

Kadane's Algorithm



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Maximum Subarray Sum

continuous

1	2	3	4	5
---	---	---	---	---

1, 2, 3, 4, 5

12, 23, 34, 45

123, 234, 345

1234, 2345

12345

$$\#subarr = \frac{n*(n+1)}{2}$$

$$n=5 \Rightarrow \frac{5*6}{2} = 15$$

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Maximum Subarray Sum

continuous part

1	2	3	4	5
---	---	---	---	---

↑

start

end (st to n-1)

0

0, 1, 2, 3, 4

1

1, 2, 3, 4

2

2, 3, 4

```
for (st = 0; st < n; st++) {
```

```
    for (end = st; end < n; end++) {
```

⇒ (st to end)

```
    }
```

```
}
```

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```

code.cpp x
code.cpp > main()
1 #include <iostream>
2 #include <vector>
3 using namespace std;
4
5 int main() {
6     int n = 5;
7     int arr[5] = {1, 2, 3, 4, 5};
8
9     for(int st=0; st<n; st++) {
10         for(int end=st; end<n; end++) {
11             for(int i=st; i<=end; i++) {
12                 cout << arr[i];
13             }
14             cout << " ";
15         }
16         cout << endl;
17     }
18
19     return 0;
}

PORTS PROBLEMS DEBUG CONSOLE OUTPUT TERMINAL
apnacollege@Shradha DSAseries % g++ -std=c++11 code.cpp && ./a.out
1 12 123 1234 12345
2 23 234 2345
3 34 345
4 45
5
apnacollege@Shradha DSAseries %

```




Maximum Subarray Sum $O(n^2)$

Brute Force Approach

3, -4, 5, 4, -1, 7, -8

$st = 0$

for (st = 0; st < n; st++) {
 for (end = st; end < n; end++) {
 $\Rightarrow (st \text{ to } end)$
 }
}



Maximum Subarray Sum $O(n^2)$


Brute Force Approach

{ 3, -4, 5, 4, -1, 7, -8 }

$st = 0$ end

$CS = -1 + 5 = 4$


for (st = 0; st < n; st++) {
 maxSum
 currSum = 0
 for (end = st; end < n; end++) {
 CS += arr[end]
 maxSum = max(CS, maxSum);
 }
 return maxSum
}



```

code.cpp x
code.cpp > main()
4
5 int main() {
6     int n = 5;
7     int arr[5] = {1, 2, 3, 4, 5};
8
9     int maxSum = INT_MIN;
10
11     for(int st=0; st<n; st++) {
12         int currSum = 0;
13         for(int end=st; end<n; end++) {
14             currSum += arr[end];
15             maxSum = max(currSum, maxSum);
16         }
17     }
18
19     cout << "max subarray sum = " << maxSum << endl;
20
21     return 0;
22 }
23
24
PORTS PROBLEMS DEBUG CONSOLE OUTPUT TERMINAL
apnacollege@Shradha DSAseries % g++ -std=c++11 code.cpp && ./a.out
max subarray sum = 15
apnacollege@Shradha DSAseries %

```



Kadane's Algorithm

Most Optimised

{ 3, -4, 5, 4, -1, 7, -8 }

currSum = 0 maxSum = INT_MIN

```

for(i = 0; i < n; i++) {
    currSum += arr[i]
    maxSum = max(cs, ms)
    if(cs < 0)
        cs = 0
}

```

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Intuition

$pos + pos \rightarrow +$
 $neg + pos \rightarrow +$
 $pos + neg \rightarrow neg$
 (reset to 0)



Kadane's Algorithm

Most Optimised

{ 3, -4, 5, 4, -1, 7, -8 }

currSum = 0 maxSum = INT_MIN

```

for(i = 0; i < n; i++) {
    currSum += arr[i]
    maxSum = max(cs, ms)
    if(cs < 0)
        cs = 0
}

```

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$CS = 0, -1, 0, 5, 9, 8, 15, 7$
 $MS = -4, 3, 5, 9, 15$

edge / corner
 $arr = [-1, -2, -3, -4, -5]$
 $max\ sub\ sum = -1$



leetcode.com/problems/maximum-subarray/

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Description Editorial Solutions Submissions

53. Maximum Subarray

Solved

Medium Topics Companies

Given an integer array `nums`, find the **subarray** with the largest sum, and return its sum.

Example 1:

Input: `nums = [-2,1,-3,4,-1,2,1,-5,4]`
 Output: 6
 Explanation: The subarray `[4,-1,2,1]` has the largest sum 6.

Example 2:

Input: `nums = [1]`
 Output: 1
 Explanation: The subarray `[1]` has the largest sum 1.

Example 3:

Input: `nums = [5,4,-1,7,8]`
 Output: 23
 Explanation: The subarray `[5,4,-1,7,8]` has the largest sum 23.

```

C++
1 int maxSubArray(vector<int>& nums) {
2     int currSum = 0, maxSum = INT_MIN;
3
4     for(int val : nums) {
5         currSum += val;
6         maxSum = max(currSum, maxSum);
7
8         if(currSum < 0) {
9             currSum = 0;
10        }
11    }
12
13    return maxSum;
14 }
  
```

Testcase Test Result

Case 1 Case 2 Case 3 +

nums = [-2,1,-3,4,-1,2,1,-5,4]

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ALPHA

Kadane's Algorithm

Most Optimised

`{ 3, -4, 5, 4, -1, 7, -8 }`

$currSum = 0$ $maxSum = INT_MIN$

$O(n)$
linear

```

for(i = 0; i < n; i++) {
    currSum += arr[i]
    maxSum = max(currSum, maxSum)
    if(currSum < 0)
        currSum = 0
}
  
```

$arr = [-1, -2, -3, -4, -5]$

edge / corner

$max\ sub\ sum = -ve$

Print Screen

ALPHA