

# ANALYSIS OF PANEL DATA

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Fixed-Effect and Random-Effect Models

**datascience@berkeley**

# Fixed-Effect Model

# Remarks on Fixed-Effect Models

# Deterministic Time-Varying and Time-Invariant Variables

- The fixed effect estimator allows for correlation between  $a_i$  and the explanatory variables in any time period, as in the case in first-differencing.
- A side-effect is that all of the time-invariant variables are eliminated alongside with the unobserved fixed effect. As such, variables such as gender, credit score at loan origination, a biometric measure at the beginning of using a wearable, the distance between the center of a city to the nearest port, etc., will all be swept away by the fixed effect transformation. As such, the effect of time-invariant variables cannot be estimated
- That said, the effect of interactions with time-invariant variables can be estimated (e.g. the interaction of education with time dummies)
- If a full set of time dummies are included, the effect of deterministic time-varying variables (e.g. experience) cannot be estimated because they cannot be distinguished from the aggregate time effect.

# Assumptions Required for valid OLS Estimation

- Under a \$ assumption on the explanatory variables, the fixed effect estimator is unbiased: the error term  $\epsilon_{it}$  is uncorrelated with all of the explanatory variables across all time period:

$$E(\epsilon_{it}|X_i, a_i) = 0 \forall t$$

- Other assumptions require that the error term be homoskedastic and serially uncorrelated across  $t$ .

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