

# ANALYSIS OF PANEL DATA

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Fixed-Effect and Random-Effect Models

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# Fixed-Effect Model

# An Introduction to Fixed-Effect Models

# A More General Form

$$y_{it} = \beta_1 x_{it1} + \cdots + \beta_k x_{itk} + a_i + u_{it}, \quad i = 1, \dots, N, t = 1, \dots, T$$

Fixed-effect, potentially correlated with explanatory variables

$$\bar{y}_i = \beta_1 \bar{x}_{i1} + \cdots + \beta_k \bar{x}_{ik} + \bar{a}_i + \bar{u}_i$$

Form time averages for each individual.

$$\Rightarrow [y_{it} - \bar{y}_i] = \beta_1 [x_{it1} - \bar{x}_{i1}] + \cdots + \beta_k [x_{itk} - \bar{x}_{ik}] + [u_{it} - \bar{u}_i]$$

Because  $a_i - \bar{a}_i = 0$  (the fixed effect is removed)

- Estimate time-demeaned equation by OLS.
- Uses time variation within cross-sectional units (= within-estimator).

# Within Estimation

- The *fixed effect transformation* is also called *within transformation*, in which *within* can be read as within each of the subjects in the dataset: each of the cross-sectional subjects' data is demeaned leveraging on time variation in both  $y$  and  $x$  and more importantly, the *unobserved individual heterogeneity* is eliminated within each of the individuals.
- The *fixed effect estimator* is also called *within estimator*.
- Because the transformation relies on time variation within each of the cross-sectional subjects, those variables without much variation to begin with will become (almost) a constant after the transformation, resulting in imprecise estimates.

# Between Estimation

- **Between Estimators:** The OLS estimators on the cross-sectional average equation introduced above, from which we subtract the cross-sectional equation, is called the  $\$$ .
- We will not discuss the  $\$$ , as it is biased when the observed explanatory variables,  $x'$ s, are correlated with the unobserved fixed effect,  $a_i$ . Also, it does not utilize the panel data efficiently: it does not leverage on the time varying information.
- If we think that the observed explanatory variables and the unobserved fixed effect are not correlated, then we should use **random effect model**, which we will discuss later in this lecture.

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