


ATPs

Architecture

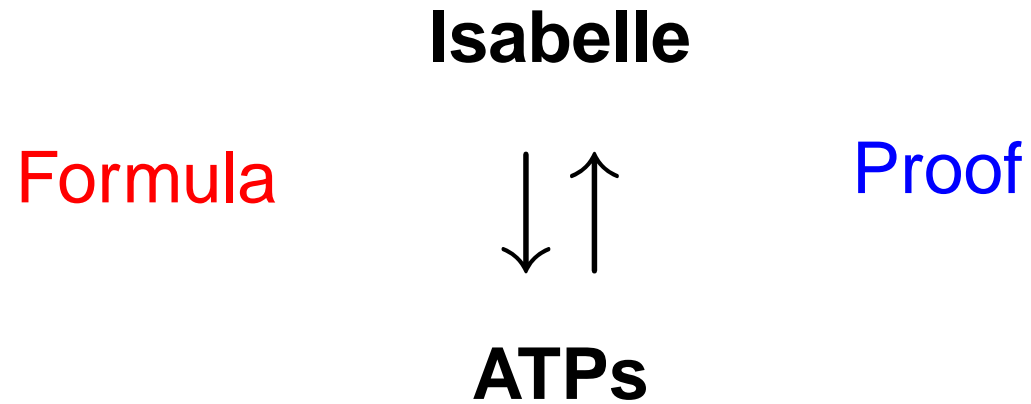
Isabelle

Formula

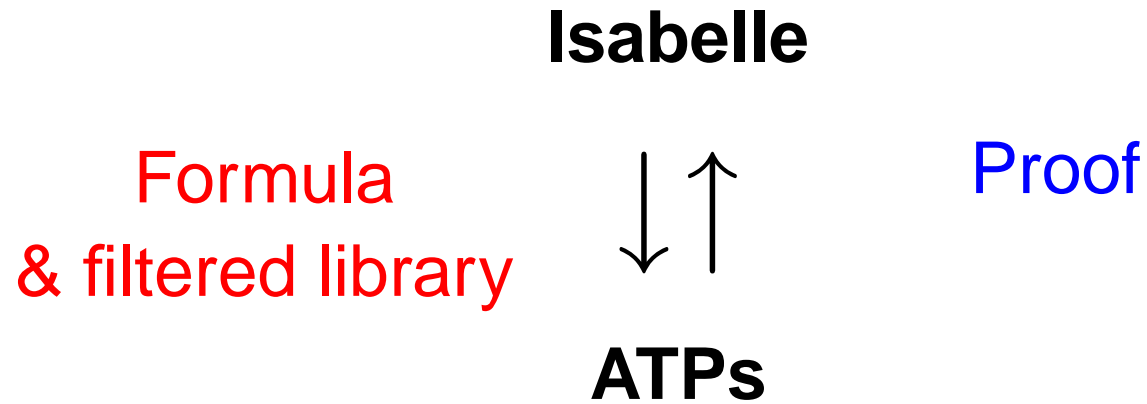


ATPs

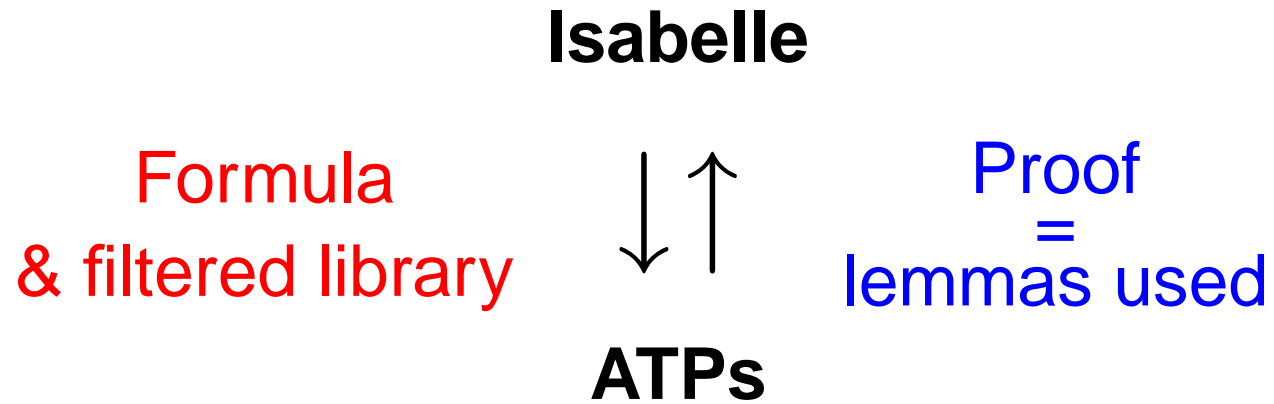
Architecture



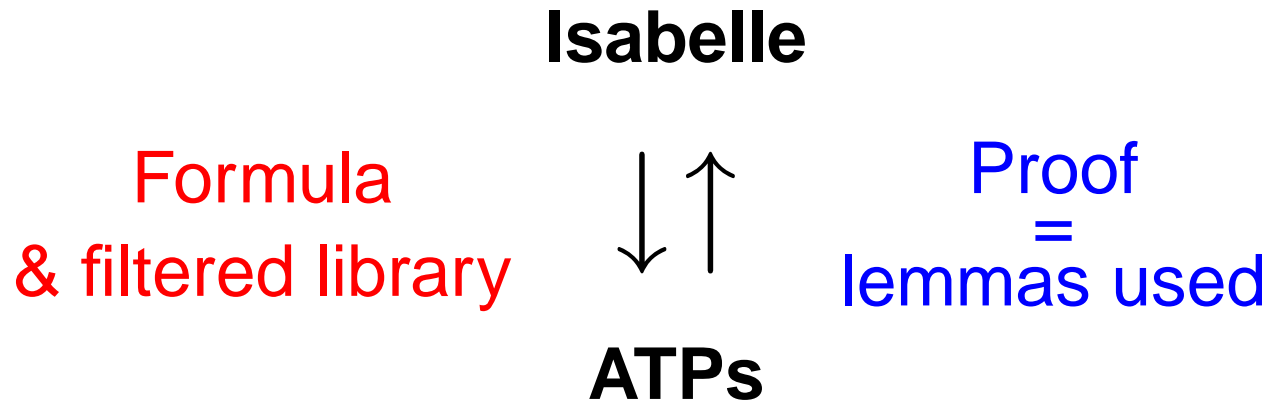
Architecture



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Empirical study:

Sledgehammer works for 1/3 of non-trivial Isabelle proofs

Demo: Sledghehammer

Automating Arithmetic

Automating arithmetic

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- complete for quantifier-free *real* arithmetic

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- complete for quantifier-free *real* arithmetic
- complete for first-order theory of *nat* and *int* (Presburger arithmetic)

Automating arithmetic

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An incomplete but (often) fast method for the quantifier-free
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Idea: (re)write polynomials as sums-of-squares to prove
non-negativity

Demo: Arithmetic