

CLASS-11  
CHAPTER-11  
CONIC SECTIONS

## EXERCISE - 11.1

In each of the following exercises 1 to 5, find the equation of the circle with

1. centre  $(0, 2)$  and radius 2
2. centre  $(-2, 3)$  and radius 4
3. centre  $(\frac{1}{2}, \frac{1}{4})$  and radius  $\frac{1}{12}$
4. centre  $(1, 1)$  and radius  $\sqrt{2}$
5. centre  $(-a, -b)$  and radius  $\sqrt{a^2 - b^2}$

In each of the following exercises 6 to 9; find the centre and radius of the circles.

6.  $(x + 5)^2 + (y - 3)^2 = 36$
7.  $x^2 + y^2 - 4x - 8y - 45 = 0$
8.  $x^2 + y^2 - 8x + 10y - 12 = 0$
9.  $2x^2 + 2y^2 - x = 0$
10. Find the equation of the circle passing through the points  $(4, 1)$  and  $(6, 5)$  and whose centre is on the line  $4x + y = 16$ .
11. Find the equation of the circle passing through the points  $(2, 3)$  and  $(-1, 1)$  and whose centre is on the line  $x - 3y - 11 = 0$ .
12. Find the equation of the circle with radius 5 whose centre lies on  $x$ -axis and passes through the point  $(2, 3)$ .
13. Find the equation of the circle passing through  $(0, 0)$  and making intercepts  $a$  and  $b$  on the coordinate axes.
14. Find the equation of a circle with centre  $(2, 2)$  and passes through the point  $(4, 5)$ .
15. Does the point  $(-2.5, 3.5)$  lie inside, outside or on the circle  $x^2 + y^2 = 25$ ?

## EXERCISE - 11.2

In each of the following exercises 1 to 6, find the coordinates of the focus, axis of the parabola, the equation of the directrix and the length of the latus rectum.

1.  $y^2 = 12x$

2.  $x^2 = 6y$

3.  $y^2 = 8x$

4.  $x^2 = -16y$

5.  $y^2 = 10x$

6.  $x^2 = -9y$

In each of the exercises 7 to 12, find the equation of the parabola that satisfies the given conditions.

7. Focus  $(6, 0)$ ; directrix  $x = -6$

8. Focus  $(0, -3)$ ; directrix  $y = 3$

9. vertex  $(0, 0)$ ; focus  $(3, 0)$

10. vertex  $(0, 0)$ ; focus  $(-2, 0)$

11. vertex  $(0, 0)$  passing through  $(5, 2)$  and symmetric with respect to  $y$ -axis.

## EXERCISE - 11.3

In each of the exercises 1 to 9, find the coordinates of the foci, the vertices, the coordinates of the foci, the vertices, the length of major axis, the minor axis, the eccentricity and the length of the latus rectum of the ellipse.

1.  $\frac{x^2}{36} + \frac{y^2}{16} = 1$

2.  $\frac{x^2}{4} + \frac{y^2}{25} = 1$

3.  $\frac{x^2}{16} + \frac{y^2}{9} = 1$
4.  $\frac{x^2}{25} + \frac{y^2}{100} = 1$
5.  $\frac{x^2}{49} + \frac{y^2}{36} = 1$
6.  $\frac{x^2}{100} + \frac{y^2}{400} = 1$
7.  $36x^2 + 4y^2 = 144$
8.  $16x^2 + y^2 = 16$
9.  $4x^2 + 9y^2 = 36$

In each of the following exercises 10 to 20, find the equation for the ellipse that satisfies the given conditions;

10. vertices  $(\pm 5, 0)$ , foci  $(\pm 4, 0)$
11. vertices  $(\pm 13)$  foci  $(\pm 5)$
12. vertices  $(\pm 6, 0)$  foci  $(\pm 4, 0)$
13. Ends of major axis  $(\pm 3, 0)$ , ends of minor axis  $(\pm 2)$
14. Ends of major axis  $(0, \pm\sqrt{5})$  , ends of minor axis  $(\pm 1, 0)$
15. Length of major axis 26, foci  $(\pm 5, 0)$
16. Length of minor axis 16, foci  $(\pm, 6)$
17. Foci  $(\pm 3, 0)$ ,  $a=4$
18.  $b=3$ ,  $c=4$ , centre at the origin; foci on the  $x$  axis.
19. centre at  $(0, 0)$ , major axis on the  $y$ -axis and passes through the points  $(3, 2)$  and  $(1, 6)$ .
20. major axis on the  $x$ -axis and passes through the points  $(4, 3)$  and  $(6, 2)$ .

## EXERCISE - 11.4

In each of the exercises 1 to 6, find the coordinates of the foci and the vertices, the eccentricity and the length of the latus rectum of the hyperbolas.

1.  $\frac{x^2}{16} - \frac{y^2}{9} = 1$
2.  $\frac{y^2}{9} - \frac{x^2}{27} = 1$
3.  $9y^2 - 4x^2 = 36$
4.  $16x^2 - 9y^2 = 576$
5.  $5y^2 - ax^2 = 36$
6.  $49y^2 - 16x^2 = 784$ .

In each of the exercises 7 to 15, find the equations of the hyperbola satisfying the given conditions.

7. vertices  $(\pm 2, 0)$ , foci  $(\pm 3, 0)$
8. vertices  $(0, \pm 5)$ , foci  $(0, \pm 8)$
9. vertices  $(0, \pm 3)$ , foci  $(0, \pm 5)$
10. Foci  $(\pm 5, 0)$ , the transverse axis is of length 8.
11. Foci  $(0, \pm 13)$ , the conjugate axis is of length 24.
12. Foci  $(\pm 3\sqrt{5}, 0)$ , the latus rectum is of length 8.
13. Foci  $(\pm 4, 0)$ , the latus rectum is of length 12
14. vertices  $(\pm 7, 0)$ ,  $e = \frac{4}{3}$ .
15. Foci  $(0, \pm \sqrt{10})$ , passing through  $(2, 3)$

## Miscellaneous Exercise on chapter 11

1. If a parabolic reflector is 20 cm in diameter and 5 cm deep . find the focus.
2. An arch is in the form of a parabola with its axis vertical. The arch is 10 m high and 5 m wide at the base. How wide is it 2 m from the vertex of the parabola ?
3. The cable of a uniform loaded suspension bridge hangs in the form of a parabola. The roadway which is horizontal and 100 m long is supported by vertical wires attached to the cable, the longest wire being 30 m and the shortest being 6 m. Find the length of a supporting wire attached to the roadway 18 m from the middle.
4. An arch is in the form of a semi-ellipse. It is 8 m wide and 2 m high at the centre Find the height of the arch at a point 1.5m from one end.
5. A rod of length 12cm moves with its ends always touching the coordinate axes. Determine the equation of the locus of a point **P** on the rod, which is 3 cm from the end in contact with the  $x$ -axis
6. Find the area of the triangle formed by the lines joining the vertex of the parabola  $x^2 = 12y$  to the ends of its latus rectum.
7. A man running a racecourse notes that sum of the distances from the two flag posts from him is always 10 m and the distance between the flag posts is 8 m. Find the equation of the posts traced by the man.
8. An equilateral triangle is inscribed in the parabola  $y^2 = 4ax$ , where one vertex is at the vertex of the parabola. Find the length of the side of the triangle.