

Chapter-6 Binary Number System



Binary Number System

0/1
Base 2

Math: Decimal Number System
0-9 // 10 Digits
Base 10

Hexadecimal
Base 16

Octal
Base 8



Decimal to Binary

$\xleftrightarrow{2 \text{ to } 10}$

2	42	0
2	21	1
2	10	0
2	5	1
2	2	0
2	1	1
	0	

$$(42)_{10} = (101010)_2$$

2	50	0
2	25	1
2	12	0
2	6	0
2	3	1
2	1	1
	0	

$$(110010)_2 = (50)_{10}$$



Decimal to Binary

Code

decNum

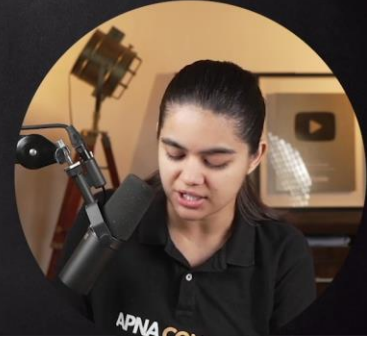
ans = 0 // binNum

```
while (decNum > 0) {
    rem = decNum % 2;
    decNum = decNum / 2;
}
```

ans = 101
 $1 \times 10^2 + 0 \times 10^1 + 1 \times 10^0$
 $100 + 0 + 1$
 $= 101$

$n=5$

2	5	1×10^0
2	2	0×10^1
2	1	1 ←
	0	



Decimal to Binary

Code decNum

ans = 0 // binNum
 pow = 1 // $10^0 \rightarrow 10^1 \rightarrow 10^2 \rightarrow 10^3 \dots$

```
while (decNum > 0) {
    rem = decNum % 2;
    decNum = decNum / 2;
    ans += (rem * pow);
    pow = pow * 10;
}
```

ans = ✓

ans = 0 + 10 + 100
 pow = 100

$n=5$
 rem = 0
 rem = 1
 rem = 1

$**(100)_2 = (6)_{10}$

$\rightarrow [110]_{10} = [6]_2$




```
code.cpp x
code.cpp > main()
3
4 int decToBinary(int decNum) {
5     int ans = 0, pow = 1;
6
7     while (decNum > 0) {
8         int rem = decNum % 2;
9         decNum /= 2;
10
11         ans += (rem * pow);
12         pow *= 10;
13     }
14
15     return ans; //binary form
16 }
17
18 int main() {
19     int decNum = 50;
20
21     cout << decToBinary(decNum) << endl;
22     return 0;
23 }
24
25
PORTS PROBLEMS DEBUG CONSOLE OUTPUT TERMINAL
apnacollege@Shradha DSASeries % g++ code.cpp && ./a.out
110010
apnacollege@Shradha DSASeries %
```



```
code.cpp x
code.cpp > main()
3
4 int decToBinary(int decNum) {
5     int ans = 0, pow = 1;
6
7     while(decNum > 0) {
8         int rem = decNum % 2;
9         decNum /= 2;
10
11         ans += (rem * pow);
12         pow *= 10;
13     }
14
15     return ans; //binary form
16 }
17
18 int main() {
19     int decNum = 50;
20
21     for(int i=1; i<=10; i++) {
22         cout << decToBinary(i) << endl;
23     }
24     return 0;
25 }
```

PORTS PROBLEMS DEBUG CONSOLE OUTPUT TERMINAL

101
110
111
1000
1001
1010



Binary to Decimal

$$\begin{array}{r} 2^5 \quad 2^4 \quad 2^3 \quad 2^2 \quad 2^1 \\ 1 \quad 1 \quad 0 \quad 0 \quad 10 \\ \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow 2^0 \\ 32 + 16 \quad 0 \quad 0 + 2 \quad 0 \\ \hline 50 \end{array}$$

1100101
→ Decimal



Binary to Decimal

Code

```
binNum; ans=0, pow=1 //2^0
while( binNum>0) {
    rem = binNum%10
    ans += binNum * pow
    binNum /= 10
    pow *= 2
}
```

ans

- ~~101~~
- ① rem
 - ② ans += rem * pow
 - ③ num = num/10
 - ④ pow = pow * 2
- update




```

code.cpp x
code.cpp > main()
17
18 int binToDecimal(int binNum) {
19     int ans = 0, pow = 1;
20
21     while(binNum > 0) {
22         int rem = binNum % 10;
23         ans += rem * pow;
24
25         binNum /= 10;
26         pow *= 2;
27     }
28
29     return ans; //decimal form
30 }
31
32 int main() {
33     cout << binToDecimal(101) << endl; //5
34     return 0;
35 }
36
37
PORTS PROBLEMS DEBUG CONSOLE OUTPUT TERMINAL
apnacollege@Shradha DSAseries % g++ code.cpp && ./a.out
5
apnacollege@Shradha DSAseries %

```

25 - 16 = 9 - 8 = 1 - 1 = 0

Common Numbers

0	→	00
1	→	01
2	→	10
3	→	11
4	→	100
5	→	101
6	→	110
7	→	111
8	→	1000
9	→	1001
10	→	1010

1	1	0	0	1
16	8	4	2	1
✓	✓	x	x	✓

36 - 32 = 4 - 4 = 0

Common Numbers

0	→	00
1	→	01
2	→	10
3	→	11
4	→	100
5	→	101
6	→	110
7	→	111
8	→	1000
9	→	1001
10	→	1010

1	0	0	1	0	1
32	16	8	4	2	1
✓	x	x	✓	x	x

37
41
19
Bin

Common Numbers

0	→	00
1	→	01
2	→	<u>10</u>
3	→	11
4	→	100
5	→	101
6	→	110
7	→	111
8	→	1000
9	→	1001
10	→	1010

$$\begin{array}{r} 0 \\ +0 \\ \hline 0 \end{array} \quad \begin{array}{r} 0 \\ +1 \\ \hline 1 \end{array} \quad \begin{array}{r} 1 \\ +0 \\ \hline 1 \end{array} \quad \begin{array}{r} 1 \\ +1 \\ \hline 10 \end{array}$$

$$\begin{array}{r} 1 \\ +1 \\ \hline 2 \end{array} 10$$



Two's complement

int n = -10

① 1010

② 01010

③ 10101

④ 10110

$$(-10)_{10} = (0110)_2$$

- ① Binary Form convert
- ② Prefix with a 0
- ③ 1's complement
0 → 1
1 → 0
- ④ add +1



Two's complement

10110

① 01001

② 01010

$$(1010) \rightarrow (10)_{10}$$

$$(-10)$$

Bin → Dec

↓ 2's comp

① 1's comp

② +1

- ① Binary Form convert
- ② Prefix with a 0
- ③ 1's complement
0 → 1
1 → 0
- ④ add +1

Dec → Bin



Qs

Convert -8 to binary & reverse.

-8

① 1000

② 01000

③ 10111


④ 11000

$(11000)_2 = (-8)_{10}$

11000 $\xrightarrow{-ve}$ (-8)

① 00111

② 01000 = 8




Bin \rightarrow Dec + code

Dec \rightarrow Bin + code

common ✓ trick

add

2's comp / 1's comp



Homework Solutions:

0001

0010

0011

0100

0101

0110

0111

1000

1001

1010