

# Software Testing 1

Software Engineering  
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# Learning objectives

- Control flow test coverage
- Estimating the number of paths

# Control Flow Test Coverage

# How much testing is needed?

- Problem 1. Sometimes developers do not write enough tests.
- Problem 2. Sometimes they write too many redundant tests, causing overhead.
- Problem 3. During software evolution, we don't have time to rerun all tests again. Identifying relevant tests to rerun is hard.

We need a way to tell how much testing is needed and where to focus!

# Test Coverage

- One way of ensuring test adequacy is to increase code coverage by tests
- What tests can give us enough coverage for this code?
- We are going to focus on control flow test coverage which is based on the code's Control Flow Graph

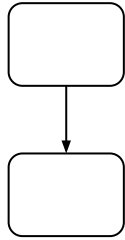
```
public class PathExample {  
  
    public int returnInput (int x,  
                            boolean cond1,  
                            boolean cond2,  
                            boolean cond3) {  
  
        if (cond1) {  
            x++;  
        }  
        if (cond2) {  
            x--;  
        }  
        if (cond3) {  
            x=x;  
        }  
        return x;  
    }  
}
```

# Control Flow Test Coverage Criteria

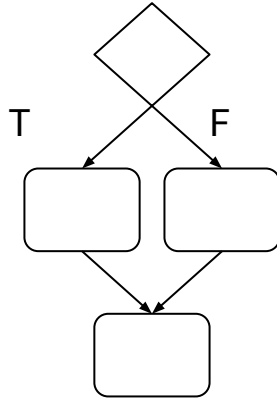
- Statement coverage
  - Percentage of statements exercised by tests
- Branch coverage
  - Percentage of branches (condition evaluations) exercised by tests
- Path coverage
  - Percentage of control flow paths exercised by tests

```
public class PathExample {  
  
    public int returnInput (int x,  
                           boolean cond1,  
                           boolean cond2,  
                           boolean cond3) {  
  
        if (cond1) {  
            x++;  
        }  
        if (cond2) {  
            x--;  
        }  
        if (cond3) {  
            x=x;  
        }  
        return x;  
    }  
}
```

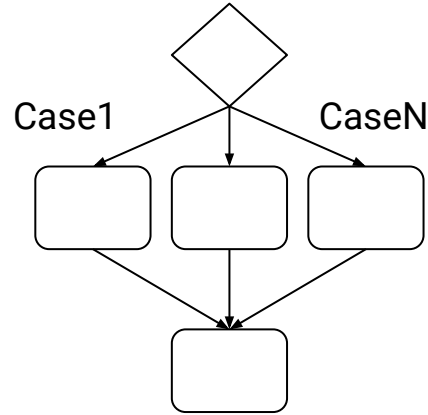
# Control Flow Graph (CFG) Notation



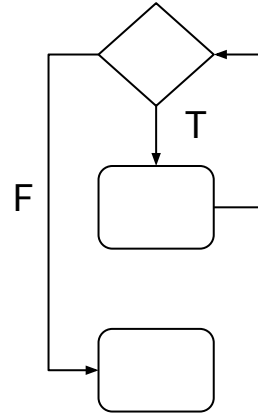
Sequence



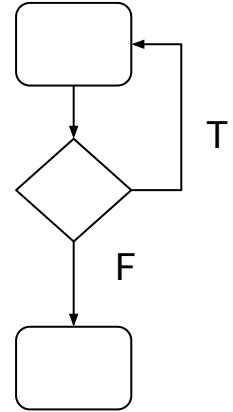
If-then-else



Switch



While



Do-While

# Example 1

After execution of each statement in the test below, what is the **cumulative** statement, branch and path coverage respectively?

```
@Test public void testReturnInput () {  
    PathExample p = new PathExample();  
    assertEquals(p.returnInput(3, true, true, true), 3);  
    assertEquals(p.returnInput(5, false, false, false), 5);  
    assertEquals(p.returnInput(2, false, true, true), 1);  
}
```

```
public class PathExample {  
  
    public int returnInput (int x,  
        boolean cond1,  
        boolean cond2,  
        boolean cond3) {  
  
        if (cond1) {  
            x++;  
        }  
        if (cond2) {  
            x--;  
        }  
        if (cond3) {  
            x=x;  
        }  
        return x;  
    }  
}
```



# Solution Step 1: Draw CFG

```
public class PathExample {
```

```
    public int returnInput (int x,  
        boolean cond1,  
        boolean cond2,  
        boolean cond3) {
```

```
        if (cond1) {  
            x++;
```

```
        }
```

```
        if (cond2) {  
            x--;
```

```
        }
```

```
        if (cond3) {  
            x=x;
```

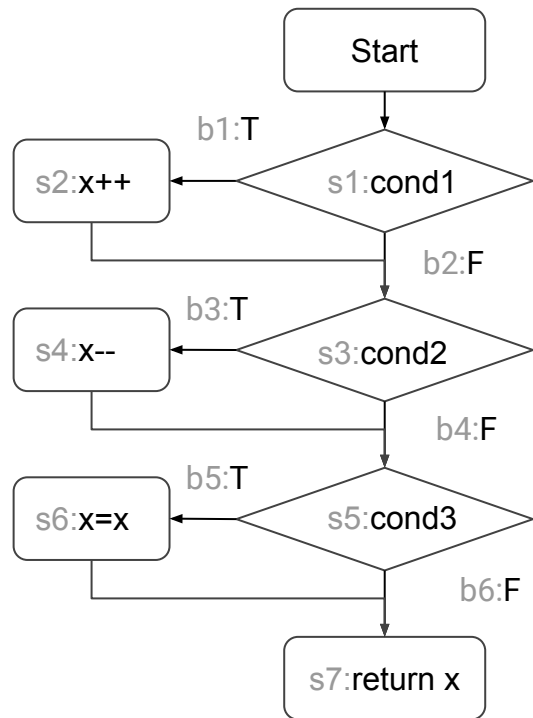
```
        }
```

```
        return x;
```

```
    }
```

```
}
```

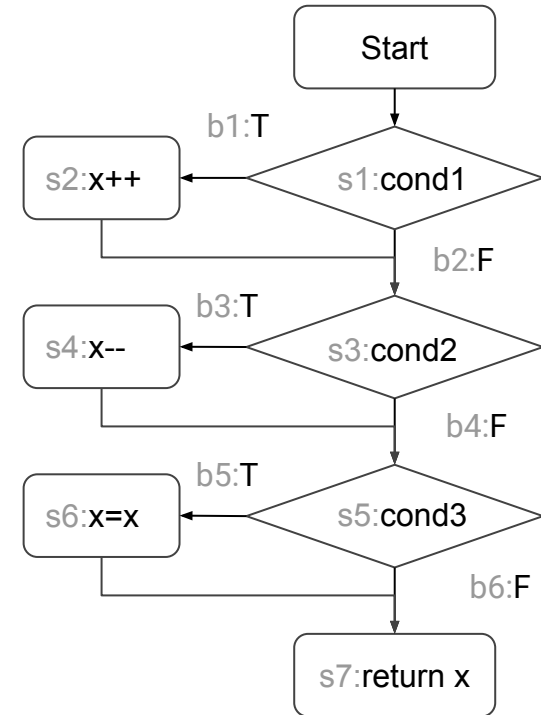
Draw the CFG of the code:



# Solution Step 2: Fill Test Coverage Table

Fill out a code coverage table below by running the consecutive statements in the test (coverage is **cumulative**):

Input	Exercised Statements	Exercised Branches	Exercised Paths
(x=3, cond1=T, cond2=T, cond3=T)	s1, s2, s3, s4, s5, s6, s7	b1, b3, b5	[b1, b3, b5]
Coverage	100%	50%	12.5%
(x=5, cond1=F, cond2=F, cond3=F)	s1, s3, s5, s7	b2, b4, b6	[b2, b4, b6]
Coverage	100%	100%	25%
(x=2, cond1=F, cond2=T, cond3=T)	s1, s3, s4, s5, s6, s7	b2, b3, b5	[b2, b3, b5]
Coverage	100%	100%	37.5%



# Branch Coverage

- Branch coverage is measured with respect to whether the decision takes the **true** or **false** branches.
- Suppose that we have a simple program  
**if** (x>1) x++ **else** x--;
- T1: x=2 makes the decision evaluate to T
- T2: x=0 makes the decision evaluate to F
- So when we have T1 only, it's 50% in terms of branch coverage, while when we have T1 and T2 we have 100%
- Is adding T3: x=3 necessary?

# Example 2

- Consider a program with three decisions in a row.

```
public static int calculate(int x, int y, int z) {  
    if (x>1) x++ else x--;  
    if (y>2) y:=0 else y:=1;  
    if (z>3) z:=0 else z:=2;  
    return x+y+z;  
}
```

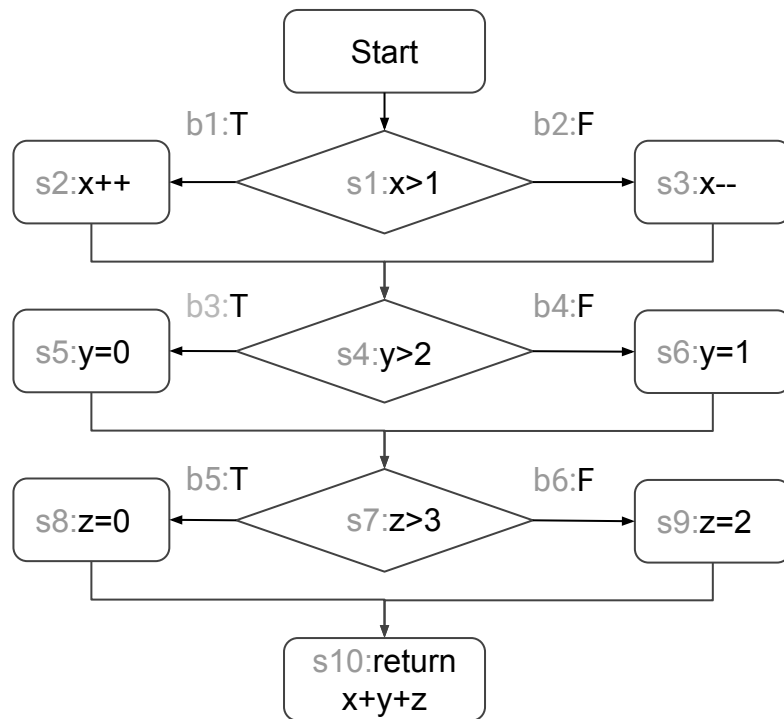
- What is a cumulative statement, branch and path coverage respectively after executing the following Test?

```
@Test  
public void testReturnInput () {  
    assertEquals(calculate(2, 3, 4), 3);  
    assertEquals(calculate(0, 1, 2), 2);  
}
```

# Solution

```
public static int calculate(int x, int y, int z) {  
    if (x>1) x++ else x--;  
    if (y>2) y:=0 else y:=1;  
    if (z>3) z:=0 else z:=2;  
    return x+y+z;  
}
```

Input	Exercised Statements	Exercised Branches	Exercised Paths
T1(x=2,y= 3,z= 4)	s1,s2,s4,s5,s7,s8 ,s10	b1,b3,b5	[b1, b3, b5]
Coverage	70%	50%	12.5%
T1(x=0,y= 1,z= 2)	s1,s3,s4,s6,s7,s9 ,s10	b2,b4,b6	[b2, b4, b6]
Coverage	100%	100%	25%



# Estimating the Number of Paths

# Estimating the number of paths

- Specifically, estimating the number of feasible loop iterations for bounded programs
- For a loop-free program with **k** decisions, the number of feasible paths is  $2^k$ 
  - Only consider decisions that are nondeterministic (i.e., may evaluate to **true** or **false**)
- How about a program with loops?
- In this case, we first perform loop **unrolling**, then the number of paths is  $2^{(\# \text{ nondeterministic decisions})}$

# Example 1

- What is the number of decisions in the loop-unrolled program?
- What is the maximum number of paths?
- After executing each statement in the test, what is the cumulative statement, branch and path coverage respectively?

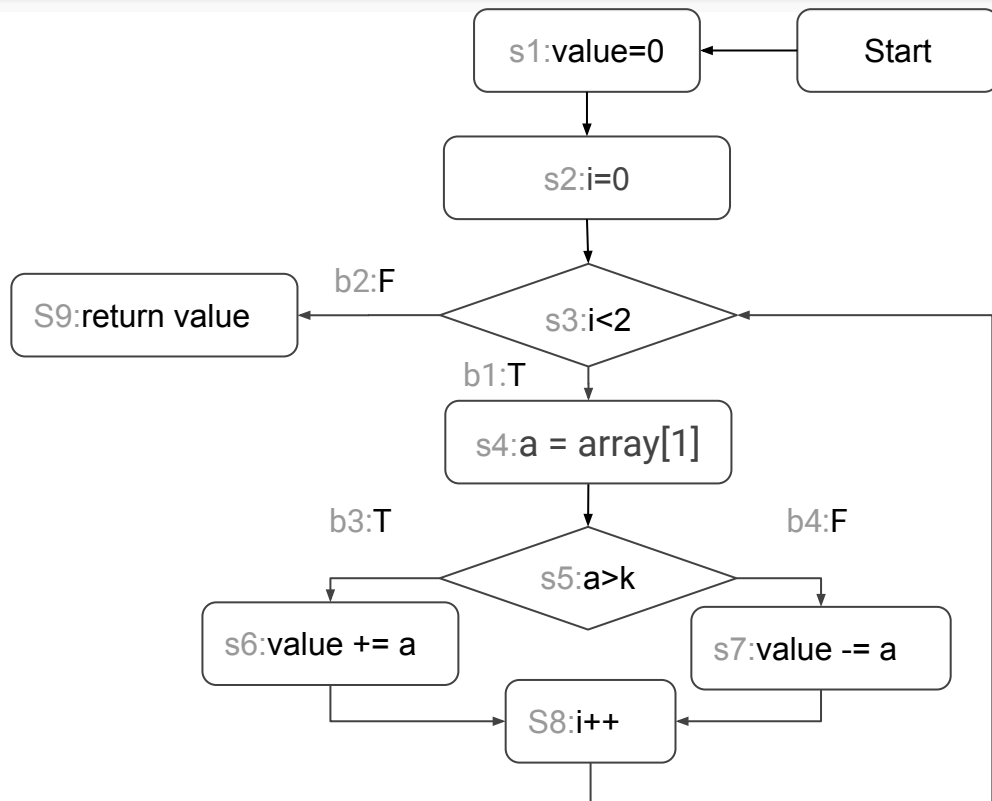
```
public static int complexfun(int array[], int k) {  
    int value = 0;  
    for (int i=0; i<2; i++) {  
        int a = array[i];  
        If (a > k) {  
            value = value+a;  
        } else {  
            value = value-a;  
        }  
    }  
    return value;  
}
```

```
@Test public void testComplexfun() {  
    int a[] = {3, 5, 7};  
    assertEquals(complexfun(a, 10), -8); // T1  
    int b[] = {5, 6, 9, 11, 15};  
    assertEquals(complexfun(b, 4), 11); // T2  
    int c[] = {7, 2, 1, 2, 5, 6};  
    assertEquals(complexfun(c, 4), 5); // T3  
}
```



# Draw CFG

```
public static int complexfun(int array[], int k) {  
    int value = 0;  
    for (int i=0; i<2; i++) {  
        int a = array[i];  
        If (a > k) {  
            value = value+a;  
        } else {  
            value = value-a;  
        }  
    }  
    return value;  
}
```



# Unroll Loop

```
public static int complexfun(int array[], int k) {  
    int value = 0;  
    for (int i=0; i<2; i++) { // bounded loop  
        int a = array[i];  
        If (a > k) {  
            value += a;  
        } else {  
            value -= a;  
        }  
    }  
    return value;  
}
```

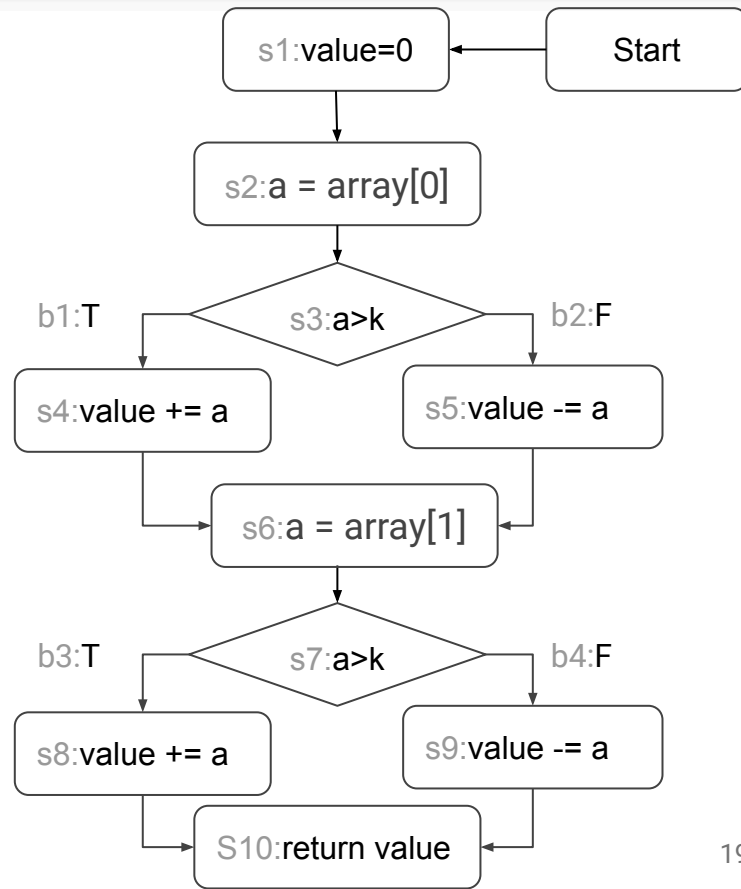
Loop Unrolling ==>

```
public static int complexfun(int array[], int k) {  
    int value = 0;  
    int a = array[0]; // first iteration  
    If (a > k) {  
        value += a;  
    } else {  
        value -= a;  
    }  
    a = array[1]; // second iteration  
    If (a > k) {  
        value += a;  
    } else {  
        value -= a;  
    }  
    return value;  
}
```

# Draw CFG of Loop Unrolled Version

```
public static int complexfun(int array[], int k) {  
    int value = 0;  
    int a = array[0]; // first iteration  
    If (a > k) {  
        value += a;  
    } else {  
        value -= a;  
    }  
    a = array[1]; // second iteration  
    If (a > k) {  
        value += a;  
    } else {  
        value -= a;  
    }  
    return value;  
}
```

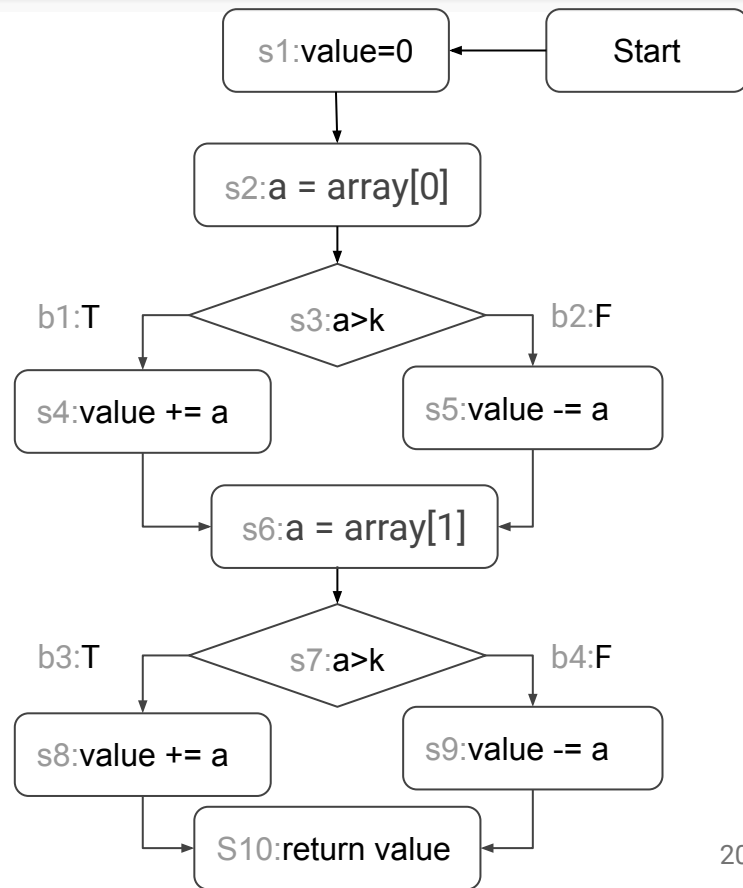
2 decisions that may take **T** or **F**  $\Rightarrow 2^2 = 4$  paths



# Calculate Coverage Criteria

```
@Test public void testComplexfun() {  
    int a[] = {3, 5, 7};  
    assertEquals(XXX.complexfun(a, 10), -8); // T1  
    int b[] = {5, 6, 9, 11, 15};  
    assertEquals(XXX.complexfun(b, 4), 11); // T2  
    int c[] = {7, 2, 1, 2, 5, 6};  
    assertEquals(XXX.complexfun(c, 4), 5); // T3  
}
```

Input	Exercised Statements	Exercised Branches	Exercised Paths
T1	s1,s2,s3,s5,s6,s7,s9,s10	b2, b4	[b2,b4]
Coverage	80%	50%	25%
T2	s1,s2,s3,s4,s6,s7,s8,s10	b1, b3	[b1,b3]
Coverage	100%	100%	50%
T3	s1,s2,s3,s4,s6,s7,s9,s10	b1, b4	[b1,b4]
Coverage	100%	100%	75%



# Example 2

- What is the number of decisions in the loop-unrolled program?
- What is the number of paths?

```
public static void fun2(int n) {  
    int sum = 0;  
    Random rand = new Random();  
    for (int i=1; i<=n; i++) {  
        for (int j=1; j<=Math.pow(3, i); j++) {  
            if (rand.nextInt() % 2 == 0)  
                sum++;  
        }  
        for (int k=1; k<=i; k++) {  
            if (Math.pow(2, k) % 2 == 0)  
                sum++;  
        }  
    }  
    System.out.println("n: "+n+"\tsum: "+sum);  
}
```

# About loop J's iteration

- When i is 1, the loop j executes  $3^1$  iterations
- When i is 2, the loop j executes  $3^2$  iterations
- ...
- When i is n, the loop j executes  $3^n$  iterations

- $T(n) = 3^1 + 3^2 + \dots + 3^n$   
 $3T(n) = 3^2 + \dots + 3^n + 3^{(n+1)}$

- Subtract the first from the second  
 $2T(n) = 3T(n) - T(n) = 3^{(n+1)} - 3^1$

- Divide the result by 2  
 $T(n) = (3^{(n+1)} - 3)/2$  iterations

```
public static void fun2(int n) {  
    int sum = 0;  
    Random rand = new Random();  
    for (int i=1; i<=n; i++) {  
        for (int j=1; j<=Math.pow(3, i); j++) {  
            if (rand.nextInt() % 2 == 0)  
                sum++;  
        }  
        for (int k=1; k<=i; k++) {  
            if (Math.pow(2, k) % 2 == 0)  
                sum++;  
        }  
    }  
    System.out.println("n: "+n+"\tsum: "+sum);  
}
```

# About loop K's iteration

- When i is 1, the loop k executes 1 iteration
  - When i is 2, the loop k executes 2 iterations
  - ...
  - When i is n, the loop k executes n iterations
- 
- $T(n) = 1 + 2 + \dots + n$  // sum from 1 to n
  - $T(n) = n(n+1)/2$  iterations

```
public static void fun2(int n) {  
    int sum = 0;  
    Random rand = new Random();  
    for (int i=1; i<=n; i++) {  
        for (int j=1; j<=Math.pow(3, i); j++) {  
            if (rand.nextInt() % 2 == 0)  
                sum++;  
        }  
        for (int k=1; k<=i; k++) {  
            if (Math.pow(2, k) % 2 == 0)  
                sum++;  
        }  
    }  
    System.out.println("n: "+n+"\tsum: "+sum);  
}
```

# Moreover

- Let's consider the decisions within the j and k loops
- **j loop decision:** `rand.nextInt()%2==0` can evaluate **true** or **false**, i.e., it is **nondeterministic**
- **k loop decision:** `Math.pow(2,k)%2==0` is always **true** because  $(2^k)\%2$  is always 0, i.e., it is **deterministic** regardless of inputs provided.
- Total number of nondeterministic decisions is therefore  $(3^{(n+1)} - 3)/2$
- Total number of paths is hence  $2^{\{(3^{(n+1)} - 3)/2\}}$  paths



# Extra point

- What if k loop decision was “`rand.nextInt()%2==0`” not “`Math.pow(2,k)%2==0`”?
- If so, the total number of iterations from loop J and K becomes:  
 $(3^{(n+1)} - 3)/2 + n(n+1)/2$ .
- The total number of paths is then  $2^{\{(3^{(n+1)} - 3)/2 + n(n+1)/2\}}$

# Example 3

- What is the number of decisions in the loop-unrolled program?
- What is the number of paths?

```
int sum = 0;
for (int i = 0; i < n; i++) {
    for (int j = 1; j <= Math.pow(2,i); j++) {
        if (a[i]<k)
            sum++;
    }
    for (int m=1; m<=i; m++) {
        if (pow(2,m) % 2 == 1)
            sum++;
        else
            sum--;
    }
}
```

# Answer

- For the **m** loop, the decision (i.e.,  $\text{pow}(2,m)\%2$ ) always evaluates to **false** for every possible input. So the decision is **deterministic**, hence does not contribute to increasing the number of paths.

- For the **j** loop  
When  $i=0$ , the inner **j** loop iterates  $2^0$   
When  $i=1$ , the inner **j** loop iterates  $2^1$   
...  
When  $i=n-1$ , the inner **j** loop iterates  $2^{(n-1)}$

```
int sum = 0;
for (int i = 0; i < n; i++) {
    for (int j = 1; j <= Math.pow(2,i); j++) {
        if (a[i]<k)
            sum++;
    }
    for (int m=1; m<=i; m++) {
        if (pow(2,m) % 2 == 1)
            sum++;
        else
            sum--;
    }
}
```

# Answer (cont'd)

- $T(n) = 2^0 + 2^1 + \dots + 2^{(n-1)}$
- Multiply  $T(n)$  by 2 on both sides of the equation
- $2T(n) = 2^1 + \dots + 2^{(n-1)} + 2^n$
- Subtract the first equation from the second,
- $T(n) = 2^n - 2^0$
- $T(n) = 2^n - 1$
  
- The decision  $(a[i] < k)$  could evaluate to **true** for some input and **false** for some other input, however it evaluates to the same value within each  $i$ .
- So the total number of paths is  $2^n$  not  $2^{(2^n - 1)}$ .

# Exercise (at home)

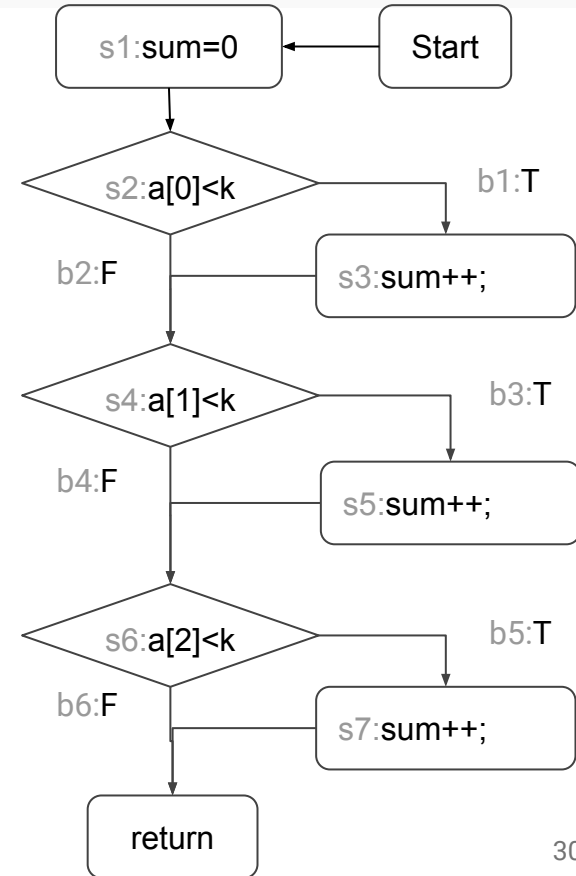
1. In example 3, assume that  $n=3$ . For a test suite with two cases  $T1=(k=2, a[]=\{4,3,5,4\})$  and  $T2=(k=1, a[]=\{2,7,5,10\})$ . What is the cumulative path coverage of the test suite? Your answer must include the total number of feasible paths (in other words express it as a ratio: path/total-paths).
2. In example 3, assume that  $n=3$ . For a test suite with two cases  $T1=(k=2, a[]=\{2,3,1\})$  and  $T2=(k=3, a[]=\{2,3,1\})$ . What is the cumulative path coverage of the test suite? Your answer must include the total number of feasible paths (in other words express it as a ratio: path/total-paths).

# Exercise (at home) answer

1. The CFG on the right is the one for the function after loop unrolling and ignoring the deterministic conditions.

- $T1=(k=2, a[]=\{4,3,5,4\})$   
paths: [b2, b4, b6]
- $T2=(k=1, a[]=\{2,7,5,10\})$   
paths: [b2, b4, b6]

Test suite cumulative path coverage =  $1/8$

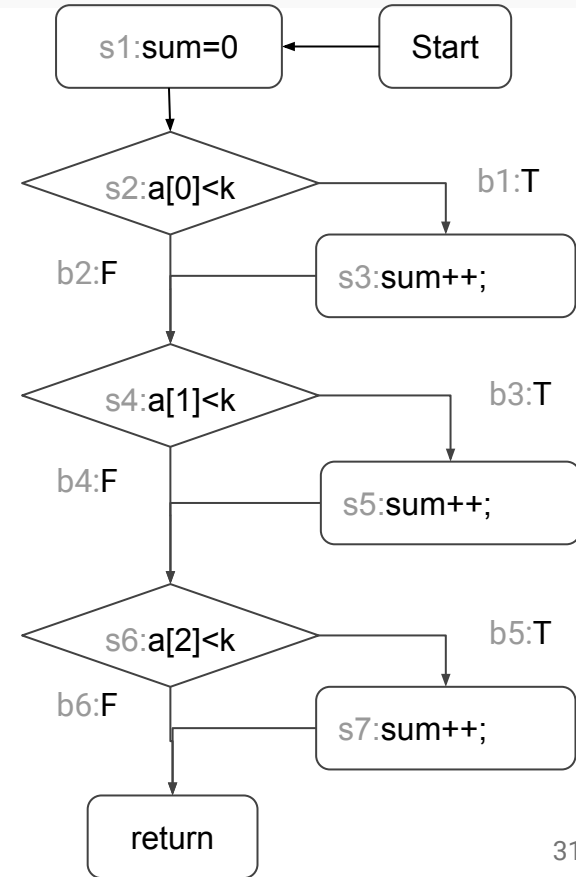


# Exercise (at home) answer

2. The CFG on the right is the one for the function after loop unrolling and ignoring the deterministic conditions.

- $T1=(k=2, a[]=\{2,3,1\})$   
paths: [b2, b4, b5]
- $T2=(k=3, a[]=\{2,3,1\})$   
paths: [b1, b4, b5]

Test suite cumulative path coverage = 2/8



# Software Testing 2 Quiz



# References

- Jorgensen, P.: “Software Testing, A Craftsman’s Approach,” CRC Press, 2013.
- Myers, G.: “The Art of Software testing,” John Wiley & Sons, 2004.
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- Buffoni, L.: “TDDD04: Software Testing”, Linkoping University, 2019.