

# NON-LOCAL KALMAN: A RECURSIVE VIDEO DENOISING ALGORITHM

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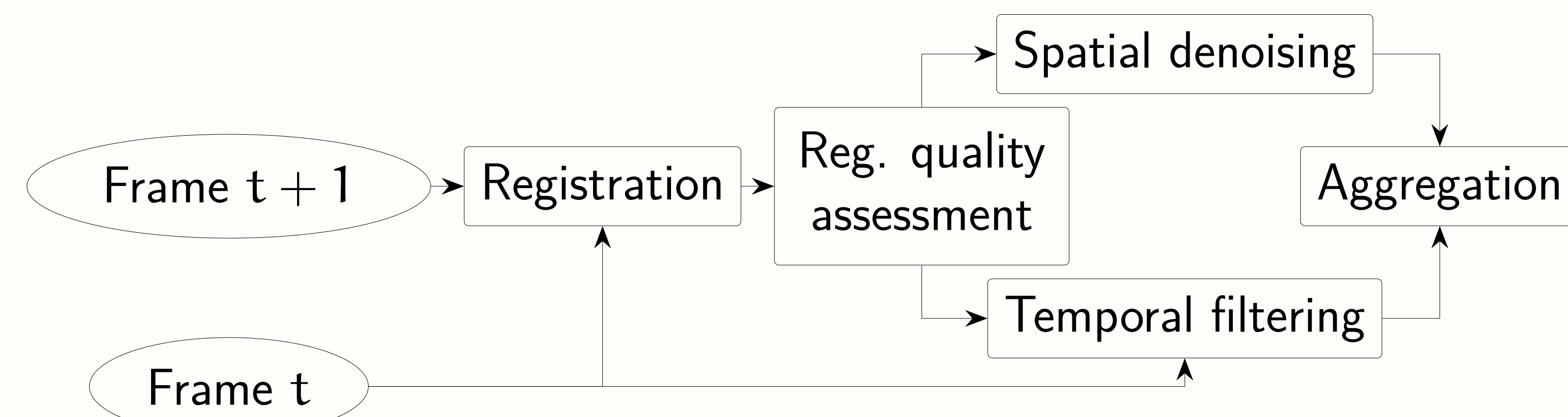
## Contributions

We propose a recursive patch-based video denoising method with the following advantages:

- Particularly suited for real-time processing
- Produces temporally consistent videos, which are much better visually
- Competitive with current state-of-the-art denoising methods

## Non-local Kalman

Pipeline of the recursive video denoising algorithm:



### Registration and registration quality assessment

The registration is used to track patches from one frame to the next:

- Assumption: patches move with the optical flow of their center
- We use TV-L1 [1] on a downscaled version of the images to limit problems due to the noise

The detection of occlusion and mismatch can be done using a statistical framework:

- When a patch is correctly tracked by the optical flow the distance between the two instances of the patches follows a  $\chi^2$  distribution.
- The number of false alarm frame work based on *a contrario* gives an optimum threshold on the distance to detect occlusions and mismatch

### Spatial denoising: creation of groups of trajectories

Use NL-Bayes [2] to create groups of patches and denoise them:

- Search for local nearest neighbors  $q_i$  for a given query patch  $q$ , these patches constitute the group
- Use a MAP estimate:  $\hat{p} = \mu + C(C + \sigma^2 I)^{-1}(q - \mu)$  where  $\hat{\mu} = \frac{1}{N} \sum_{i=1}^N q_i$  and  $\hat{C} = \frac{1}{N} \sum_{i=1}^N q_i q_i^T - \sigma^2 I$ ,

### Temporal filtering: Kalman filtering along patches trajectories

For the patches in a group we assume the following model:

$$p_{t+1,i} = p_{t,i} + w_{t,i} \text{ with } w_{t,i} \sim \mathcal{N}(0, C_t)$$

$$q_{t,i} = p_{t,i} + n_{t,i} \text{ with } n_{t,i} \sim \mathcal{N}(0, \sigma^2 I).$$

where  $q_i$ s are the observation (noisy patch) and the  $p_i$ s what we tried to estimate. We apply Kalman filter [3] to estimate the  $p_{t,i}$ s.

## Remarks

The study of the algorithm showed some limits on how video denoising algorithms are studied:

- Optical flow, while being suited to video processing, is difficult to use when the video has been degraded:
- PSNR are not a good fit to measure the quality of video denoising. The eye prefers a temporally consistent and it's not a problem if there's slight deformation.

## References

- [1] Zach et al. "A duality based approach for realtime TV-L 1 optical flow". *Joint Pattern Recognition Symposium*, 2007.
- [2] Lebrun et al. "A nonlocal bayesian image denoising algorithm". *SIAM*, 2013.
- [3] Kalman "A new approach to linear filtering and prediction problems." *Journal of basic Engineering* 82, 1960
- [4] Dabov et al. "Video denoising by sparse 3D transform-domain collaborative filtering". *EUSIPCO*, 2007.
- [5] Maggioni et al. "Video denoising by sparse 3D transform-domain collaborative filtering". *IEEE TIP*, 2012.

## Experiments

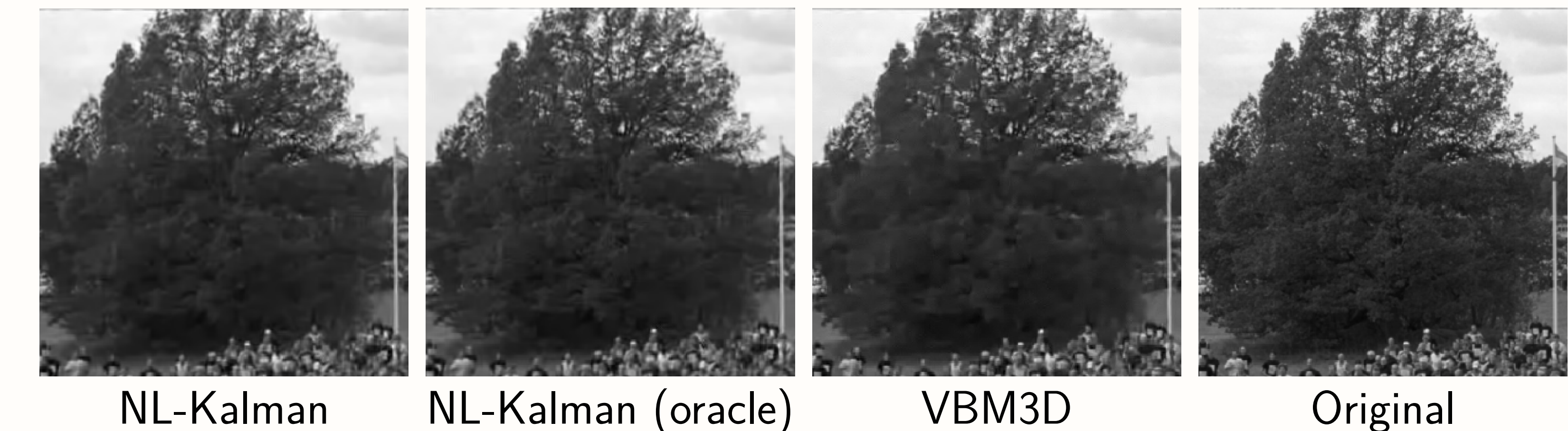
### Quantitative evaluation

Our algorithm is compared against VBM3D [4] and VBM4D [5], two state-of-the-art algorithms:

$\sigma$ Method	Bus	Foreman	Pedestrian_area	Crowd_run	Touchdown_pass	Station2	Average
10 VBM3D	33.32/.7824	<b>37.40</b> /.6681	<b>40.78</b> /.6577	35.62/.8017	39.08/.6103	38.92/.7266	37.52/.7078
VBM4D	<b>33.39</b> /.8237	37.39/.6871	40.56/.7463	<b>35.69</b> /.8457	<b>39.60</b> /.6752	<b>39.93</b> /.7746	<b>37.76</b> /.7588
NL-Kalman	33.34/. <b>8502</b>	36.16/.6782	38.67/.7420	34.29/.8383	38.82/. <b>6940</b>	39.91/. <b>7916</b>	36.86/. <b>7657</b>
NL-Kalman (oracle)	33.87/.8713	36.93/.7230	39.23/.7592	34.64/.8514	39.58/.7433	40.50/.8059	37.46/.7923
20 VBM3D	29.57/.6064	34.60/.5763	<b>36.93</b> /.5579	<b>32.22</b> /.7122	36.09/.4703	35.45/.5689	34.14/.5820
VBM4D	29.55/.6856	<b>34.61</b> /. <b>6073</b>	36.75/. <b>6468</b>	32.07/.7439	<b>36.41</b> /.4795	36.23/.6395	<b>34.27</b> /.6338
NL-Kalman	<b>29.58</b> /. <b>7291</b>	33.19/.5844	35.61/.6444	30.89/. <b>7478</b>	35.91/. <b>5181</b>	<b>36.81</b> /. <b>6868</b>	33.66/. <b>6518</b>
NL-Kalman (oracle)	30.43/.7752	34.18/.6301	36.45/.6738	31.44/.7746	36.99/.6135	37.46/.7116	34.49/.6965
30 VBM3D	<b>27.59</b> /.4995	32.77/.5224	34.44/.4869	<b>30.14</b> /.6394	34.55/.3906	33.36/.4536	32.14/.4987
VBM4D	27.53/.5988	<b>32.91</b> /. <b>5612</b>	<b>34.45</b> /. <b>5745</b>	29.95/.6704	<b>34.76</b> /.3801	34.14/.5420	<b>32.29</b> /.5545
NL-Kalman	27.30/. <b>6327</b>	31.27/.5335	33.27/.5680	28.64/. <b>6708</b>	33.91/. <b>4034</b>	<b>34.73</b> /. <b>5986</b>	31.52/. <b>5678</b>
NL-Kalman (oracle)	28.48/.6993	32.50/.5802	34.43/.6102	29.44/.7078	35.20/.5186	35.46/.6338	32.59/.6250

### Qualitative evaluation

Detail of the Crowd\_run sequence (noise standard deviation  $\sigma = 30$ ):



Detail of the Pedestrian\_area sequence (noise standard deviation  $\sigma = 30$ ):

