CS2050-2019-Fall Exam 2

Tejas Rajamadam Pradeep

TOTAL POINTS

89.5 / 100

QUESTION 1 1 Cartesian Product Definition 5 / 5 V - 0 pts {<a,b>| a A ^ b B} QUESTION 2 2 Set Subtraction 5 / 5 V - 0 pts Correct proof by counterexample

QUESTION 3

```
3 Euclidean Algorithm 5 / 5

√ - 0 pts Correct answer 4 with correct work
gcd(56,20)=
gcd(20,16)=
gcd(16,4)=
gcd(4,0)=4
```

QUESTION 4

```
4 Least Common Multiple 5 / 5

\( \sigma - 0 \) pts 2^2 * 3^2 * 5^5 * 7^3 * 11^3
```

QUESTION 5

5 MC Binary Search 5 / 5

+ 0 pts A

√ + **5** pts B

+ **0** pts C

+ 0 pts D

+ O pts E

+ 0 pts No Answer

QUESTION 6

6 MC Compare one to everything else 5/5

+ 0 pts A

+ 0 pts B

+ **0** pts C

√ + **5** pts D

+ 0 pts E

+ 0 pts No Answer

QUESTION 7

7 MC Inductive Hypothesis 5 / 5

+ 0 pts A

+ 0 pts B

+ 0 pts C

√ + 5 pts D

+ 0 pts No Answer

QUESTION 8

8 MC Powerset 5/5

+ 0 pts A

+ 0 pts B

+ 0 pts C

√ + **5** pts D

+ 0 pts No Answer

QUESTION 9

9 MC Cardinality of Powerset 5 / 5

+ 0 pts A

+ 0 pts B

√ + 5 pts C

+ 0 pts D

+ 0 pts E

+ 0 pts No Answer

QUESTION 10

10 MC 1-1 and onto of mapping #1 o / 5

+ 0 pts A

+ 0 pts B

+ 0 pts C

+ 5 pts D

√ + 0 pts E

+ 0 pts No Answer

QUESTION 11

11 MC 1-1 and onto of mapping #25/5

- + **0** pts A
- + 0 pts B
- + **0** pts C
- + 0 pts D
- √ + 5 pts E
 - + 0 pts No Answer

QUESTION 12

12 Math Induction 9.5 / 10

 $\sqrt{-0.5}$ pts Main conclusion does not state that P(n) is true for all positive integers n

QUESTION 13

13 Set complement 5 / 5

√ - 0 pts {a,c}

QUESTION 14

14 Terms of a sequence 5/5

$$\sqrt{-0}$$
 pts a1 = 3, a2 = 9, a3= 27

QUESTION 15

15 MC 1-1 and onto of a function 5 / 5

- + 0 pts A
- + 0 pts B
- + 0 pts C
- + 0 pts D
- √ + **5** pts E
 - + 0 pts No Answer

QUESTION 16

16 MC Set Logic 5 / 5

- + 0 pts A
- √ + **5** pts B
 - + 0 pts No Answer

QUESTION 17

17 MC Proper Subsets 0 / 5

- √ + 0 pts A
 - + **5 pts** B
 - + 0 pts C

+ 0 pts No Answer

QUESTION 18

18 MC Divisibility 5 / 5

- √ + 5 pts A
 - + 0 pts B
 - + 0 pts C
 - + 0 pts No Answer

QUESTION 19

19 Caesar Cipher 5 / 5

√ - 0 pts KHOOR

Copyright © 2019 All rights reserved. Duplication and/or usage for purposes of any kind without permission is strictly forbidden.

CS 2050 Exam 2 - Fall 2019 October 18

	TERAS	PRADEEP	
Name (print clearly):		C 1'de	and with the Academic Honor Code of Georgia

Taking this exam signifies you are aware of and in accordance with the Academic Honor Code of Georgia.

Fairness matters - Do not open this exam until instructed to do so.

- There are no breaks during this exam.
- Signing signifies you are aware of and in accordance with the Academic Honor Code of Georgia Tech and the Code of Conduct.
- When time is called you are to stop writing immediately. No exceptions.
- You are not allowed to speak to other students during the exam unless that student is a TA proctor.
- Do your best to keep your answers covered.
- You are to uphold the honor and integrity expected of you.
- Books, notes, laptops, cell phones, smart watches, etc. are NOT allowed.
- Calculators are not allowed in CS2050.

Page:	2	3	4	5	6	7	Total
Points:	10	10	35	10	30	5	100
Score:							

[5] 1. Give the definition of $A \times B$ (the Cartesian product of A and B) using set builder notation. Assume A and B are sets. Your solution should contain no set operations other than "is an element-of" written as the symbol ∈.

[5] 2. Given sets named A and B, prove A - B = B - A is always true (that is that set subtraction is a commutative operation) or use a proof by counter-example to show that set subtraction is not commutative.

Conclusion: hence using counter axample, 9 harr hown that the state ment.

A. B. B-A is not always here.

[5] 3. Show your work computing gcd(56, 20) using the Euclidean algorithm. (We want to see 1) all of the intermediate results and also 2) the final integer answer.) No credit for answers not demonstrating the correct use of the Euclidean algorithm or simply giving the final integer result.

$$gcd(56,20) = gcd(20,56 \mod 20)$$

= $gcd(20,16)$
= $gcd(16, 20 \mod 16)$
= $gcd(16,4)$
= $gcd(4,16 \mod 4)$
= $gcd(4,0) = 4$

[5] 4. Give the least common multiple (lcm) of the following. Leave your answer in prime factorized form. $lcm(3^2 \cdot 5^5 \cdot 7^3, 2^2 \cdot 3^1 \cdot 5^5 \cdot 11^3) =$

- [5] 5. Assume you have n pieces of data to process. If an algorithm tends to repeatedly cut the data in half each time and pursue the processing with only one of the halves as it continues (and it never comes back to process the other half), what is the correct Big O to describe the behavior of the algorithm? (Give the smallest, most descriptive Big O, that describes the behavior.) Circle your answer.
 - (a) O(1)
 - ((b)) $O(\log n)$:
 - (c) O(n)
 - (d) $O(n^2)$
 - (e) $O(2^n)$
- [5] 6. If an algorithm needs to compare every piece of data with every other piece of data (and assume that there is no way to prevent this behavior), what is the correct Big O to describe the behavior of the algorithm given n pieces of data? (Give the smallest, most descriptive Big O, that describes the behavior.) Circle your answer.
 - (a) O(1)
 - (b) $O(\log n)$
 - (c) O(n)
 - (a) $O(n^2)$
- [5] 7. Within an inductive proof proving P(n) is true for all positive integers, what exactly is the inductive hypothesis? Circle your answer.
 - (a) inductive principle
 - (h) the statement that P(l-) > P(l- 1) is true
 - (c) the outcome that P(k + 1) is true
- (d) the assumption that P(k) is true 8. If $\mathbb{P}(S) = \{\}$, then what is true? Circle your answer.

 (a) $S = \{\}$ (b) $S = \{0\}$ (c) $S = \{\{\}\}$

- (c) $S = \{\{\}\}$

(d) there has been an error because {} cannot be the powerset of any set

- [5] 9. If $S = \{1, 1, 2, 2, 5\}$, then what is the size of $\mathbb{P}(S)$? Circle your answer.
 - (a) 5

 - - (c) none of the above
- [5] 10. Imagine a function f mapping elements of set A to elements of set B. The cardinality of set A is 10. The cardinality of set B is 20. What do we know about this function f? Circle your answer.
 - (a) f is one-to-one
 - (b) f cannot be one-to-one
 - 6 (c) f is onto
 - (d) f cannot be onto
 - (c) none of the above
- [5] 11. Imagine a function f mapping elements of set A to elements of set B. The cardinality of set A is 10. The cardinality of set B is 10. What do we know about this function f? Circle your answer.
 - (a) f is one-to-one
 - (b) f cannot be one-to-one
 - (c) f is onto
 - (d) f cannot be onto
 - (e) none of the above

[10] 12. Use the Principle of Mathematical Induction to prove

$$P(n): \sum_{i=1}^{n} (2i-1) = n^2$$
. Prove $P(n)$ is true for all $n \in \mathbb{Z}^+$.

Basis Step: Show that P(1) is the

$$n^2 = 1^2 = 1$$

RHS

I have show that the train basis step is true, in Pla) is true.

3. H3+...+2K-1 = K2 def'n of 2 operation

$$(1)^{-1} = K^{2} + (2(K+1)^{-1})$$

4. (+3+,,,+2K-1+2(K+1)-1 = K2+(2(K+1)-1) Adding 2(K+1)-1 to LHS

Simply fying math

1,1+3+ ...+2K-1+2(K+1)-1= K2+K+K+1 7. 143+ -- +2K-1+2(MK+1)-1 = K(K+1) +(K+1)

1+3+...+2K-1+2(K+1)-1:(K+1)(K+1)

o & ai-1= (KII)

1. PCK+1)

Spliting 2K into K+K Fautoring K from K2+K Factoring (1) on RHS def n 7 E

Simply lying (K+1) K+1) to

definit P(K+1)

Hence & Assume PCK), ghave shown pekrith be the, hence the Indudive step is true. Conclusion: - 9 lare 3 hown both basis step and inductive step to be the, hence, using the Principle of Mathematical Induction, I have shown Pan to be true.

[5] 13. Suppose the universal set $U = \{a, c, g, t\}$. $S = \{g, t\}$. Write \overline{S} (the complement of S) using list notation.

[5] 14. What are the terms a_1, a_2, a_3 of the sequence $\{a_n\}$, where $a_n = 3^n, n \in \mathbb{Z}^+$?

$$a_{1} = 3^{2}$$
 $a_{2} = 3^{2} = 9$
 $a_{3} = 3^{3} = 97$

[5] 15. You are given the following function information. What is true? Circle your answer.

$$f: \mathbb{Z} \to \mathbb{Z}$$
, where $f(x) = x^2$.

- (a) f is not a function \checkmark
- (b) f is one-to-one and onto \times
- (c) f is one-to-one, but not onto y
- (d) f is not one-to-one, but it is onto
- e (e) f is not one-to-one, and it is not onto
- [5] 16. If A, B, and C are sets such that $A \cup C = B \cup C$ then we know A = B. Circle your answer.
 - (a) the statement is true
- A= {1,23 C- {234
- (b) the statement is false
- [5] 17. For all sets, S, $\{\} \subset S$. Circle your answer.
 - (a) the statement is true
 - (b) the statement is false
 - (c) cannot be determined
- [5] 18. If a, b, c, d are four positive integers such that $a \mid b$ and $b \mid c$, then $a \mid cd$. Circle your answer,
 - (a) the statement is true
- c + b: 200
- (b) the statement is false
- (c) it cannot be determined A Koor

[5] 19. If the original phrase is "hello", what is resultant phrase when encrypted by the Caesar cipher? For your reference, the English alphabet is given here. abcdefghijklmnopqrstuvwxyz

abcdefghijklmnopvåstuvwxy2 012345678910111213141516171819202122232425

 $h - (p+3) \mod 26 = (7+3) \mod 26 = 10 \mod 26 = 10 - K$ $e - (p+3) \mod 26 = (4+3) \mod 26 = 7 \mod 26 = 7 - h$ $e - (p+3) \mod 26 = (4+3) \mod 26 = 14 \mod 26 = 14 = 0$ $e - (p+3) \mod 26 = (1+3) \mod 26 = 14 \mod 26 = 14 = 0$ $e - (p+3) \mod 26 = (1+3) \mod 26 = 17 \mod 26 = 1$ $e - (p+3) \mod 26 = (14+3) \mod 26 = 17 \mod 26 = 1$

encypted version of hello, using a Gesar cipher is Khoor

This page provides extra space if you need it. Clearly mark any question that has its answer here.

Do not open this exam until instructed to do so.