GeeksforGeeks
A computer science portal for geeks

Placements   Practice   GATE CS   IDE   Q&A   GeeksQuiz

Login/Register

Design a stack that supports getMin() in O(1) time and O(1) extra space

An approach that uses O(1) time and O(n) extra space is discussed here.

In this article, a new approach is discussed that supports minimum with O(1) extra space. We define a variable **minEle** that stores the current minimum element in the stack. Now the interesting part is, how to handle the case when minimum element is removed. To handle this, we push "2x – minEle" into the stack instead of x so that previous minimum element can be retrieved using current minEle and its value stored in stack. Below are detailed steps and explanation of working.

Push(x) : Inserts x at the top of stack.

- If stack is empty, insert x into the stack and make minEle equal to x.
- If stack is not empty, compare x with minEle. Two cases arise:
  - If x is greater than or equal to minEle, simply insert x.
  - If x is less than minEle, insert (2*x – minEle) into the stack and make minEle equal to x. For example, let previous minEle was 3. Now we want to insert 2. We update minEle as 2 and insert 2*2 – 3 = 1 into the stack.

Pop() : Removes an element from top of stack.

- Remove element from top. Let the removed element be y. Two cases arise:
  - If y is greater than or equal to minEle, the minimum element in the stack is still minEle.
  - If y is less than minEle, the minimum element now becomes (2*minEle – y), so update (minEle = 2*minEle – y). This is where we retrieve previous minimum from current minimum and its value in stack. For example, let the element to be removed be 1 and minEle be 2. We remove 1 and update minEle as 2*2 – 1 = 3.

Important Points:

- Stack doesn't hold actual value of an element if it is minimum so far.
- Actual minimum element is always stored in minEle

Illustration

Push(x)

Number inserted	Present Stack	minEle
3	3	3
5	5 3	3
2	1 5 3	2
1	0 1 5 3	1
1	1 0 1 5 3	1
-1	-3 1 0 1 5 3	-1

- Number to be Inserted: 3, Stack is empty, so insert 3 into stack and minEle = 3.
- Number to be Inserted: 5, Stack is not empty, 5> minEle, insert 5 into stack and minEle = 3.
- Number to be Inserted: 2, Stack is not empty, 2< minEle, insert (2*2-3 = 1) into stack and minEle = 2.
- Number to be Inserted: 1, Stack is not empty, 1< minEle, insert (2*1-2 = 0) into stack and minEle = 1.
- Number to be Inserted: 1, Stack is not empty, 1 = minEle, insert 1 into stack and minEle = 1.
- Number to be Inserted: -1, Stack is not empty, -1 < minEle, insert (2*-1 – 1 = -3) into stack and minEle = -1.

Pop()

Number removed	Original Number	Present Stack	minEle
-		-3 1 0 1 5 3	-1
-3	-1	1 0 1 5 3	1
1	1	0 1 5 3	1
0	1	1 5 3	2
1	2	5 3	3
5	5	3	3

- Initially the minimum element minEle in the stack is -1.
- Number removed: -3, Since -3 is less than the minimum element the original number being removed is minEle which is -1, and the new minEle = 2*-1 – (-3) = 1
- Number removed: 1, 1 == minEle, so number removed is 1 and minEle is still equal to 1.
- Number removed: 0, 0< minEle, original number is minEle which is 1 and new minEle = 2*1 – 0 = 2.
- Number removed: 1, 1< minEle, original number is minEle which is 2 and new minEle = 2*2 – 1 = 3.
- Number removed: 5, 5> minEle, original number is 5 and minEle is still 3

Implementation:

C++

```
// C++ program to implement a stack that supports
// getMinimum() in O(1) time and O(1) extra space.
#include <bits/stdc++.h>
using namespace std;

// A user defined stack that supports getMin() in
// addition to push() and pop()
struct MyStack
{
    stack<int> s;
    int minEle;

    // Prints minimum element of MyStack
```

```cpp
    void getMin()
    {
        if (s.empty())
            cout << "Stack is empty\n";

        // variable minEle stores the minimum element
        // in the stack.
        else
            cout <<"Minimum Element in the stack is: "
                 << minEle << "\n";
    }

    // Prints top element of MyStack
    void peek()
    {
        if (s.empty())
        {
            cout << "Stack is empty ";
            return;
        }

        int t = s.top(); // Top element.

        cout << "Top Most Element is: ";

        // If t < minEle means minEle stores
        // value of t.
        (t < minEle)? cout << minEle: cout << t;
    }

    // Remove the top element from MyStack
    void pop()
    {
        if (s.empty())
        {
            cout << "Stack is empty\n";
            return;
        }

        cout << "Top Most Element Removed: ";
        int t = s.top();
        s.pop();

        // Minimum will change as the minimum element
        // of the stack is being removed.
        if (t < minEle)
        {
            cout << minEle << "\n";
            minEle = 2*minEle - t;
        }

        else
            cout << t << "\n";
    }

    // Removes top element from MyStack
    void push(int x)
    {
        // Insert new number into the stack
        if (s.empty())
        {
            minEle = x;
            s.push(x);
            cout <<  "Number Inserted: " << x << "\n";
            return;
        }

        // If new number is less than minEle
        if (x < minEle)
```

```cpp
        {
            s.push(2*x - minEle);
            minEle = x;
        }

        else
            s.push(x);

        cout <<  "Number Inserted: " << x << "\n";
    }
};

// Driver Code
int main()
{
    MyStack s;
    s.push(3);
    s.push(5);
    s.getMin();
    s.push(2);
    s.push(1);
    s.getMin();
    s.pop();
    s.getMin();
    s.pop();
    s.peek();

    return 0;
}
```

Run on IDE

Java

```java
// Java program to implement a stack that supports
// getMinimum() in O(1) time and O(1) extra space.
import java.util.*;

// A user defined stack that supports getMin() in
// addition to push() and pop()
class MyStack
{
    Stack<Integer> s;
    Integer minEle;

    // Constructor
    MyStack() { s = new Stack<Integer>(); }

    // Prints minimum element of MyStack
    void getMin()
    {
        // Get the minimum number in the entire stack
        if (s.isEmpty())
            System.out.println("Stack is empty");

        // variable minEle stores the minimum element
        // in the stack.
        else
            System.out.println("Minimum Element in the " +
                                " stack is: " + minEle);
    }

    // prints top element of MyStack
    void peek()
    {
        if (s.isEmpty())
```

```java
        {
            System.out.println("Stack is empty ");
            return;
        }

        Integer t = s.peek(); // Top element.

        System.out.print("Top Most Element is: ");

        // If t < minEle means minEle stores
        // value of t.
        if (t < minEle)
            System.out.println(minEle);
        else
            System.out.println(t);
    }

    // Removes the top element from MyStack
    void pop()
    {
        if (s.isEmpty())
        {
            System.out.println("Stack is empty");
            return;
        }

        System.out.print("Top Most Element Removed: ");
        Integer t = s.pop();

        // Minimum will change as the minimum element
        // of the stack is being removed.
        if (t < minEle)
        {
            System.out.println(minEle);
            minEle = 2*minEle - t;
        }

        else
            System.out.println(t);
    }

    // Insert new number into MyStack
    void push(Integer x)
    {
        if (s.isEmpty())
        {
            minEle = x;
            s.push(x);
            System.out.println("Number Inserted: " + x);
            return;
        }

        // If new number is less than original minEle
        if (x < minEle)
        {
            s.push(2*x - minEle);
            minEle = x;
        }

        else
            s.push(x);

        System.out.println("Number Inserted: " + x);
    }
};

// Driver Code
public class Main
{
```

```java
    public static void main(String[] args)
    {
        MyStack s = new MyStack();
        s.push(3);
        s.push(5);
        s.getMin();
        s.push(2);
        s.push(1);
        s.getMin();
        s.pop();
        s.getMin();
        s.pop();
        s.peek();
    }
}
```

Run on IDE

Output:

```
Number Inserted: 3
Number Inserted: 5
Minimum Element in the stack is: 3
Number Inserted: 2
Number Inserted: 1
Minimum Element in the stack is: 1
Top Most Element Removed: 1
Minimum Element in the stack is: 2
Top Most Element Removed: 2
Top Most Element is: 5
```

How does this approach work?

When element to be inserted is less than minEle, we insert "2x – minEle". The important thing to notes is, 2x – minEle will always be less than x (proved below), i.e., new minEle and while popping out this element we will see that something unusual has happened as the popped element is less than the minEle. So we will be updating minEle.

```
How 2*x - minEle is less than x in push()?
x < minEle which means x - minEle < 0

// Adding x on both sides
x - minEle + x < 0 + x

2*x - minEle < x

We can conclude 2*x - minEle < new minEle
```

While popping out, if we find the element(y) less than the current minEle, we find the new minEle = 2*minEle – y.

```
How previous minimum element, prevMinEle is, 2*minEle - y
in pop() is y the popped element?

  // We pushed y as 2x - prevMinEle. Here
  // prevMinEle is minEle before y was inserted
```

```
y = 2*x - prevMinEle

// Value of minEle was made equal to x
minEle = x .

new minEle = 2 * minEle - y
           = 2*x - (2*x - prevMinEle)
           = prevMinEle // This is what we wanted
```

Exercise:

Similar approach can be used to find the maximum element as well. Implement a stack that supports getMax() in O(1) time and constant extra space.

This article is contributed by **Nikhil Tekwani.** If you like GeeksforGeeks and would like to contribute, you can also write an article and mail your article to contribute@geeksforgeeks.org. See your article appearing on the GeeksforGeeks main page and help other Geeks.

Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above.

Company Wise Coding Practice   Topic Wise Coding Practice

30 Comments Category: Stack

Related Posts:

- Find if an expression has duplicate parenthesis or not
- Implement a stack using single queue
- Check if a given array can represent Preorder Traversal of Binary Search Tree
- Minimum number of bracket reversals needed to make an expression balanced
- Iterative Depth First Traversal of Graph
- Sort a stack using recursion
- Length of the longest valid substring
- Find maximum of minimum for every window size in a given array

(Login to Rate and Mark)

4.2   Average Difficulty : **4.2/5.0**
       Based on **63** vote(s)
                                          Add to TODO List

                                          Mark as DONE

Writing code in comment? Please use code.geeksforgeeks.org, generate link and share the link here.