Problem Set 1

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GitHub repository link: https://github.com/tedheo10/homework1_STATS506

Problem 1 - Wine data

P1-a. import "wine.data" into a data.frame in R and give column names

```
winedata <- read.table("wine.data", sep = ",")
colnames(winedata) <- c("class", "alcohol", "acid", "ash", "alcalinity",
"magnesium", "phenols", "flavanoids", "nonflavanoid_phenols",
"proanthocyanins", "color_intensity", "hue", "protein", "proline")</pre>
```

P1-b. check the number of wines within each class

```
[class1 = 59, class2 = 71, class3 = 48]
```

[1] "correct as reported in wine.names"

P1-c-1. the correlation between alcohol content and color intensity

the correlation: 0.5463642

```
alcohol <- winedata$alcohol
color <- winedata$color_intensity
cor(alcohol, color)</pre>
```

[1] 0.5463642

P1-c-2. the highest and the lowest correlation

the highest : class1(0.4082913) the lowest : class2(0.2697891)

[1] 0.4082913 0.2697891 0.3503777

P1-c-3. the alcohol content of the wine with the highest color intensity the alcohol content with the hightest color intensity: **14.34**

```
length(which(color == max(color)))
```

[1] 1

```
alcohol_hcolor <- winedata$alcohol[winedata$color_intensity == max(color)]
alcohol_hcolor</pre>
```

[1] 14.34

P1-c-4. the percentage of the wines with a higher content of proanthocyanins compare to ash the percentage : **8.426966**%

```
proanthocyanins <- winedata$proanthocyanins
proan_higher <- winedata$proanthocyanins[winedata$proanthocyanins > winedata$alength(proan_higher) / length(proanthocyanins) * 100
```

[1] 8.426966

P1-d. table for the average value of each variable

the table : average_table

```
average_table <- matrix(0, nrow = 4, ncol = length(colnames(winedata))-1)
colnames(average_table) <- colnames(winedata[2:14])
rownames(average_table) <- c("overall", "class1", "class2", "class3")

cal_mat <- as.matrix(winedata)
n <- ncol(cal_mat)-1

ave_overall <- numeric(n)</pre>
```

```
ave_class1 <- numeric(n)
ave_class2 <- numeric(n)

for ( i in 1:n) {
    ave_overall[i] <- mean(cal_mat[,i+1])
    ave_class1[i] <- mean(cal_mat[cal_mat[,1] == 1, i+1])
    ave_class2[i] <- mean(cal_mat[cal_mat[,1] == 2, i+1])
    ave_class3[i] <- mean(cal_mat[cal_mat[,1] == 3, i+1])
}

average_table["overall",] <- ave_overall
average_table["class1",] <- ave_class1
average_table["class2",] <- ave_class2
average_table["class3",] <- ave_class3
average_table</pre>
```

```
acid
        alcohol
                            ash alcalinity magnesium phenols flavanoids
overall 13,00062 2,336348 2,366517
                                  19.49494 99.74157 2.295112 2.0292697
class1 13.74475 2.010678 2.455593 17.03729 106.33898 2.840169 2.9823729
class2 12.27873 1.932676 2.244789
                                  20.23803 94.54930 2.258873 2.0808451
class3 13.15375 3.333750 2.437083 21.41667 99.31250 1.678750 0.7814583
       nonflavanoid_phenols proanthocyanins color_intensity
                                                            hue protein
                                                5.058090 0.9574494 2.611685
overall
                 0.3618539
                               1.590899
class1
                 0.2900000
                                 1.899322
                                                5.528305 1.0620339 3.157797
class2
                 0.3636620
                                1.630282
                                               3.086620 1.0562817 2.785352
                                 1.153542 7.396250 0.6827083 1.683542
class3
                 0.4475000
        proline
overall 746.8933
class1 1115.7119
class2 519.5070
class3 629.8958
```

P1-e. t-test to examine whether the level of phenols differs across the three classes

We can reject the hypothesis that the level of phenols is the same across the three classes because all three p-values are less than 0.01. So we can conclude that the level of phenols differs across the three classes.

```
t-test p-value between class1 and class2 : 1.889e^{-11} t-test p-value between class1 and class3 : < 2.2e^{-16} t-test p-value between class2 and class3 : 1.622e^{-10}
```

```
phenols1 <- winedata$phenols[winedata$class == 1]
phenols2 <- winedata$phenols[winedata$class == 2]
phenols3 <- winedata$phenols[winedata$class == 3]

t.test(phenols1, phenols2)</pre>
```

```
data: phenols1 and phenols2
t = 7.4206, df = 119.14, p-value = 1.889e-11
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 0.4261870 0.7364055
sample estimates:
mean of x mean of y
 2.840169 2.258873
         t.test(phenols1, phenols3)
    Welch Two Sample t-test
data: phenols1 and phenols3
t = 17.12, df = 98.356, p-value < 2.2e-16
alternative hypothesis: true difference in means is not equal to {\tt 0}
95 percent confidence interval:
 1.026801 1.296038
sample estimates:
```

```
t.test(phenols2, phenols3)
```

```
data: phenols2 and phenols3
t = 7.0125, df = 116.91, p-value = 1.622e-10
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
    0.4162855 0.7439610
sample estimates:
mean of x mean of y
    2.258873    1.678750
```

Problem 2 - AskAManager.org Data

P2-a. import AskAManager.csv into a data.frame

```
salary <- read.csv("AskAManager.csv")</pre>
```

P2-b. simplify the variable names

mean of x mean of y 2.840169 1.678750

Welch Two Sample t-test

```
"state", "city", "experience", "experience_field", "education", "gender", "race")
```

P2-c. restrict the data to those paid in USD

the number of observations before: 28,062

the number of oberservations after the restriction: 23,374

```
length(salary$currency)
```

[1] 28062

```
length(salary$currency[salary$currency == "USD"])
```

[1] 23374

```
salary_res <- salary[salary$currency == "USD", ]
nrow(salary_res) == length(salary$currency[salary$currency == "USD"])</pre>
```

[1] TRUE

P2-d. Eliminate any rows for which their age, years of experience in their field, and years of experience total are impossible

the number of observation after the elimination: 23,116

```
age <- salary_res$age
field <- salary_res$experience_field
total <- salary_res$experience
age[!duplicated(age)]</pre>
```

- [1] "25–34" "45–54" "35–44" "18–24" "65 or over"
- [6] "55-64" "under 18"

field[!duplicated(field)]

```
[1] "5-7 years" "2 - 4 years" "21 - 30 years" "11 - 20 years" [5] "8 - 10 years" "1 year or less" "31 - 40 years" "41 years or more"
```

```
total[!duplicated(total)]
```

```
[1] "5-7 years" "2 - 4 years" "8 - 10 years" "21 - 30 years" [5] "11 - 20 years" "41 years or more" "31 - 40 years" "1 year or less"
```

```
age_kind <- c("25-34" = 16, "45-54" = 36, "35-44" = 26, "18-24" = 6, "65 or over" = 56, "55-64" = 46, "under <math>18" = 0)

experience_kind <- c("5-7 \text{ years}" = 5, "2 - 4 \text{ years}" = 2,
```

```
"8 - 10 years" = 8, "21 - 30 years" = 21,
                               "11 - 20 years" = 11, "41 years or more" = 41,
                               "31 - 40 years" = 31, "1 year or less" = 1 )
         age_trans <- age_kind[age]</pre>
         field_trans <- experience_kind[field]</pre>
         total_trans <- experience_kind[total]</pre>
         n_usd <- nrow(salary_res)</pre>
         memo <- logical(n_usd)</pre>
         for(i in 1:n_usd) {
           # if age < 18, eliminate the data
           # if age - 18 < field experience, eliminate the data
           # if age - 18 < total experience, eliminate the data
           # if total experience < field experience, eliminate the data
           if(age\_trans[i] == 0) {
                memo[i] = FALSE
           }
           else if(field_trans[i]>age_trans[i]) {
                memo[i] = FALSE
           }
           else if(total_trans[i]>age_trans[i]) {
                memo[i] = FALSE
           else if(field_trans[i]>total_trans[i]) {
                memo[i] = FALSE
           }
           else {
                memo[i] = TRUE
           }
         }
         #test whether age is under 18
         salary_year <- salary_res[memo, ]</pre>
         salary_year$age[!duplicated(salary_year$age)]
                              "35-44"
[1] "25-34"
                 "45-54"
                                            "18-24"
                                                         "65 or over"
[6] "55-64"
         #test example for whether their is reasonable with total experience
         experience_test <- salary_year$age[salary_year$experience</pre>
                                              == "41 years or more"]
         experience_test[!duplicated(experience_test)]
[1] "65 or over" "55-64"
         #test example for whether their is reasonable with field experience
         fieldexp_test <- salary_year$age[salary_year$experience_field</pre>
                                            == "41 years or more"]
         fieldexp_test[!duplicated(fieldexp_test)]
```

```
[1] "5-7 years" "2 - 4 years" "8 - 10 years" "1 year or less"
```

```
nrow(salary_year)
```

[1] 23116

P2-e. eliminate any rows with extremely low or high salaries.

The other monetary compensation is added to salalry in order to eliminate false slalrries.

The extreme high salary: 1,459,608 USD (mean + 2*standard deviation)

-> There are values on the right side of the distribution that differ from the mean by more than twice the standard deviation.

The extreme low salary: 1,000 USD

-> There's a very thick tail on the left side of the distribution.

The sample size: 23,044

```
income <- salary_year$salary
bonus <- salary_year$bonus
bonus[is.na(bonus)] <- 0
monetary_reward <- income + bonus
summary(monetary_reward)</pre>
```

```
Min. 1st Qu. Median Mean 3rd Qu. Max. 0 58000 81000 106240 120000 102000000
```

```
n_year <- length(monetary_reward)

mean_monetary <- mean(monetary_reward)

sd_monetary <- sd(monetary_reward)

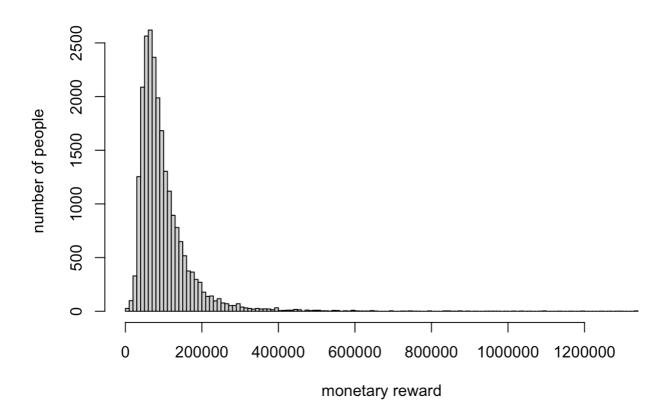
mean_monetary + 2*sd_monetary</pre>
```

[1] 1459608

```
mean_monetary - sd_monetary
```

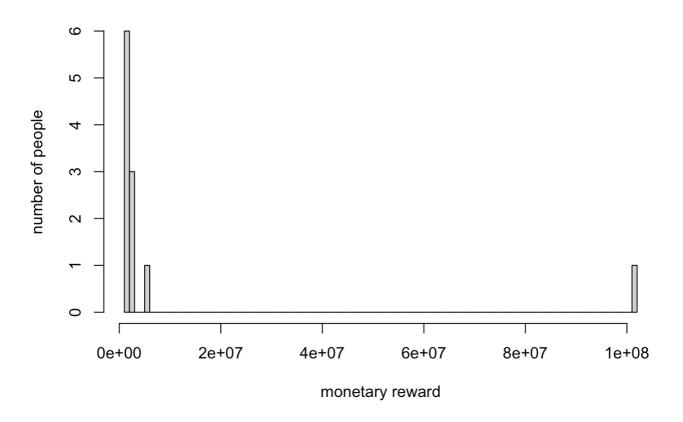
[1] -570443.5

Monetary reward between 1,000 and 1,459,608 USD



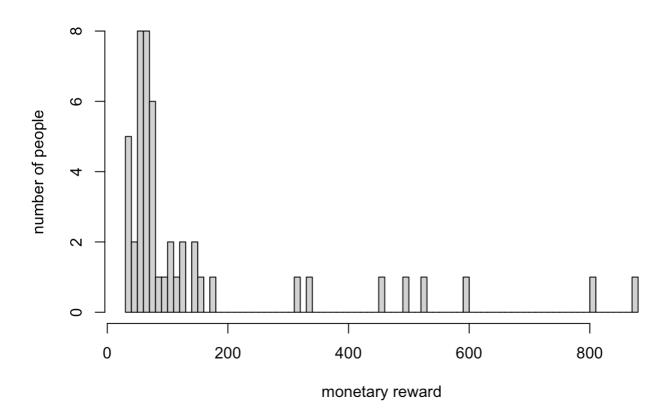
```
hist(monetary_reward[monetary_reward > 1459608], breaks = 100, main =
    "Monetary reward over 1,459,608 USD",
    xlab = "monetary reward", ylab = "number of people")
```

Monetary reward over 1,459,608 USD



```
hist(monetary_reward[monetary_reward < 1000 & monetary_reward > 0],
    breaks = 100, main = "Monetary reward less than 1,000 USD",
    xlab = "monetary reward", ylab = "number of people")
```

Monetary reward less than 1,000 USD



```
salary_year$monetary_reward <- monetary_reward
salary_monetary <- salary_year[monetary_reward <= 1459608 & monetary_reward >=
nrow(salary_monetary)
```

[1] 23044

Problem 3 - Palindromic Numbers

P3-a. function "isPalindromic" that check if a given positive integer is a palindromic

```
#' Palindromic of Integers
#'
#' Determine whether a positive integer is palindromic or not
#'
#' This function takes a positive integer x and returns a logical value
#' whether the integer is a palindromic number or not and return reversed #'
#' number.
#'
#' @param x a positive integer
#' @param na.rm logical, should NA's be removed? Default is FALSE
#' @return list of a logical value and a numeric value
isPalindromic <- function(x, na.rm = FALSE) {
   if(!is.numeric(x)) {
        # this code is from STATS 506 class note
        warning("x must be a positive integer, attemting to convert")</pre>
```

```
suppressWarnings(x <- as.numeric(x))</pre>
    if(all(is.na(x))) {
      stop(
    "x must be a positive integer or convertible to a positive integer")
    }
  if(length(x) == 0) {
    # this code is from STATS 506 class note
    stop("x must have strictly positive length")
  if(!is.logical(na.rm)) {
    # this code is from STATS 506 class note
    warning("na.rm must be logical")
  if(x \ll 0)
    stop(
  "x must be a positive integer or convertible to a positive integer")
  if(x != round(x)) {
    stop(
  "x must be a positive integer or convertible to a positive integer")
  }
  y <- as.character(x)</pre>
  z <- as.numeric(unlist(strsplit(y, "")))</pre>
  k <- length(z)</pre>
  check_palindromic <- logical(k)</pre>
  reverse <- numeric(k)</pre>
  for(i in 1:k) {
    if(z[i] == z[k+1-i]) {
     check_palindromic[i] <- TRUE</pre>
    } else {
      check_palindromic[i] <- FALSE</pre>
    reverse[i] \leftarrow z[k+1-i]
  reverse_return <- as.numeric(paste(reverse, collapse = ""))</pre>
  if(all(check_palindromic == TRUE)) {
    return(list(isPalindromic = TRUE, reversed = reverse_return))
  }
  else {
    return(list(isPalindromic = FALSE, reversed = reverse_return))
  }
}
isPalindromic(1100) # check the "isPalindromic()" function
```

\$isPalindromic

[1] FALSE

\$reversed

[1] 11

P3-b. create a nextPalindrome function that finds the next palindromic number strictly greater than the input

```
#' Next Palindrome
#' Find the next palindromic number strictly greater than the input
#'
#' This function takes a positive integer x and check from x+1 to the next #'
#' and return the next palindromic number.
#'
#' @param x a positive integer
#' @param na.rm logical, should NA's be removed? Default is FALSE
#' @return a numeric value
nextPalindrome <- function(x, na.rm = FALSE) {</pre>
  if(!is.numeric(x)) {
    # this code is from STATS 506 class note
   warning("x must be a positive integer, attemting to convert")
    suppressWarnings(x <- as.numeric(x))</pre>
    if(all(is.na(x))) {
      stop(
     "x must be a positive integer or convertible to a positive integer")
   }
  }
  if(length(x) == 0) {
    # this code is from STATS 506 class note
    stop("x must have strictly positive length")
  if(!is.logical(na.rm)) {
   # this code is from STATS 506 class note
   warning("na.rm must be logical")
  }
  if(x \ll 0)
   stop(
     "x must be a positive integer or convertible to a positive integer")
  if(x != round(x)) {
    stop(
    "x must be a positive integer or convertible to a positive integer")
  }
  y <- as.character(x+1)
  z <- as.numeric(unlist(strsplit(y, "")))</pre>
  k <- length(z)</pre>
  check <- logical(k)</pre>
  next_palindrome <- numeric(k)</pre>
  while(!all(check == TRUE)) {
    for(i in 1:k) {
      if(z[i] == z[k+1-i]) {
        check[i] <- TRUE</pre>
      } else {
        check[i] <- FALSE</pre>
      }
```

```
next_palindrome[i] <- z[i]</pre>
               }
               y <- as.character(as.numeric(y)+1)</pre>
               z <- as.numeric(unlist(strsplit(y, "")))</pre>
               k <- length(z)</pre>
            next_palindrome <- as.numeric(paste(next_palindrome, collapse = ""))</pre>
            return(nextPalindrome = next_palindrome)
          }
          nextPalindrome(1523) # check the "nextPalindrome()" function
[1] 1551
P3-c. Use above functions to find the next palindrome for each of the following: (391, 9928,
19272719, 109, 2)
i. 391 : 393
ii. 9928 : 9999
iii. 19272719 : 19277291
iv. 109 : 111
v. 2 : 3
          nextPalindrome(391)
[1] 393
          nextPalindrome(9928)
[1] 9999
          nextPalindrome(19272719)
[1] 19277291
         nextPalindrome(109)
[1] 111
         nextPalindrome(2)
```

[1] 3