HW 4

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Problem 4

a)

```
## (Intercept) Area Elevation Nearest Scruz
## 3.1548078779 -0.0005799429 0.0035405940 0.0088255719 -0.0057094223
## Adjacent
## -0.0006630311
## [1] 716.8458
```

The values of the coefficients and the deviance is shown in the output above.

b)

The form of the adjusted dependent variable is:

```
z = eta + (y-mu)*(d.eta.d.mu)
```

The eta is 4.060443, 3.4339872, 1.0986123, 3.2188758, 0.6931472, 2.8903718, 3.1780538, 2.3025851, 2.0794415, 0.6931472, 4.574711, 4.5325995, 4.060443, 1.6094379, 3.6888795, 5.8493248, 3.9318256, 0.6931472, 4.6443909, 4.6821312, 2.4849066, 4.2484952, 5.6347896, 5.4680601, 6.0958246, 4.1271344, 5.6524892, 3.7841896, 2.7725887, 3.0445224, the d.eta.d.mu is 0.0172414, 0.0322581, 0.3333333, 0.04, 0.5, 0.05555556, 0.0416667, 0.1, 0.125, 0.5, 0.0103093, 0.0107527, 0.0172414, 0.2, 0.025, 0.0028818, 0.0196078, 0.5, 0.0096154, 0.0092593, 0.0833333, 0.0142857, 0.0035714, 0.0042194, 0.0022523, 0.016129, 0.0035088, 0.0227273, 0.0625, 0.047619, the variance of mu is 58, 31, 3, 25, 2, 18, 24, 10, 8, 2, 97, 93, 58, 5, 40, 347, 51, 2, 104, 108, 12, 70, 280, 237, 444, 62, 285, 44, 16, 21, and the weights are 58, 31, 3, 25, 2, 18, 24, 10, 8, 2, 97, 93, 58, 5, 40, 347, 51, 2, 104, 108, 12, 70, 280, 237, 444, 62, 285, 44, 16, 21.

$\mathbf{c})$

```
## (Intercept) Area Elevation Nearest Scruz
## 3.5191545412 -0.0005298484 0.0031643557 0.0025188990 -0.0037899780
## Adjacent
## -0.0006623523
## [1] 576.8075
```

The intercept is fairly close to the values computed by the glm function. The Area and Adjacent variables are very close to the final values. The other values appear to be on the right track, but are not close to their final values yet.

d)

```
## (Intercept) Area Elevation Nearest Scruz
## 3.2102594447 -0.0005651969 0.0034606226 0.0077171134 -0.0052400871
## Adjacent
## -0.0006604828
## [1] 570.9648
```

This deviance is fairly close to the glm deviance, but still can probably converge closer.

\mathbf{e}

```
##
     (Intercept)
                                    Elevation
                                                     Nearest
                           Area
##
    3.1562582546 -0.0005793855 0.0035379237 0.0087861184 -0.0056868875
##
        Adjacent
  -0.0006630167
##
   [1] "Iteration 1 Deviance: 725.51031962005"
##
##
     (Intercept)
                           Area
                                    Elevation
                                                     Nearest
    3.1548090631 -0.0005799422 0.0035405910 0.0088255087 -0.0057093801
##
##
        Adjacent
  -0.0006630313
##
   [1] "Iteration 2 Deviance: 760.699799799015"
##
     (Intercept)
                           Area
                                    Elevation
                                                     Nearest
                                                                      Scruz
##
    3.1548078779 -0.0005799429 0.0035405940 0.0088255719 -0.0057094223
##
        Adjacent
## -0.0006630311
##
   [1] "Iteration 3 Deviance: 761.977437469427"
##
                           Area
                                    Elevation
                                                     Nearest
                                                                      Scruz
     (Intercept)
##
    3.1548078779 -0.0005799429 0.0035405940 0.0088255719 -0.0057094223
##
        Adjacent
##
   -0.0006630311
##
   [1] "Iteration 4 Deviance: 761.979247760923"
##
                                    Elevation
     (Intercept)
                           Area
                                                     Nearest
##
    3.1548078779 - 0.0005799429 0.0035405940 0.0088255719 - 0.0057094223
##
        Adjacent
  -0.0006630311
##
  [1] "Iteration 5 Deviance: 761.979247765408"
##
     (Intercept)
                           Area
                                    Elevation
                                                     Nearest
                                                                      Scruz
    3.1548078779 -0.0005799429 0.0035405940 0.0088255719 -0.0057094223
##
##
        Adjacent
## -0.0006630311
   [1] "Iteration 6 Deviance: 761.979247765408"
##
     (Intercept)
                           Area
                                    Elevation
                                                     Nearest
                                                                      Scruz
##
    3.1548078779 -0.0005799429
                                0.0035405940 0.0088255719 -0.0057094223
##
        Adjacent
##
  -0.0006630311
   [1] "Iteration 7 Deviance: 761.979247765408"
##
##
     (Intercept)
                           Area
                                    Elevation
    3.1548078779 \ -0.0005799429 \ \ 0.0035405940 \ \ 0.0088255719 \ -0.0057094223
##
##
        Adjacent
## -0.0006630311
  [1] "Iteration 8 Deviance: 761.979247765408"
##
     (Intercept)
                                    Elevation
                                                     Nearest
                                                                     Scruz
                           Area
```

```
3.1548078779 -0.0005799429 0.0035405940 0.0088255719 -0.0057094223
##
        Adjacent
  -0.0006630311
  [1] "Iteration 9 Deviance: 761.979247765408"
##
     (Intercept)
                          Area
                                   Elevation
                                                    Nearest
                                                                    Scruz
   3.1548078779 -0.0005799429 0.0035405940 0.0088255719 -0.0057094223
##
##
        Adjacent
## -0.0006630311
## [1] "Iteration 10 Deviance: 761.979247765408"
```

The deviance is very close to the target after 10 iterations and appears to have converged. All of the coefficients are very close to the glm's as well.

Problem 6

a)

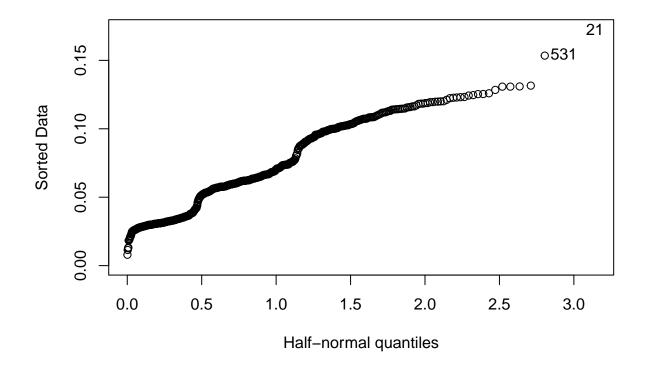
```
##
## Call:
## glm(formula = Shots ~ Team + Position + Tackles.per.90.min +
       Passes.per.90.min, family = "poisson", data = worldcup)
##
##
## Deviance Residuals:
##
       Min
                 1Q
                      Median
                                   3Q
                                            Max
## -3.9451 -1.4487 -0.3227
                               0.5258
                                         5.4445
##
## Coefficients:
##
                       Estimate Std. Error z value Pr(>|z|)
                                  0.200122
## (Intercept)
                       0.164837
                                              0.824 0.410119
## TeamArgentina
                       0.778391
                                  0.221968
                                              3.507 0.000454 ***
## TeamAustralia
                                  0.258458
                                            -0.611 0.541105
                      -0.157955
## TeamBrazil
                                  0.216579
                       0.832805
                                             3.845 0.000120 ***
## TeamCameroon
                       0.069575
                                  0.247975
                                             0.281 0.779038
## TeamChile
                                  0.235277
                                              1.201 0.229780
                       0.282551
## TeamDenmark
                      -0.094604
                                  0.252068
                                            -0.375 0.707430
## TeamEngland
                       0.460226
                                  0.229875
                                              2.002 0.045277 *
## TeamFrance
                      -0.167531
                                  0.259100 -0.647 0.517899
## TeamGermany
                       0.688142
                                  0.219869
                                             3.130 0.001749 **
## TeamGhana
                       0.840148
                                  0.214732
                                              3.913 9.13e-05 ***
## TeamGreece
                      -0.034924
                                  0.253378 -0.138 0.890372
## TeamHonduras
                      -1.035233
                                  0.330693 -3.130 0.001745 **
## TeamItaly
                       0.096256
                                  0.247014
                                             0.390 0.696776
## TeamIvory Coast
                       0.293131
                                  0.241622
                                              1.213 0.225061
## TeamJapan
                       0.142848
                                             0.590 0.555169
                                  0.242102
## TeamMexico
                       0.364535
                                  0.237609
                                              1.534 0.124986
## TeamNetherlands
                       0.788152
                                  0.219050
                                              3.598 0.000321 ***
## TeamNew Zealand
                      -0.633606
                                  0.314859
                                             -2.012 0.044183 *
                                  0.259024
## TeamNigeria
                      -0.169823
                                            -0.656 0.512065
                                  0.252334
                                             0.692 0.489247
## TeamNorth Korea
                       0.174491
## TeamParaguay
                       0.348329
                                  0.230826
                                              1.509 0.131285
## TeamPortugal
                                  0.230425
                       0.457938
                                              1.987 0.046883 *
## TeamSerbia
                       0.165891
                                  0.242190
                                             0.685 0.493369
## TeamSlovakia
                      -0.018986
                                  0.247267
                                            -0.077 0.938796
## TeamSlovenia
                      -0.517359
                                  0.302901 -1.708 0.087634 .
```

```
## TeamSouth Africa
                       0.198270
                                  0.247507
                                             0.801 0.423093
                                  0.234687
## TeamSouth Korea
                       0.418820
                                             1.785 0.074327 .
## TeamSpain
                       1.008485
                                  0.214527
                                             4.701 2.59e-06 ***
## TeamSwitzerland
                                  0.282767
                                            -1.562 0.118223
                      -0.441761
## TeamUSA
                       0.425214
                                  0.224804
                                             1.891 0.058560
## TeamUruguay
                       0.606591
                                  0.216224
                                             2.805 0.005026 **
## PositionForward
                       1.215280
                                  0.082578
                                            14.717 < 2e-16 ***
## PositionGoalkeeper -3.922002
                                  1.003696
                                            -3.908 9.32e-05 ***
## PositionMidfielder 0.807259
                                  0.082679
                                             9.764 < 2e-16 ***
## Tackles.per.90.min -0.031253
                                  0.018116
                                            -1.725 0.084490 .
                                            -3.819 0.000134 ***
## Passes.per.90.min -0.006863
                                  0.001797
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 2182.6 on 594
                                      degrees of freedom
## Residual deviance: 1487.0 on 558
                                      degrees of freedom
##
  AIC: 2661.3
##
## Number of Fisher Scoring iterations: 6
```

Tackles and passes per 90 minutes have a negative relationship with shots per 90 minutes. Passes per 90 minutes is significant by the .0005 threshold and Tackles per 90 minutes may or may not be significant.

b)

```
## Amoah
## 0.1728024
```



Amoah has high leverage since he is a forward, plays for Gahana, and has a lot of tackles per 90 minutes. These three combinations are unusual predictor values and have the potential to affect the fit of the model.

$\mathbf{c})$

Amoah ## 0.02235704

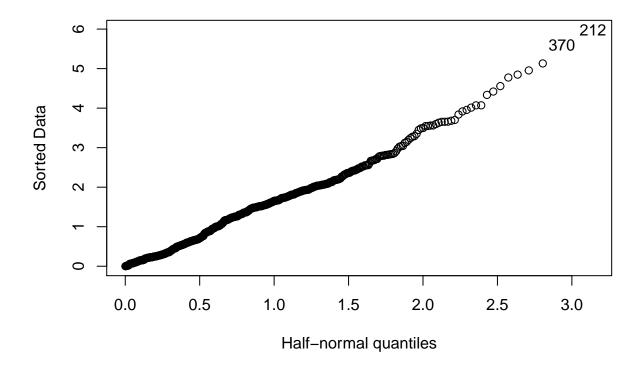
Amoah has high influence since he has the unusual predictor values mentioned above, but he also has zero shots, influencing the model when the weights would predict he would have a lot of shots.

\mathbf{d})

Gyan ## 0.1867534

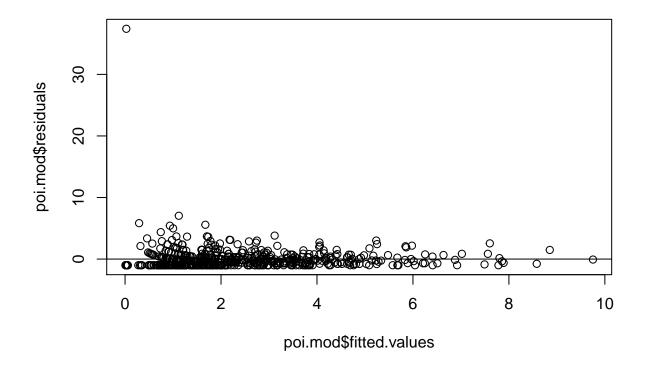
Gyan has the highest number of shots cross the entire dataset and a low number of passes per 90 minutes compared to his team.

e)

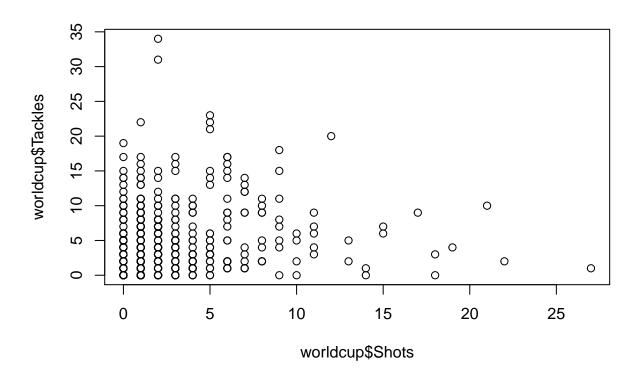


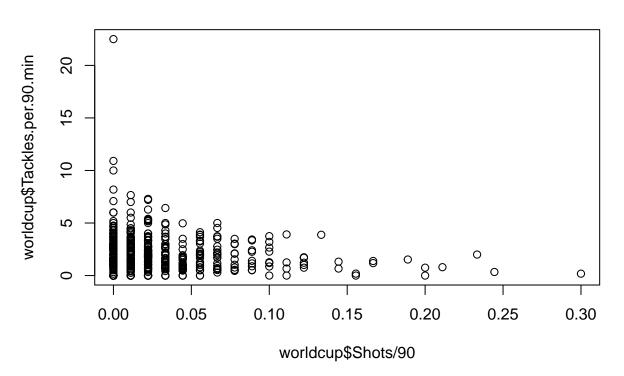
The player with the largest jacknife residual is 11, 2, 501, 27, 151, 1, 0, 0.179640718562874, 27.125748502994. As with the Cook's distance, Gyan has the highest number of shots cross the entire dataset and a low number of passes per 90 minutes compared to his team.

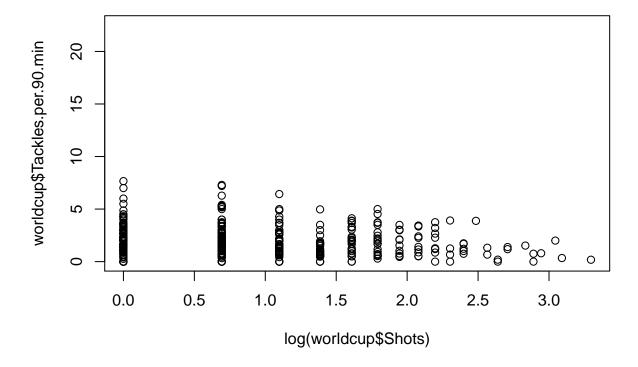
f)



The horizontal line is drawn at residuals of 0. Ideally the points should be normally distributed throughout the line. This plot indicates the residuals are larger on the lower quantiles, and there is an especially large residual for one point fitted at almost 0 shots.

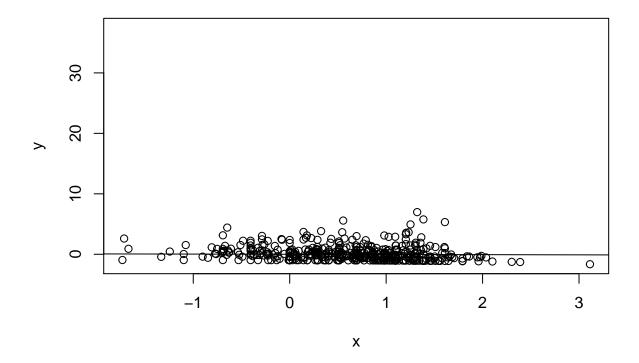




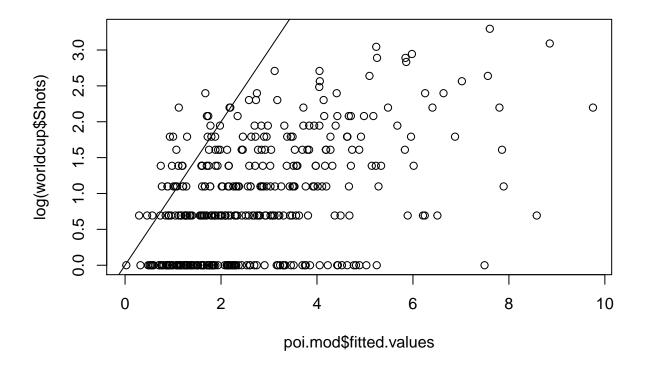


The plots appear to show that there is a slightly negative relationship between the linearized shots per game and the tackles per 90 minutes.

h)



f)



Our link function may not be the best for our data as the plot of fitted values versus the linearized response shows that the fitted values are much higher than the linearized response.