

Assignment 1

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Abstract—This document contains the solution for Ex. 3.37 of Discrete-Time Signal Processing by Oppenheim and Wilsky.

Problem 1. Consider a sequence $x[n]$ for which z -transform is

$$X(z) = \frac{\frac{1}{3}}{1 - \frac{1}{2}z^{-1}} + \frac{\frac{1}{4}}{1 + \frac{1}{3}z^{-1}} \quad (0.1)$$

and for which region of convergence includes the unit circle. Determine $x[0]$ using initial-value theorem.

Solution: The initial value theorem of Z-transform states that:

$$x(n) \xleftrightarrow{Z} X(z) \quad (0.2)$$

Where, $x(n)$ is casual sequence. Then,

$$x(0) = \lim_{n \rightarrow 0} x(n) = \lim_{z \rightarrow \infty} X(z) \quad (0.3)$$

So,

$$x(0) = \lim_{z \rightarrow \infty} X(z) \quad (0.4)$$

$$= \lim_{z \rightarrow \infty} \frac{\frac{1}{3}}{1 - \frac{1}{2}z^{-1}} + \frac{\frac{1}{4}}{1 + \frac{1}{3}z^{-1}} \quad (0.5)$$

$$= \frac{1}{3} + \frac{1}{4} = \frac{7}{12} \quad (0.6)$$