

Shylaja S S

Department of Computer Science & Engineering



Bubble Sort

Major Slides Content: Anany Levitin

Shylaja S S

Department of Computer Science & Engineering

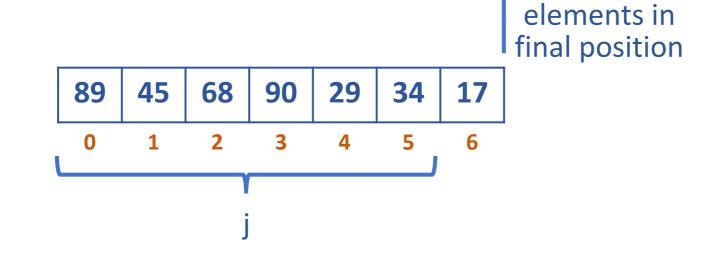


- Compare adjacent elements of the list and exchange them if they are out of order
- By doing it repeatedly, we end up bubbling the largest element to the last position on the list
- The next pass bubbles up the second largest element and so on and after n-1 passes, the list is sorted
- Pass i $(0 \le i \le n-2)$ can be represented as follows:

$$A[0], A[1], A[2], ..., A[j] \xrightarrow{?} A[j+1], ..., A[n-i-1] \mid A[n-i] \leq \leq A[n-1]$$

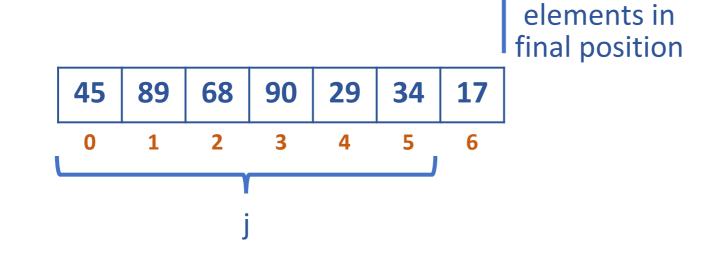
Bubble Sort





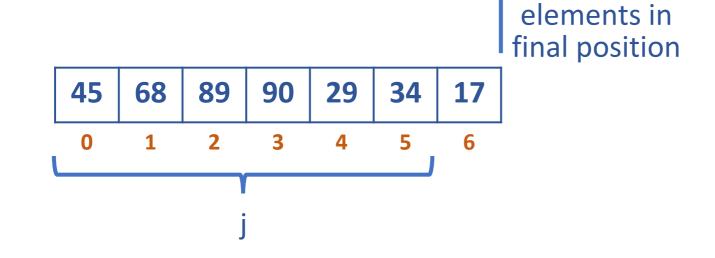
Bubble Sort





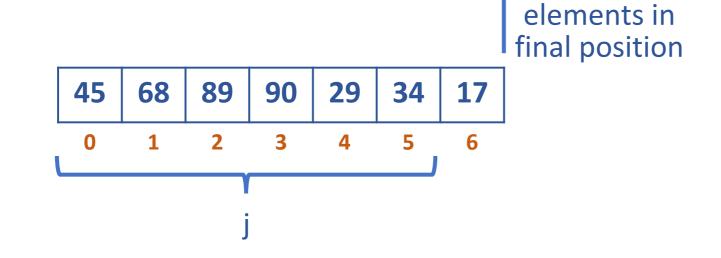
Bubble Sort





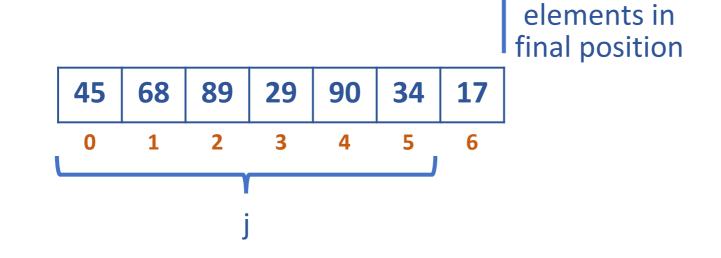
Bubble Sort





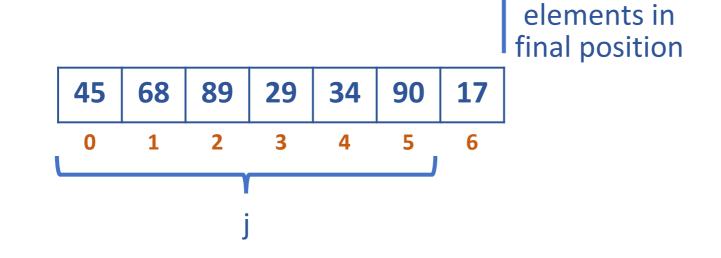
Bubble Sort



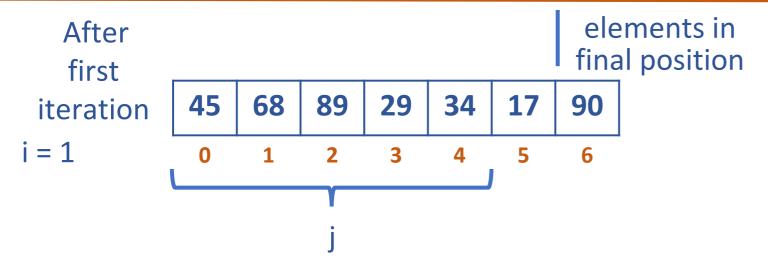


Bubble Sort

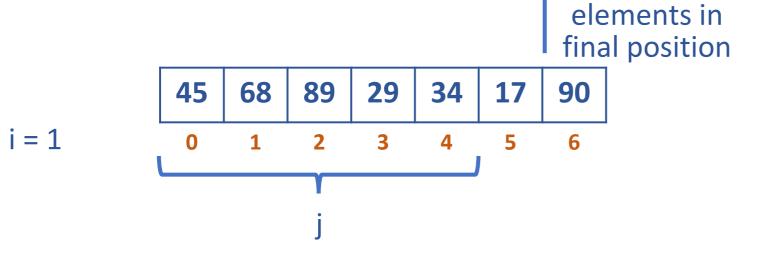




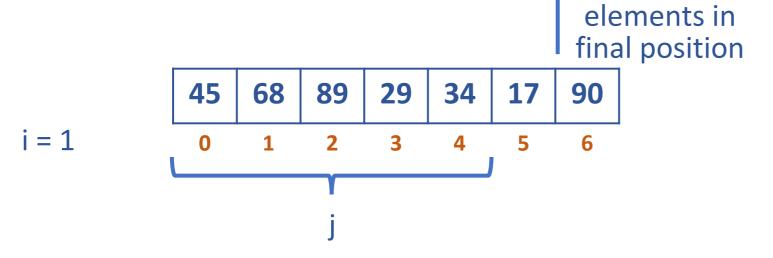




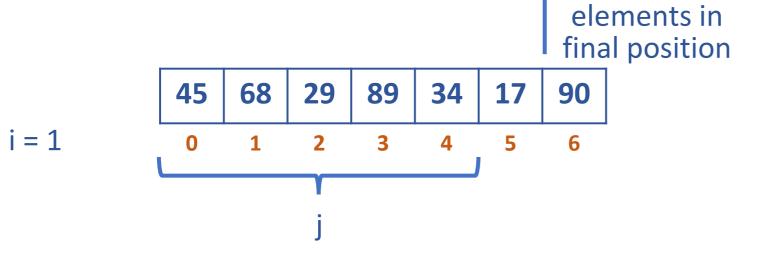




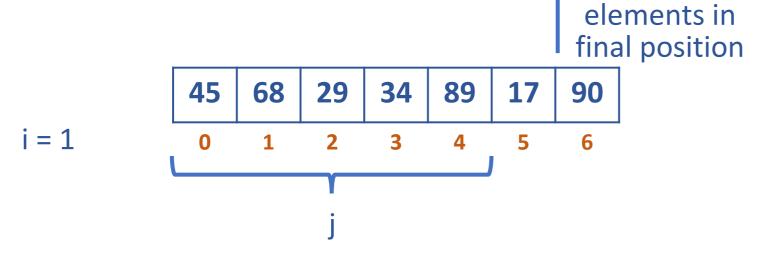




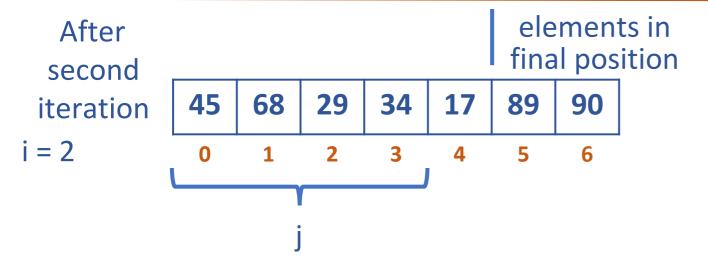




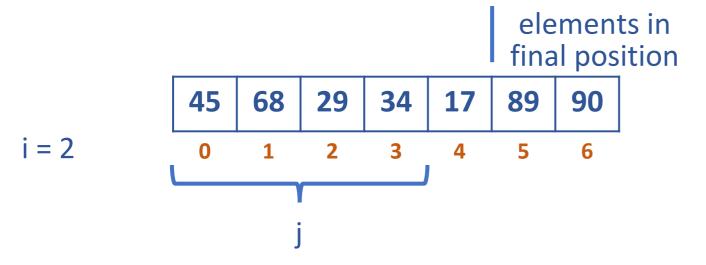




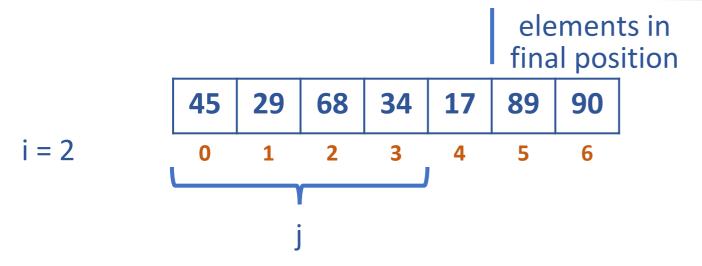




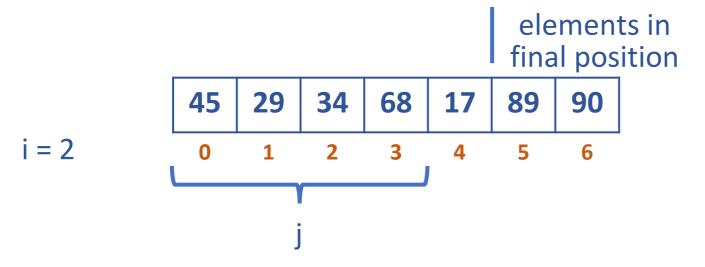




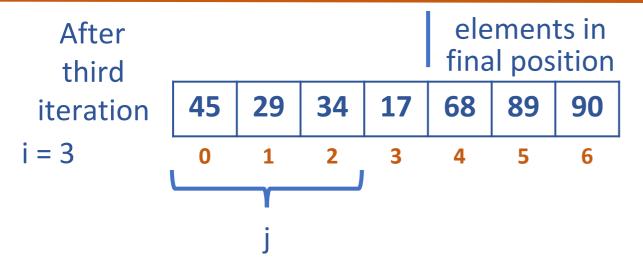






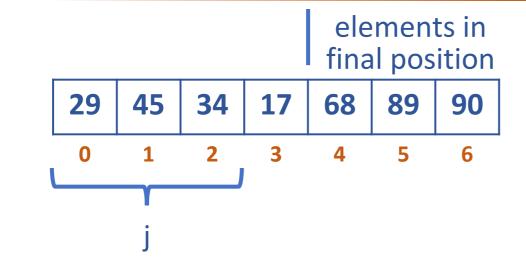






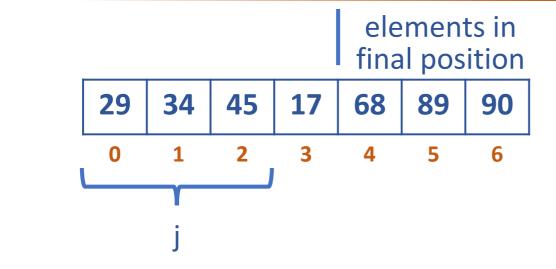
Bubble Sort



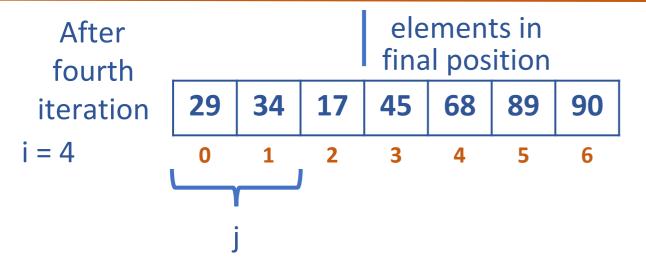


Bubble Sort



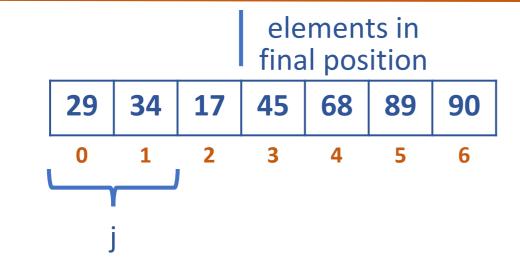




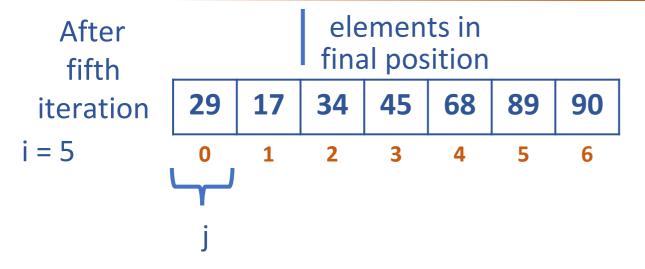


Bubble Sort





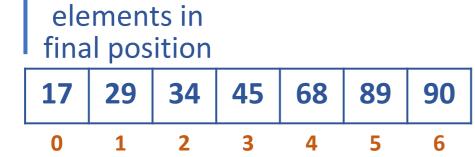




Bubble Sort



After sixth iteration





```
ALGORITHM BubbleSort(A[0 .. n - 1])

//Sorts a given array by bubble sort in their final positions

//Input: An array A[0 .. n - 1] of orderable elements

//Output: Array A[0 .. n- 1] sorted in ascending order

for i <-- 0 to n - 2 do

for j <-- 0 to n - 2 - i do

if A[j+1] < A[j] swap A[j] and A[j+1]
```

Bubble Sort



Bubble Sort Analysis

$$C(n) = \sum_{i=0}^{n-2} \sum_{j=0}^{n-2-i} 1 = \sum_{i=0}^{n-2} [(n-2-i) - 0 + 1]$$

$$=\sum_{i=0}^{n-2}(n-1-i)=\frac{(n-1)n}{2}\in\Theta(n^2)$$

Bubble Sort is a $\Theta(n^2)$ algorithm



THANK YOU

Shylaja S S

Department of Computer Science & Engineering

shylaja.sharath@pes.edu