

CLASS-9
CHAPTER-10
CIRCLES

Exercise 10.4

1. If two equal chords of a circle intersect prove that the parts of one chord are separately equal to the parts of the other chord
2. If non-parallel sides of a trapezium are equal. prove that it is cyclic
3. If PQ and R are the mid-points of the sides BC , CA and AB of a triangle and AD is the perpendicular from A on BC , prove that PQR and D are concyclic
4. $ABCD$ is a parallelogram. A circle through A, B is so drawn that it intersects AD at P and BC at Q . prove that P, Q, R and D are concyclic.
5. Prove that angle bisector of any angle of a triangle and perpendicular bisector of the opposite side if intersect, they will intersect on the circumcircle of the triangle.
6. If two chords AB and CD of a circle $AYDZBWCX$ intersect at right angles see Fig 1) , prove that $\text{arc } CXA + \text{arc } DZB = \text{arc } AYD + \text{arc } AYD + \text{arc } BWC = \text{semi-circle}$
7. If ABC is an equilateral triangle inscribed in a circle and P be any point on the minor arc BC which does not coincide with B or C , prove that PA is angle bisector of $\angle BPC$
8. In Fig-2, AB and CD are two chords of a circle intersecting each other at point E prove that $\angle AEC = \frac{1}{2} \times (\text{Angle subtended by arc } CXA \text{ at centre} + \text{angle subtended by arc } DYB \text{ at the centre})$.
9. If bisectors of opposite angles of a cyclic quadrilateral $ABCD$ intersect the circle, circumscribing it at the points P and Q , prove that PQ is a diameter of the circle,

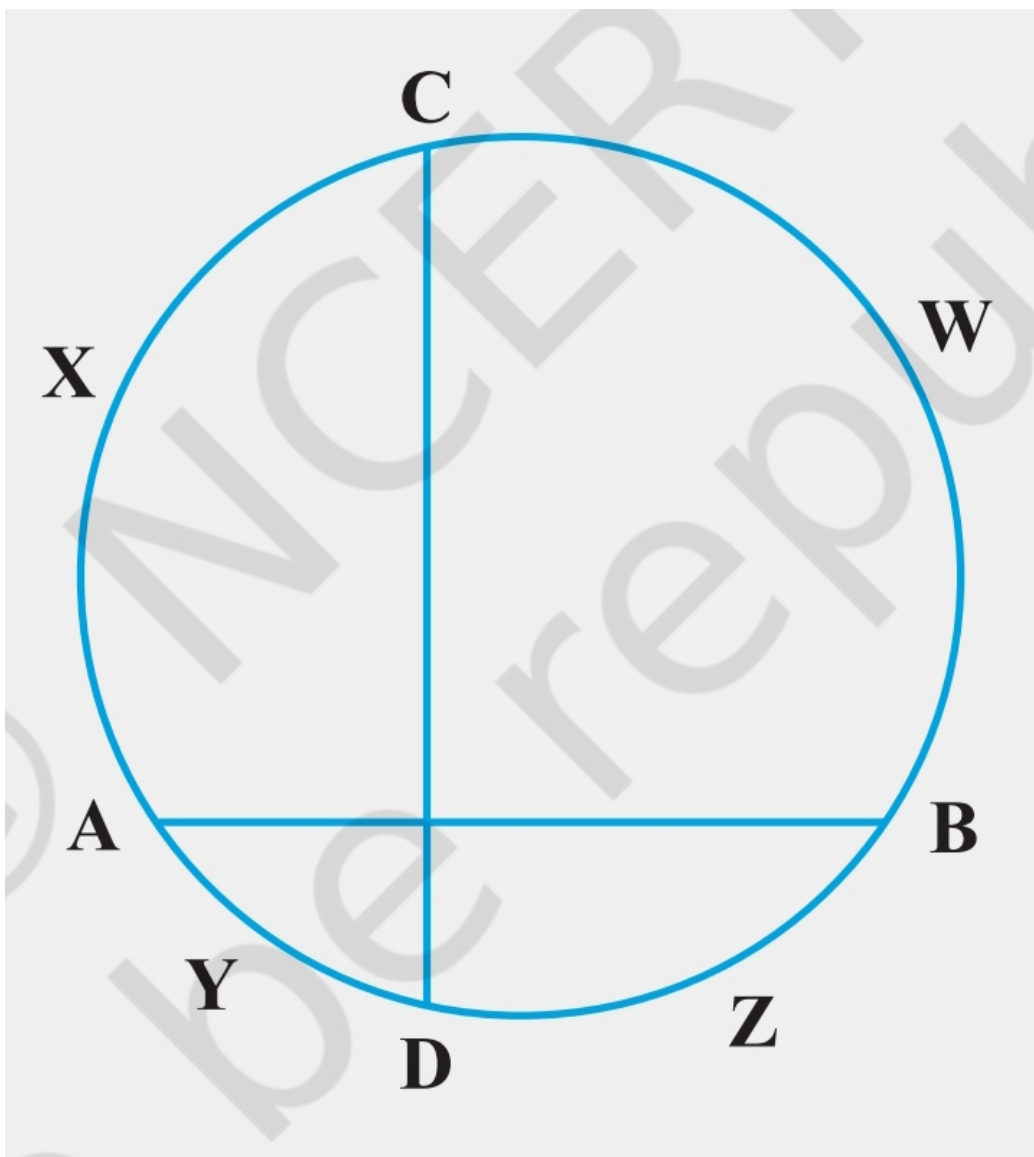


Figure 1

10. A circle has radius $\sqrt{2}$ cm it is divided into two segments by a chord of length 2cm . prove that the angle subtended by the chord at a point in major segment is 45° .

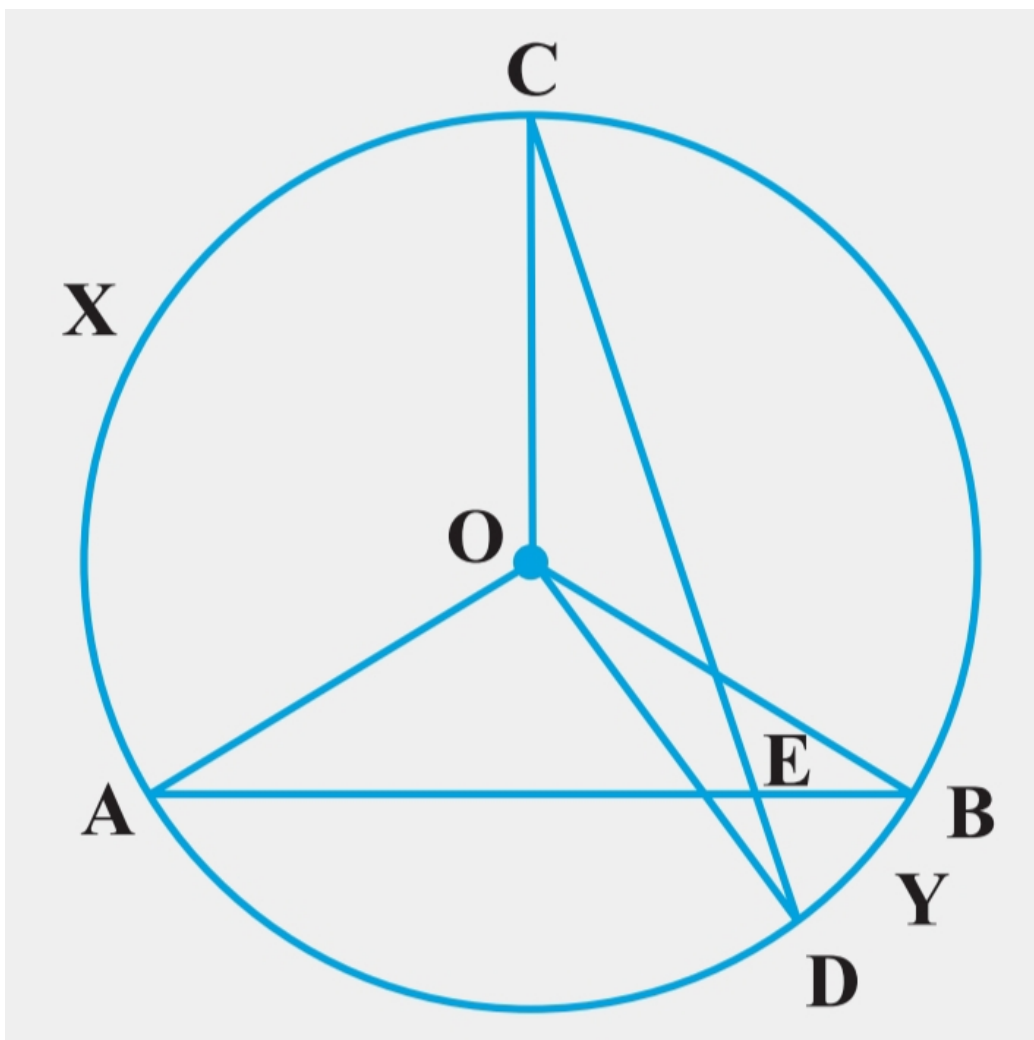


Figure 2

11. Two equal chords AB and CD of a circle when produced intersect at a point P prove that $PB = PD$
12. AB and AC are two chords of a circle of radius r such that $AB = 2AC$. If P and q are the distances of AB and AC from the centre, prove that $4q^2 = p^2 + 3r^2$

13. In Fig 3, O is the centre of the circle, $\angle BCO = 30^\circ$. Find x and y^2

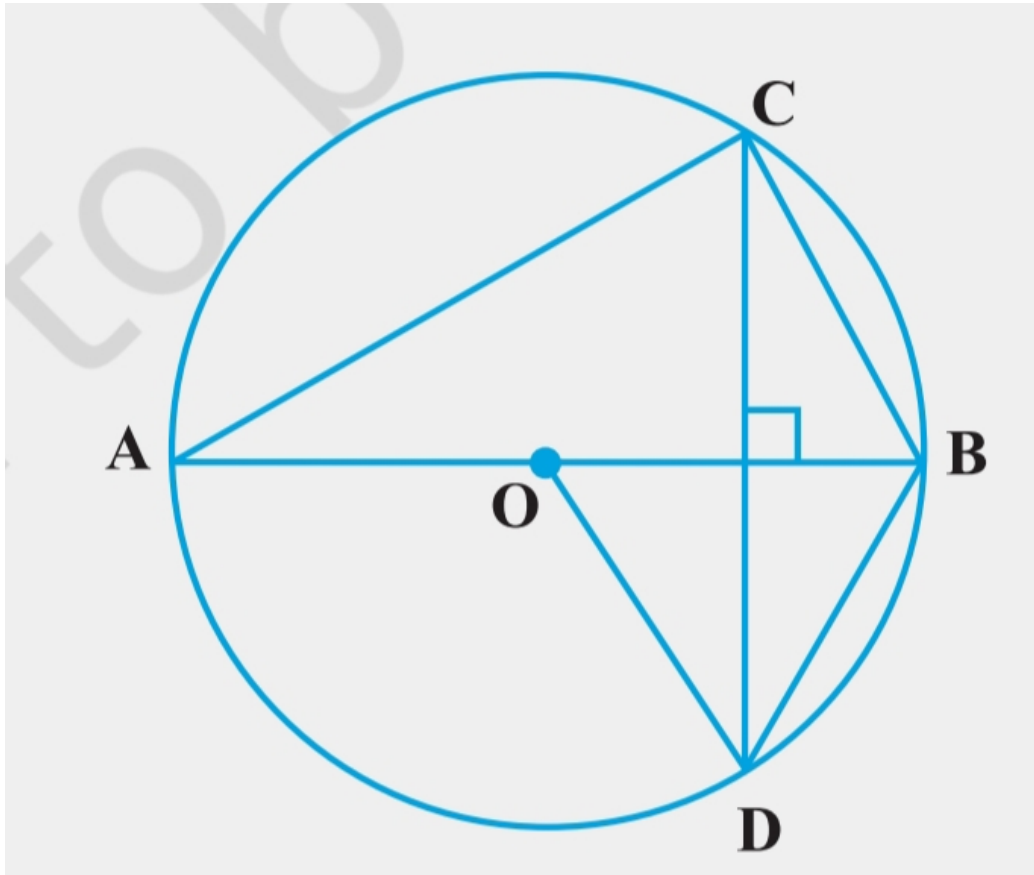


Figure 3

14. In fig 4, O is the centre of the circle $BD = OD$ and $CD \perp AB$. Find $\angle CAB$

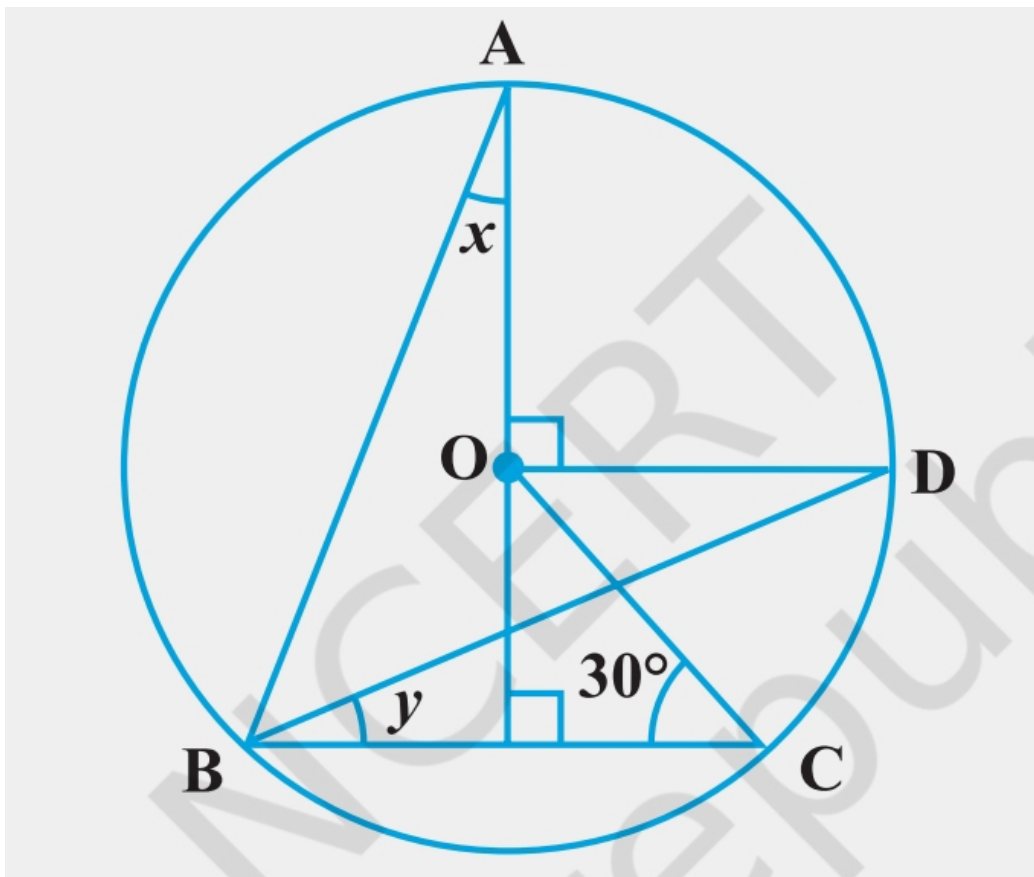


Figure 4