

# CP 8318 Assignemnt 2

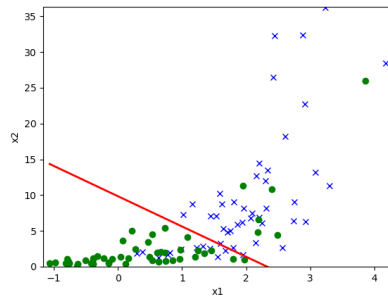
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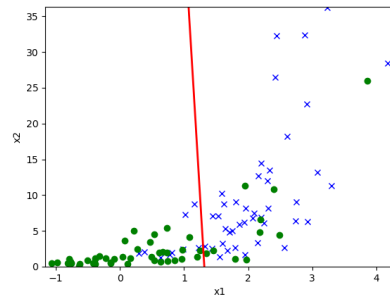
## 1

### 1.1 Question 3

The resulting line for logistic regression gives the appearance of a more true division between the two groups. On the other hand the GDA line lands where would likely be the actual middle of the two, which implies that that is the overlap of the two distributions. From this it seems that logistic regression will fit well for a specific dataset (in this scenario), while the GDA will fit better for the ‘general’ case. By this, I mean that as we see more data, the logistic regression will create a more accurate division while the GDA will remain unchanged since it is working from the underlying distribution.



(a) Log Reg

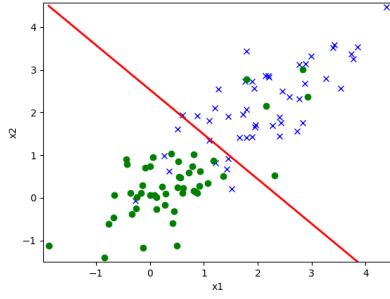


(b) GDA

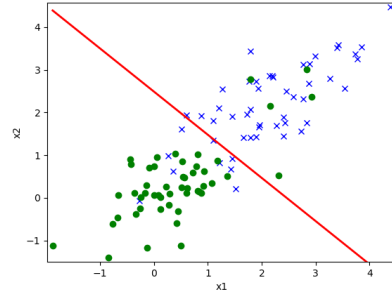
### 1.2 Question 4

In this case, the two seem quite similar. The difference is only visible (in the given figures) at the x-intercept, and even then zooming in is required. The logistic regression is further from an intercept of 4 than the GDA is, but only slightly. Checking the count of datapoints in the files we have 800 in the training files, and 100 in the valid files. This is the same for the previous example, and thus the only conclusion here is that the logistic regression was quite close by

coincidence. Indeed, with this dataset there appears to be a more identical form to the two distributions. Perhaps its this apparent fact that leads to the result that we have here.



(a) Log Reg



(b) GDA

### 1.3 Question 5

I suspect that normalizing the distributions, and then translating them so that only their tails overlap would potentially affect the results in the first dataset. It appears that the first dataset has a platykurtic (group a) distribution and a leptokurtic (group b) distribution which seems to be skewed toward the left. This being the case, then normalizing them and translating the two so that quartile 4 of group a overlaps with quartile 1 of group b may yield significantly better results since that seems to be the ideal situation for GDA (supposing the data point count is not too high).

## 2

### 2.1 Question 1

$$\begin{aligned}
 p(y; \lambda) &= \frac{e^{-\lambda} \lambda^y}{y!} \\
 &= e^{\ln(\frac{e^{-\lambda} \lambda^y}{y!})} \\
 &= e^{\ln(e^{-\lambda}) + \ln(\lambda^y) - \ln(y!)} \\
 &= e^{\ln(-\lambda + y \ln(\lambda) - \ln(y!))} \\
 &= e^{\ln(-\lambda + y \ln(\lambda))} e^{-\ln(y!)} \\
 &= \frac{1}{y!} e^{y \ln(\lambda) - \lambda}
 \end{aligned}$$

Thus we have natural parameters:

$$b(y) = \frac{1}{y!}$$

$$\eta = \ln(\lambda)$$

$$T(y) = y$$

$$a(\eta) = \lambda$$

## 2.2 Question 2

$$\begin{aligned} g(n) &= E[y; \eta] \\ &= E[y; \ln(\lambda)] \\ &= E(e^y; \lambda) \\ &= \end{aligned}$$

## 2.3

## 2.4 Question 4

The graph shown in 3 displays a marked difference between the true value of the dataset, and the predicted value. Were it otherwise, the data would fit closer to a line, however as it stands it appears to have something close to a normal distribution in terms of how off the data is. This is supported by the clear linear trend of the overall data. It is then clear that the prediction has some source of error within which results in it being in the ballpark, but still not correct by some margin.

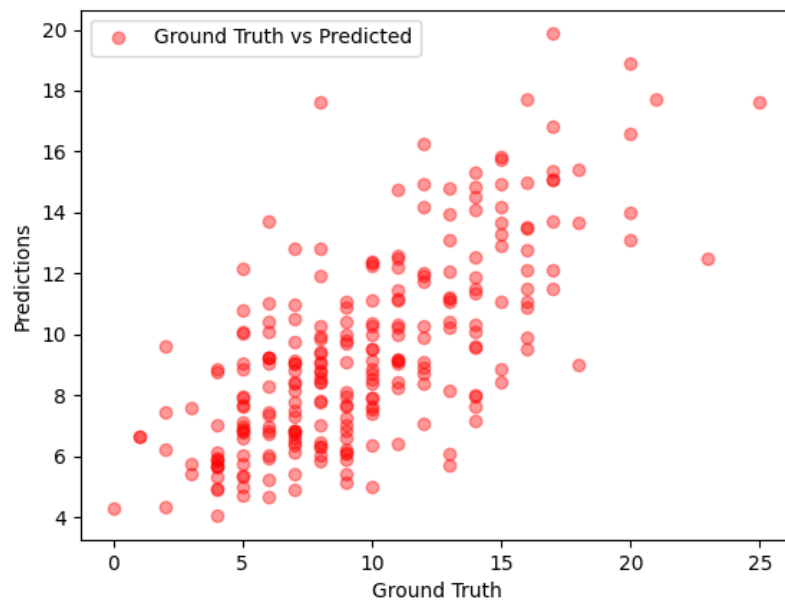


Figure 3: Poisson Regression