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In [1]: # 1 Bisection
a = float(input("Enter a: "))
b = float(input("Enter b: "))
e = float(input("Enter the tolerance (e): "))

def f(num):
    return (num**4) + 3*(num**2) + num - 10

k = 1
c = (a + b) / 2

print("{:<10} {:<10} {:<10} {:<10} {:<10} {:<10}".format("Iteration", "a", "f(a)", "b", "f(b)",
print("-" * 60))

while True:
    fc = f(c)

    print("{:<10} {:<10.5f} {:<10.5f} {:<10.5f} {:<10.5f} {:<10.5f} {:<10.5f}".format(
        k, a, f(a), b, f(b), c, fc))

    if f(a) * f(c) < 0:
        b = c
    else:
        a = c

    c_prev = c
    c = (a + b) / 2

    if abs(c - c_prev) < e:
        break

    k += 1

print("\nNumber of iterations are: ", k)
print("Root of the equation is: ", c)

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Iteration	a	f(a)	b	f(b)	c	
1	1.00000	-5.00000	2.00000	20.00000	1.50000	3.31250
2	1.00000	-5.00000	1.50000	3.31250	1.25000	-1.62109
3	1.25000	-1.62109	1.50000	3.31250	1.37500	0.62134
4	1.25000	-1.62109	1.37500	0.62134	1.31250	-0.55199
5	1.31250	-0.55199	1.37500	0.62134	1.34375	0.02116
6	1.31250	-0.55199	1.34375	0.02116	1.32812	-0.26873
7	1.32812	-0.26873	1.34375	0.02116	1.33594	-0.12462
8	1.33594	-0.12462	1.34375	0.02116	1.33984	-0.05194
9	1.33984	-0.05194	1.34375	0.02116	1.34180	-0.01544
10	1.34180	-0.01544	1.34375	0.02116	1.34277	0.00285
11	1.34180	-0.01544	1.34277	0.00285	1.34229	-0.00630
12	1.34229	-0.00630	1.34277	0.00285	1.34253	-0.00172
13	1.34253	-0.00172	1.34277	0.00285	1.34265	0.00056
14	1.34253	-0.00172	1.34265	0.00056	1.34259	-0.00058
15	1.34259	-0.00058	1.34265	0.00056	1.34262	-0.00001
16	1.34262	-0.00001	1.34265	0.00056	1.34264	0.00028

Number of iterations are: 16

Root of the equation is: 1.3426284790039062

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In [3]: #2 False Position
a = float(input("Enter a: "))
b = float(input("Enter b: "))
e = float(input("Enter the tolerance (e): "))

def f(num):
    return (num**3) - num - 4
# (a * func(b) - b * func(a)) / (func(b) - func(a))
k = 1
c = (a* f(b) - b * f(a))/(f(b)-f(a))
while True:
    print("-" * 50)
    fc = f(c)
    formatted_string = "a : {} f(a) : {} b : {} f(b): {} c: {} fc: {}".format(a, f(a), b, f(b), c, fc)
    print(formatted_string)

    if f(a) * f(c) < 0:
        b = c
    else:
        a = c

    c_prev = c
    c = (a* f(b) - b * f(a))/(f(b)-f(a))

    if abs(c - c_prev) < e:
        break

    k += 1

print("Number of iterations are: ", k)
print("Root of the equation is: ", c)

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-----
a : 1.0 f(a) : -4.0 b : 2.0 f(b): 2.0 c: 1.6666666666666667 fc: -1.0370370370370363
-----
a : 1.6666666666666667 f(a) : -1.0370370370370363 b : 2.0 f(b): 2.0 c: 1.780487804878049 fc: -0.13609785116292317
-----
a : 1.780487804878049 f(a) : -0.13609785116292317 b : 2.0 f(b): 2.0 c: 1.7944736520357012 fc: -0.016025004208394478
-----
a : 1.7944736520357012 f(a) : -0.016025004208394478 b : 2.0 f(b): 2.0 c: 1.7961073423838807 fc: -0.0018622083672488188
-----
a : 1.7961073423838807 f(a) : -0.0018622083672488188 b : 2.0 f(b): 2.0 c: 1.7962970110890724 fc: -0.00021606859402067968
-----
a : 1.7962970110890724 f(a) : -0.00021606859402067968 b : 2.0 f(b): 2.0 c: 1.796319015621034 fc: -2.5065572228477606e-05
Number of iterations are: 6
Root of the equation is: 1.7963215682792548

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In [19]: #ques 3 Secant Method
x0 = 2.0
x1 = 3.0
e = 0.001

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def f(x):
    # return x**3 - 4
    return x**3-4*x-9

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k = 1
while True:
    print("-" * 50)
    f_x0 = f(x0)
    f_x1 = f(x1)

    x2 = x1 - f_x1 * (x1 - x0) / (f_x1 - f_x0)

    formatted_string = "x0 : {} f(x0) : {} x1 : {} f(x1): {} x2: {} f(x2): {}".format(x0, f_x0, x1, f_x1, x2, f_x2)
    print(formatted_string)

    if abs(x2 - x1) < e:
        break

    x0 = x1
    x1 = x2

    k += 1

print("Number of iterations are: ", k)
print("Root of the equation is: ", x2)

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x0 : 2.0 f(x0) : -9.0 x1 : 3.0 f(x1): 6.0 x2: 2.6 f(x2): -1.8239999999999998
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x0 : 3.0 f(x0) : 6.0 x1 : 2.6 f(x1): -1.8239999999999998 x2: 2.6932515337423313 f(x2): -0.23722651080748847
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x0 : 2.6 f(x0) : -1.8239999999999998 x1 : 2.6932515337423313 f(x1): -0.23722651080748847 x2: 2.7071928657142923 f(x2): 0.011955954723166684
-----

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x0 : 2.6932515337423313 f(x0) : -0.23722651080748847 x1 : 2.7071928657142923 f(x1): 0.011955954723166684 x2: 2.7065239505340752 f(x2): -7.197464652008989e-05
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Number of iterations are: 4

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Root of the equation is: 2.7065239505340752

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In [5]: *#ques 4 Newton Raphson Method*

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x_n = 3.5
tolerance = 0.000001

def f(x):
    return x**2 - 12

def f_prime(x):

k = 0

while True:
    print(f"Iteration {k}: x_n = {x_n}, f(x_n) = {f(x_n)}")

    x_next = x_n - f(x_n) / f_prime(x_n)

    if abs(x_next - x_n) < tolerance:
        break

    x_n = x_next
    k += 1

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print("Approximate value of  $\sqrt{12}$ :", round(x_next, 5))
print("Number of iterations:", k)
```

Iteration 0:  $x_n = 3.5$ ,  $f(x_n) = 0.25$

Iteration 1:  $x_n = 3.4642857142857144$ ,  $f(x_n) = 0.001275510204083119$

Iteration 2:  $x_n = 3.464101620029455$ ,  $f(x_n) = 3.389069647141696e-08$

Approximate value of  $\sqrt{12}$ : 3.4641

Number of iterations: 2

In [5]: #5 Birge Vieta Method

```
import pandas as pd

def bCal(data,guess: float)->None:
    val = data["ai"][len(data["bi"])] + (data["bi"][-1] * guess)
    data["bi"].append(val)
    return None

def cCal(data,guess: float)->None:
    val = data["bi"][len(data["ci"])] + (data["ci"][-1] * guess)
    data["ci"].append(val)
    return None

coefficient = str(input("Enter the coefficients (eg : -2,3,-121) :"))
guess = float(input("Enter the initial guess :"))
listCoefficient = [float(val) for val in coefficient.split(",")]
outputList = []
k = 0
while True:
    data = {
        "ai":[],
        "bi":[],
        "ci":[],
    }

    data["ai"] = listCoefficient
    data["bi"].append(listCoefficient[0])
    data["ci"].append(listCoefficient[0])

    while True:
        bCal(data,guess)
        cCal(data,guess)
        if len(data["ai"]) == len(data["bi"]) == len(data["ci"]):
            guess = guess - (data["bi"][-1]/data["ci"][-2])
            break
    outputList.append(data)
    k+=1
    if k > 3:
        break

print(f"\nNumber of Iteration {k}\nThe BirgeVieta Table:")
for i in outputList:
    print(pd.DataFrame(i,range(1,len(i["ai"])+1)))
    print()
```

Number of Iteration 4

The BirgeVieta Table:

	ai	bi	ci
1	1.0	1.000	1.00
2	-1.0	-0.500	0.00
3	-1.0	-1.250	-1.25
4	1.0	0.375	-0.25

	ai	bi	ci
1	1.0	1.000	1.000
2	-1.0	-0.200	0.600
3	-1.0	-1.160	-0.680
4	1.0	0.072	-0.472

	ai	bi	ci
1	1.0	1.000000	1.000000
2	-1.0	-0.094118	0.811765
3	-1.0	-1.085260	-0.349896
4	1.0	0.016883	-0.300082

	ai	bi	ci
1	1.0	1.000000	1.000000
2	-1.0	-0.045867	0.908265
3	-1.0	-1.043764	-0.177158
4	1.0	0.004111	-0.164921