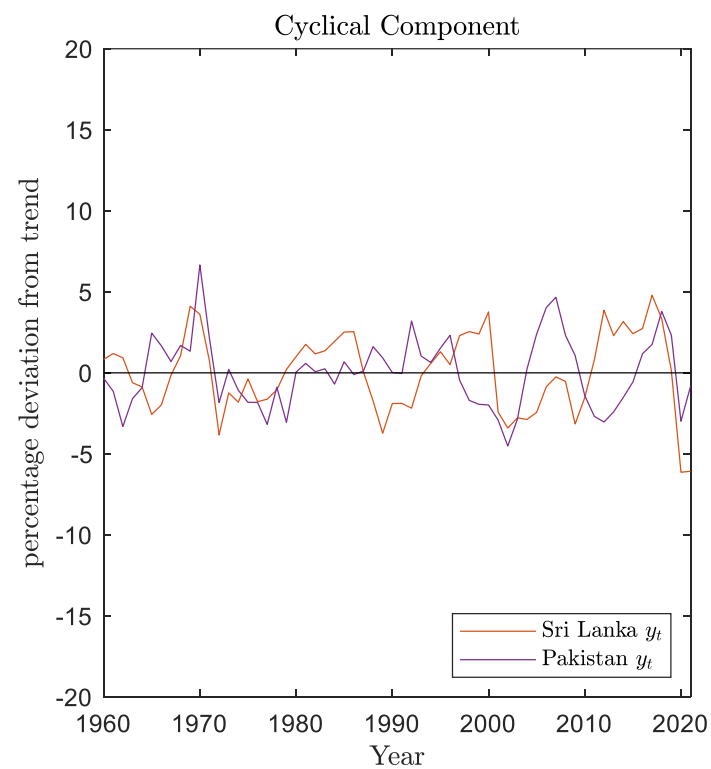
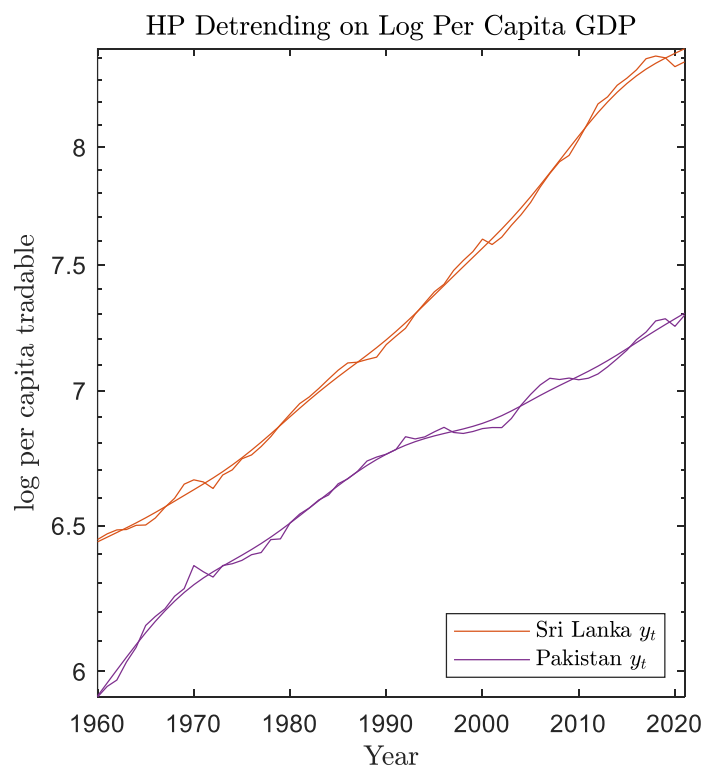


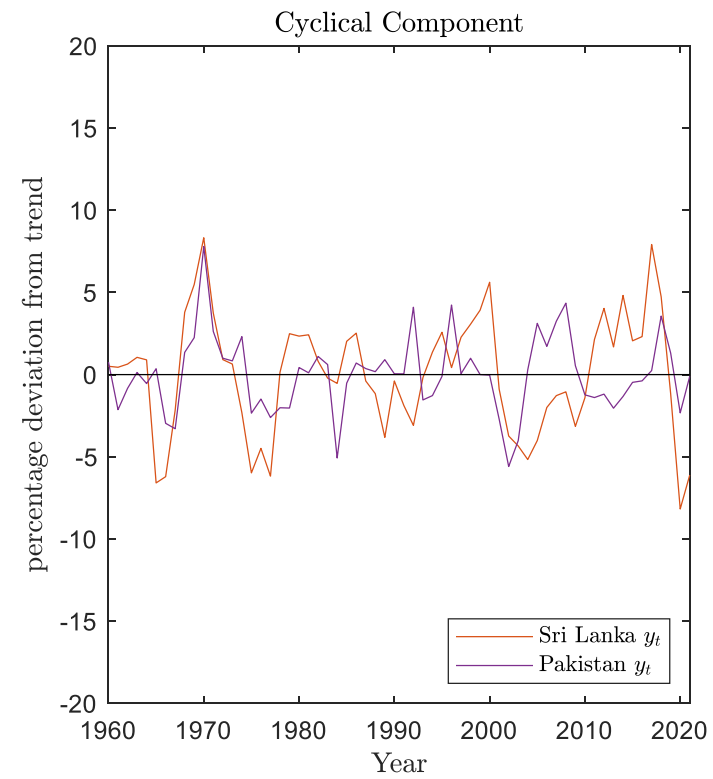
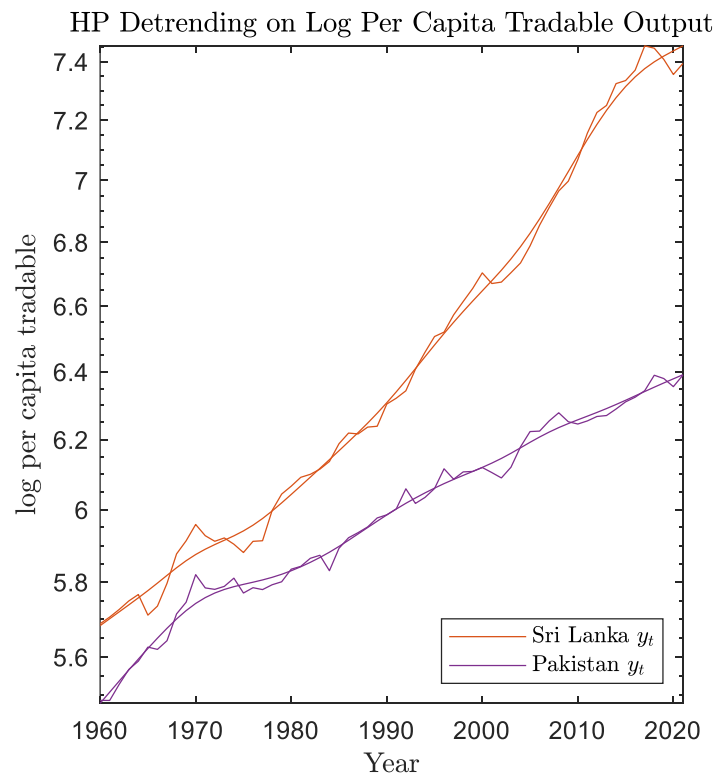
## Output Process

- 比較使用不同 filtering (HP-Filter/ Removing Log Quadratic trend) 與 Output proxy(Real GDP / Real Tradable GDP)，所產生的  $y^T$

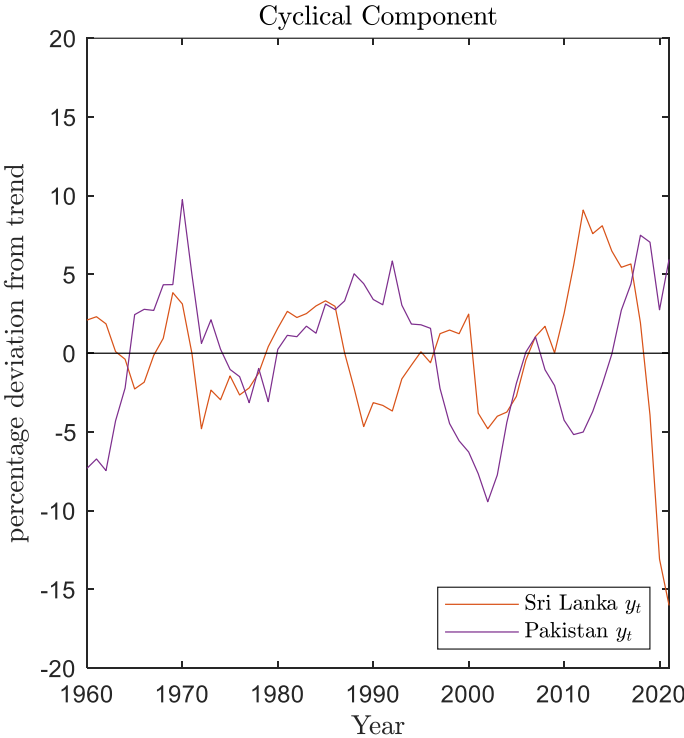
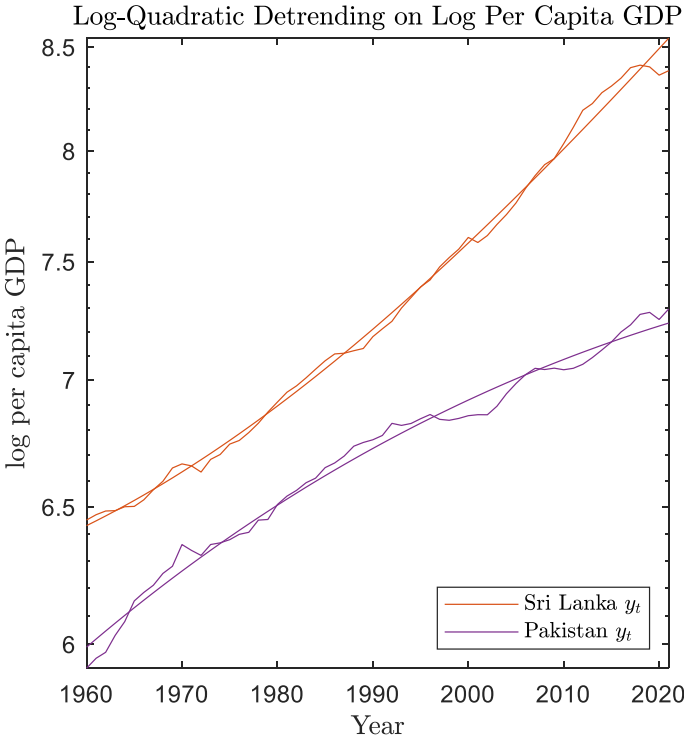
## GDP + HP filter



## Tradable + HP filter

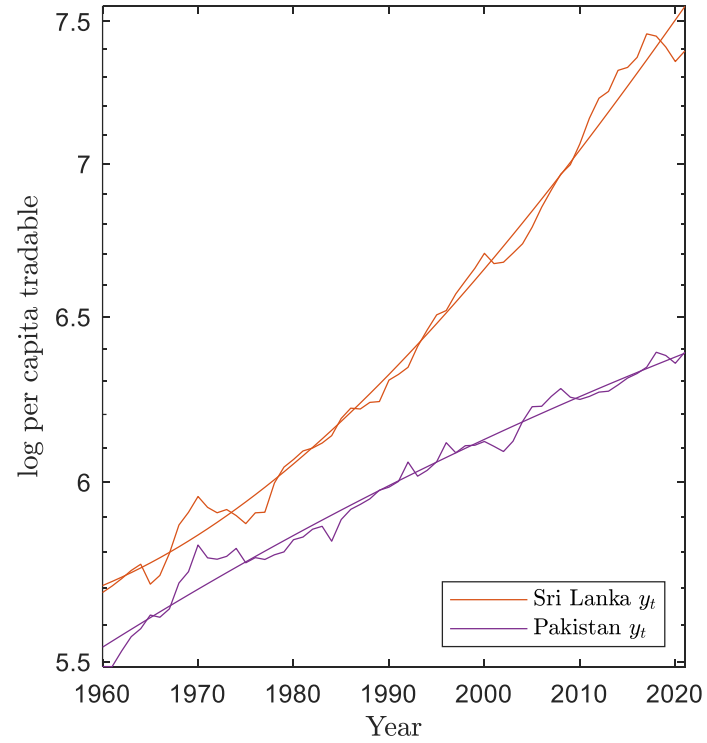


GDP + Log-quadratic

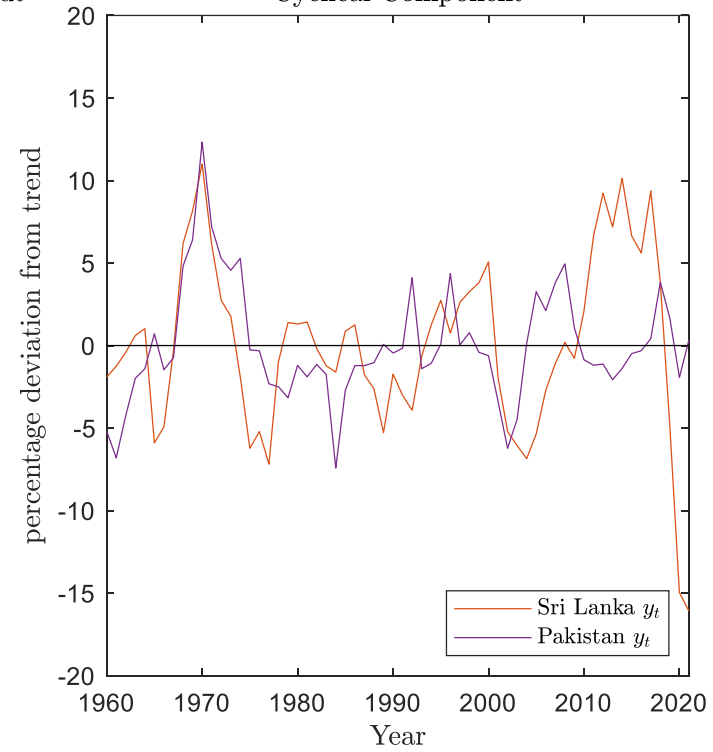


## Tradable + Log-quadratic

Log-Quadratic Detrending on Log Per Capita Tradable Output



Cyclical Component



結果如下表：

| Output Proxy    | Filtering | Sri Lanka |          |                   | Pakistan |          |                   |
|-----------------|-----------|-----------|----------|-------------------|----------|----------|-------------------|
|                 |           | $\rho$    | $\sigma$ | Unconditional std | $\rho$   | $\sigma$ | Unconditional std |
| <b>GDP</b>      | HP        | 0.912     | 0.0122   | 2.98%             | 0.9008   | 0.0110   | 2.52%             |
| <b>Tradable</b> | HP        | 0.9114    | 0.0180   | 4.37%             | 0.8518   | 0.0116   | 2.21%             |
| <b>GDP</b>      | Log-Q     | 0.9326    | 0.0212   | 5.88%             | 0.9585   | 0.0216   | 7.56%             |
| <b>Tradable</b> | Log-Q     | 0.9325    | 0.0266   | 7.38%             | 0.9239   | 0.0174   | 4.55%             |

使用不同 output proxy 與 filtering 的組合估計  $(\beta, \delta_1, \delta_2)$  的結果。注意，當使用 tradable output 作為 output 的 proxy 時，估計時的 target 會由 debt-to-GDP 變為 debt-to-tradable GDP。

| Output Proxy    | Filtering | Sri Lanka |            |            | Pakistan |            |            |
|-----------------|-----------|-----------|------------|------------|----------|------------|------------|
|                 |           | $\beta$   | $\delta_1$ | $\delta_2$ | $\beta$  | $\delta_1$ | $\delta_2$ |
| <b>GDP</b>      | HP        | 0.7302    | -0.5292    | 0.5995     | 0.6947   | -0.4939    | 0.5482     |
| <b>Tradable</b> | HP        | 0.7499    | -0.2532    | 0.339      | 0.6912   | -0.4799    | 0.5408     |
| <b>GDP</b>      | Log-Q     | 0.805     | -0.4834    | 0.5755     | 0.8297   | -0.4408    | 0.5225     |
| <b>Tradable</b> | Log-Q     | 0.9186    | -0.2000    | 0.2981     | 0.9229   | -0.4424    | 0.5186     |

(Seems that  $y^T$  received by removing the log quadratic term yields a more sensible subjective discount parameter.)

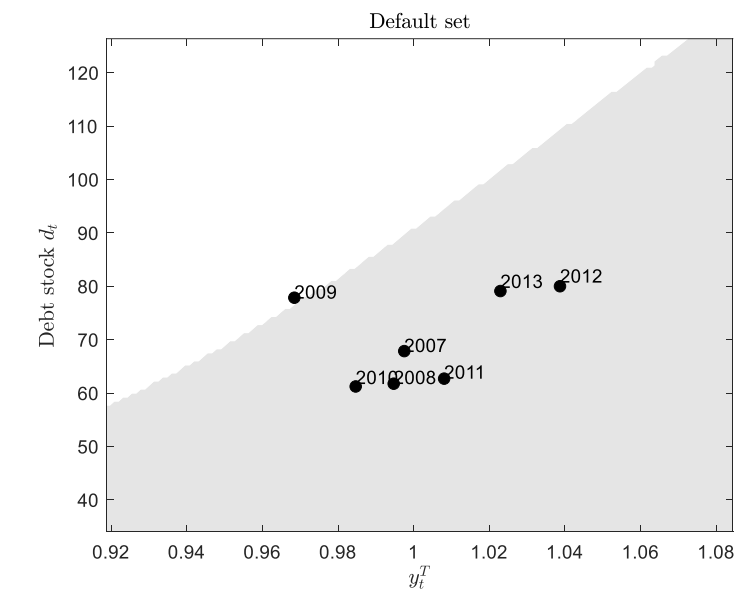
### Default set

座標上的 debt level，是由  $\text{total debt} / \text{nominal GDP}$  而來。若  $y_T$  的 proxy 是 tradable GDP，則會是  $\text{total debt} / \text{nominal tradable GDP}$ 。

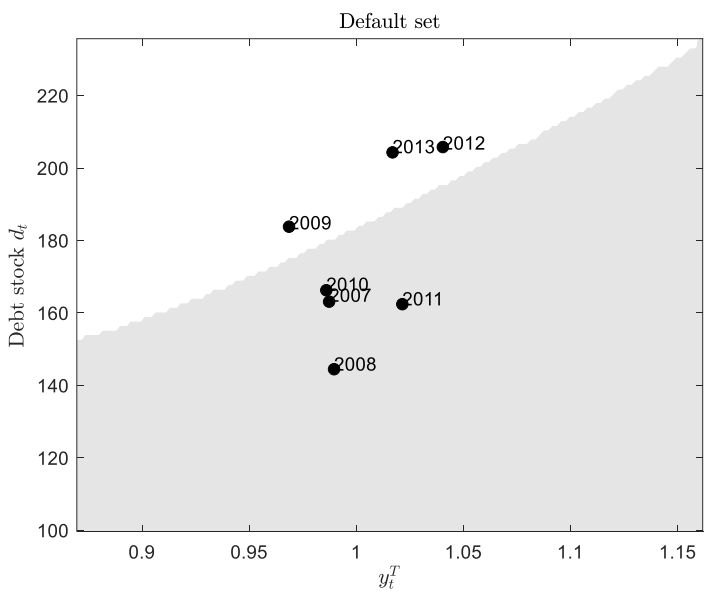
與 target debt ratio 時的做法相同，我將計算後的  $\text{annual debt-to-GDP ratio} * 0.37 (\text{haircut}) * 4 (\text{quarters})$ ，表示 unsecured debt to GDP ratio per quarter.

Sri Lanka

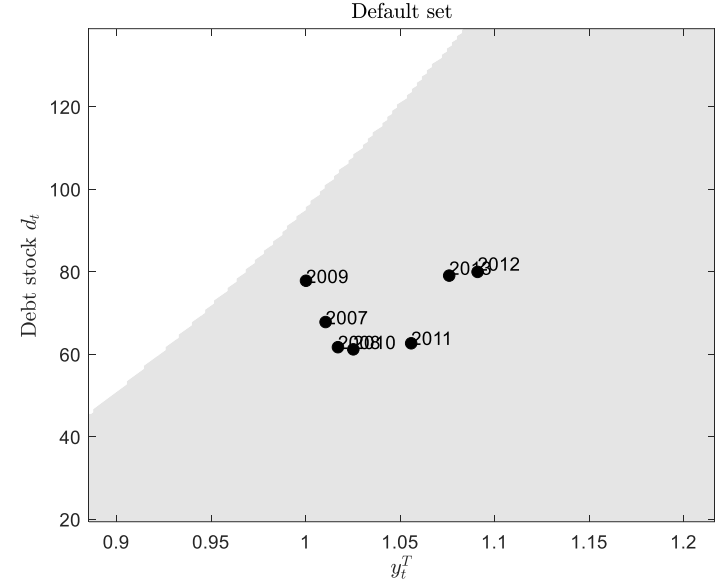
GDP + HP



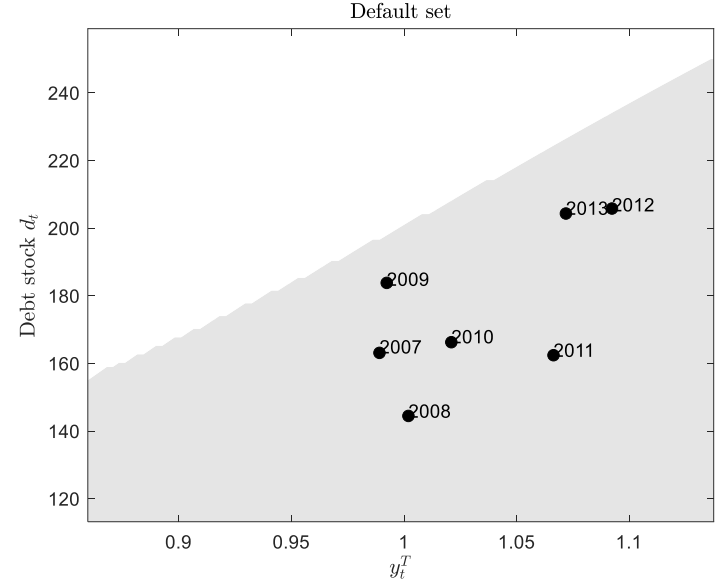
Tradable + HP



GDP +log-quadratic



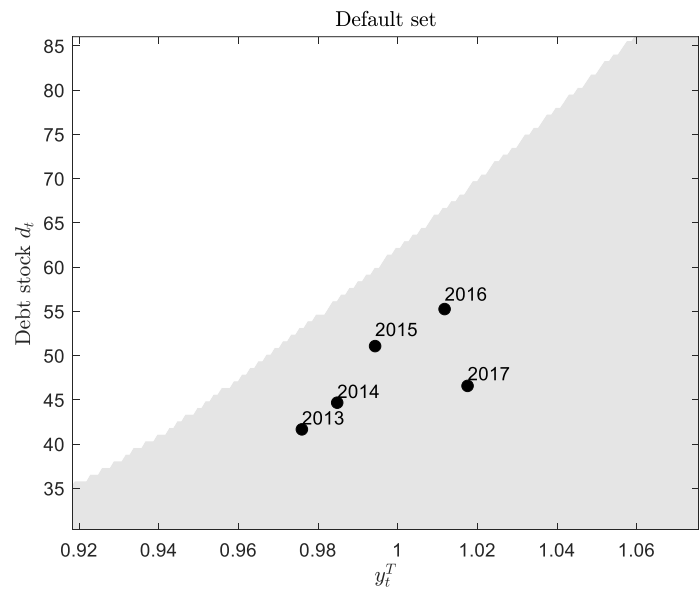
Tradable + log-quadratic



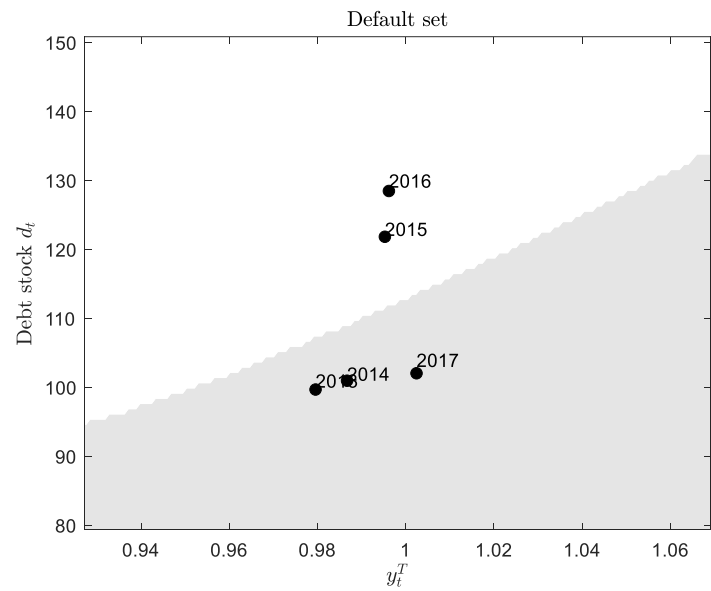


Pakistan

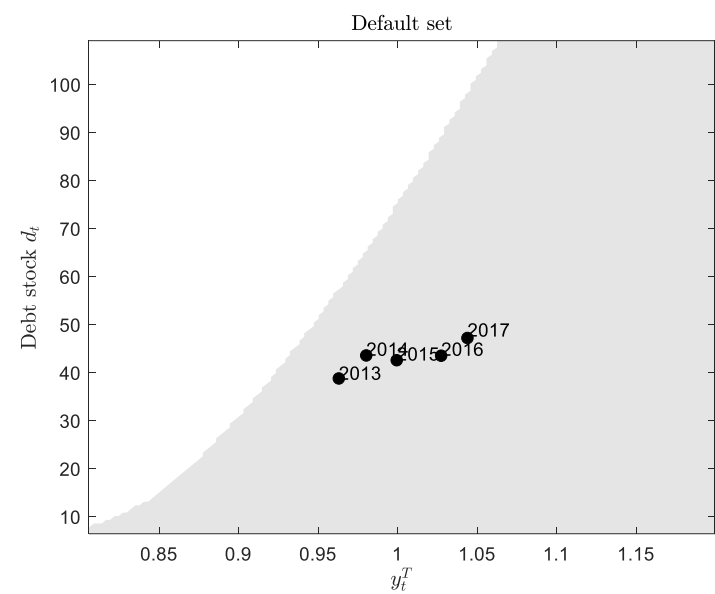
GDP + HP



Tradable + HP



GDP +log-quadratic



Tradable + log-quadratic

