

**Solutions to Questions - Chapter 6**  
**Mortgages: Additional Concepts, Analysis, and Applications**

**Question 6-1**

*What are the primary considerations that should be made when refinancing?*

The borrower must determine whether the present value of the savings in monthly payments is greater than the refinancing costs (points, origination fees, costs of (1) appraisal, (2) credit reports, (3) survey, (4) title insurance, (5) closing fees, etc.

**Question 6-2**

*What factors must be considered when deciding whether to refinance a loan after interest rates have declined?*

The payment savings resulting from the lower interest rate must be weighed against the costs associated with refinancing such as points on the new loan or prepayment penalties on the loan being refinanced.

**Question 6-3**

*Why might the market value of a loan differ from its outstanding principal balance?*

The remaining principal balance of a loan depends on the original contract interest rate, whereas the market value of the loan depends on the current market interest rate.

**Question 6-4**

*Why might a borrower be willing to pay a higher price for a home with an assumable loan?*

An assumable loan allows the borrower to save interest costs if the interest rate is lower than the current market interest rate. The investor may be willing to pay a higher price for the home if the additional price paid is less than the present value of the expected interest savings from the assumable loan.

**Question 6-5**

*What is a buydown loan? What parties are usually involved in this kind of loan?*

A buydown loan is a loan that has lower payments than a loan that would be made at the current interest rate. The payments are usually lowered for the first few years of the loan term. The payments are “bought down” by giving the lender funds in advance that equal the present value of the amount by which the payments have been reduced.

**Question 6-6**

*Why might a wraparound lender provide a wraparound loan at a lower rate than a new first mortgage?*

Although the wraparound loan is technically a “second mortgage,” the wraparound lender is only required to make payments on the existing mortgage if the borrower makes payments on the wraparound loan. Furthermore, the wraparound lender is typically taking over an existing mortgage that has a below market interest rate. Thus, the wraparound lender is benefiting from the spread between the rate being earned on the wraparound loan and that being paid on the existing loan. This allows the wraparound lender to earn a higher return on the incremental funds being advanced even if the rate on the wraparound loan is less than the rate on a new first mortgage.

**Question 6-7**

*Assuming the borrower is in no danger of default, under what conditions might a lender be willing to accept a lesser amount from a borrower than the outstanding balance of a loan and still consider the loan paid in full?*

If interest rates have risen significantly, the market value of the loan will be less. Thus, the lender may be willing to accept less than the outstanding balance of the loan, especially if the lender still receives more than the market value of the loan. The lender can then make a new loan at the higher market interest rate.

**Question 6-8**

*Under what conditions might a home with an assumable loan sell for more than comparable homes with no assumable loans available?*

The home with an assumable loan might be expected to sell for more than comparable homes with no assumable loans available when the contract interest rate on the assumable loan is significantly less than the current market rate on a loan with similar maturity and similar loan-to-value ratio. Note that if the dollar amount of the assumable loan is significantly less than that which could be obtained with a market rate loan, the benefit of the assumable loan is diminished because the borrower may need to make up the difference with a second mortgage.

### Question 6-9

*What is meant by the incremental cost of borrowing additional funds?*

The incremental cost of borrowing funds is a measure of what it really costs to obtain additional funds by getting a loan with a higher loan-to-value ratio that has a higher interest rate. This measure is important because the contract interest rate on the loan with the higher loan-to-value ratio does not take into consideration the fact that this higher rate must be paid on the entire loan - not just the additional funds borrowed. Thus, the borrower should consider the incremental cost of the additional funds to know what it is really costing to borrow the additional funds.

### Question 6-10

*Is the incremental cost of borrowing additional funds affected significantly by early repayment of the loan?*

The incremental cost of borrowing additional funds can be affected significantly by early repayment of the loan, especially if additional points were paid to obtain the additional funds. Thus, the borrower should consider how long he or she expects to have the loan when calculating the incremental cost of the additional funds.

## Solutions to Problems - Chapter 6

### Residential Financial Analysis

#### INTRODUCTION

The following solutions were obtained using an HP 12C financial calculator. Answers may differ slightly due to rounding or use of the financial tables to approximate the answers. As pointed out in the chapter, there is often more than one way of approaching the solution to the problems in this chapter. Thus "alternative solutions" are shown where appropriate.

#### Problem 6-1

(a)

Because the amount of the loan does not matter in this case, it is easiest to assume some arbitrary dollar amount that is easy to work with. Therefore we will assume that the purchase price of the home is \$100,000. Thus the choice is between an 80 percent loan for \$80,000 or a 90 percent loan for \$90,000. The loan information and calculated payments are as follows:

<u>Alternative</u>	<u>Interest Rate</u>	<u>Loan Term</u>	<u>Loan Amount</u>	<u>Monthly Payments</u>
90% Loan	8.5%	25 yrs.	\$90,000	\$724.70
80% Loan	8.0%	25 yrs.	<u>80,000</u>	<u>617.45</u>
Difference			\$10,000	\$107.25

i(n,PV,PMT,FV)

n	=	25x12 or 300
PMT	=	\$107.25
PV	=	-\$10,000
FV	=	0

Solve for the *annual* interest rate:

i	=	12.26%
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Solving for the interest rate with a financial calculator we obtain an incremental borrowing cost of 12.3 percent. (Note: Be sure to solve for the interest rate assuming *monthly* payments. With an HP12C you will first solve for the monthly interest rate, then multiply the monthly rate by 12 to obtain the nominal annual rate.)

(b)

<u>Alternative</u>	<u>Loan Amount</u>	<u>Points</u>	<u>Net Proceeds</u>	<u>Monthly Payments</u>
90% Loan	\$90,000	\$1,800	\$88,200	\$724.70
80% Loan	<u>80,000</u>	<u>0</u>	<u>80,000</u>	<u>617.45</u>
Difference			\$8,200	\$107.25

$$\$107.25 \times (\text{MPVIFA}, \%, 25 \text{ yrs.}) = \$8,200$$

I (n, PV, PMT, FV)

$$\begin{aligned}
 n &= 25 \times 12 \text{ or } 300 \\
 PMT &= \$107.25 \\
 PV &= -\$8,200 \\
 FV &= 0
 \end{aligned}$$

Solve for the *annual* interest rate:

$$i = 15.35\%$$

Solving for the interest rate with a financial calculator we now obtain an incremental borrowing cost of 15.35 percent.

(c)

We now need the loan balance after 5 years.

<u>Alternative</u>	<u>Loan Amount</u>	<u>Monthly Payments</u>	<u>Loan Balance</u>
90% Loan	\$90,000	\$724.70	\$83,508.62
80% Loan	<u>80,000</u>	<u>617.45</u>	<u>73,819.37</u>
Difference	\$10,000	\$107.25	\$9,689.37

Note that the net proceeds of the loan is still \$8,200 as in Part b. Thus we have:

I (n, PV, PMT, FV)

$$\begin{aligned}
 n &= 25 \times 12 \text{ or } 300 \\
 PMT &= \$107.25 \\
 PV &= -\$8,200 \\
 FV &= \$9,689.37
 \end{aligned}$$

Solve for the *annual* interest rate:

$$i = 17.96\%$$

Solving for the interest rate with a financial calculator we now obtain an incremental borrowing cost of 17.96 percent.

### **Problem 6-2**

(a)

For this problem we need to know the effective cost of the \$180,000 loan at 9% combined with the \$40,000 loan at 13%

	<u>Loan Amount</u>	<u>Interest Rate</u>	<u>Loan Term</u>	<u>Monthly Payments</u>
	\$180,000	9%	20 yrs..	\$1619.51
	<u>40,000</u>	13%	20 yrs..	<u>468.63</u>
Combined	\$220,000			\$2,088.14

I (n, PV, PMT, FV)

$$\begin{aligned}
 n &= 240 \\
 PMT &= \$2,088.14 \\
 PV &= -\$220,000 \\
 FV &= \$0
 \end{aligned}$$

Solve for the *annual* interest rate:

$$i = 9.76\%$$

Solving for the effective cost of the combined loans we obtain 9.76%. This is greater than the 9.5% rate on the single \$220,000 loan. Thus the \$220,000 loan is preferable.

(b) **REV**

We now need the loan balance after 5 years

	<u>Loan Amount</u>	<u>Interest Rate</u>	<u>Loan Term</u>	<u>Monthly Payments</u>	<u>Loan Balance</u>
	\$180,000	9%	20 yrs..	\$1619.51	\$159,672.44
	<u>40,000</u>	13%	20 yrs..	<u>468.63</u>	<u>37,038.81</u>
Combined	\$220,000			\$2,088.14	<b>\$196,711.25</b>

i (n, PV, PMT, FV)

n = 60  
 PMT = \$2,088.14  
 PV = -\$220,000  
 FV = \$196,711.25  
 Solve for the *annual* interest rate:  
 i = 9.74%

Solving for the interest rate, which represents the combined cost, we obtain 9.74%. The effective cost of the single \$220,000 would still be 9.5% even if it is repaid after 5 years because there were no points or prepayment penalties. Thus the \$220,000 loan is still better.

(c)

Assuming the loan is held for the full term (to compare with Part a:)

	<u>Loan Amount</u>	<u>Interest Rate</u>	<u>Loan Term</u>	<u>Monthly Payments</u>
	\$180,000	9%	20 yrs..	\$1619.51
	<u>40,000</u>	13%	10 yrs..	<u>597.24</u>
Combined	\$220,000			\$2,216.75

The combined payments are made for the *first 10 years* only. After that, only the payment on the \$180,000 loan is made.

(c) **IRR (CF1, CF2, ....CFn)**

<b>CF<sub>j</sub></b>	<b>n<sub>j</sub></b>
-\$220,000.00	
2,216.75	n = 12
2,216.75	n = 12
2,216.75	n = 12
2,216.75	n = 12
2,216.75	n = 12
2,216.75	n = 12
2,216.75	n = 12
2,216.75	n = 12
2,216.75	n = 12
2,216.75	n = 12
1,619.51	n = 12
1,619.51	n = 12
1,619.51	n = 12
1,619.51	n = 12
1,619.51	n = 12
1,619.51	n = 12
1,619.51	n = 12
1,619.51	n = 12
1,619.51	n = 12
1,619.51	n = 12
1,619.51	n = 12

Solve for the IRR: = 0.79% x 12 = 9.49% (annual rate, compounded monthly)

Note that the payment of \$1,619.51 is first discounted as a 10 year annuity (years 11 to 20) and further discounted as a lump sum for 10 years to recognize the fact that the annuity does not start until year 10. When calculating the IRR in excel input the monthly payment (annuity) in each cell for each period as opposed to one lump annual payment amount.

Solving for the cost we obtain 9.49%. This is less than 9.5% rate for the single \$220,000 loan. Thus, the combined loans are preferred.

Assuming the loan is held for 5 years (to compare with Part b):

We now need the loan balance after 5 years.

	<u>Loan Amount</u>	<u>Interest Rate</u>	<u>Loan Term</u>	<u>Monthly Payments</u>	<u>Loan Balance</u>
	\$180,000	9%	20 yrs..	\$1619.51	\$159,672.68
	<u>40,000</u>	13%	10 yrs..	597.24	<u>26,248.89</u>
Combined	\$220,000			\$2,216.75	\$185,921.57

i (n, PV, PMT, FV)

n	=	60
PMT	=	\$2,216.75
PV	=	-\$220,000
FV	=	\$185,921.57
Solve for the <i>annual</i> interest rate:		
i	=	9.67%

We now obtain 9.67%. This is greater than the 9.5% rate for a single loan.

### **Problem 6-3**

Preliminary calculation:

The existing loan is for \$95,000 at a 11% interest rate for 30 years (monthly payments). The monthly payment is \$904.71. The balance of the loan after 5 years is \$92,306.41.

Payment on a new loan for \$92,306.41 at a 10% rate with a 25 year term are \$838.79.

(a)

<u>Alternative</u>	<u>Interest Rate</u>	<u>Loan Term</u>	<u>Loan Amount</u>	<u>Monthly Payments</u>
Old loan	11%	30 yrs..	\$95,000	\$904.71
New loan	<u>10%</u>	25 yrs..	92,306	<u>838.79</u>
Savings				\$65.92

Cost of refinancing are  $\$2,000 + (.03 \times \$92,306.41) = \$4,769.19$ . Considering the \$4,769.19 as an “investment” necessary to take advantage of the lower payments resulting from refinancing

I (n, PV, PMT, FV)

n	=	300
PMT	=	\$65.92
PV	=	-\$4,769.19
FV	=	\$0
Solve for the <i>annual</i> interest rate:		
i	=	16.30%

Solving for the rate we obtain 16.30%. It is desirable to refinance if the investor can not get a higher yield than 16.30% on alternative investments.

### **Alternate solution:**

Amount of new loan	\$92,306.00
Cost of refinancing	<u>\$4,769.19</u>
Net proceeds	\$87,536.81

The net proceeds can be compared with the payment on the new loan to obtain an effective cost of the new loan. We have:

i (n, PV, PMT, FV)

n	=	300
PMT	=	\$838.79
PV	=	-\$87,536.81

$$\begin{aligned} \text{FV} &= \$0 \\ \text{Solve for the } \textit{annual} \text{ interest rate:} \\ i &= 10.70\% \end{aligned}$$

Solving for the effective cost we obtain 10.70%. Because the effective cost is *less* than the cost of the existing loan (11%) the conclusion is to refinance.

(b)

For a 5-year holding period we must also consider the balance of the old and new loan after 5 years. We have:

<u>Alternative</u>	<u>Loan Amount</u>	<u>Interest Rate</u>	<u>Loan Term</u>	<u>Monthly Payments</u>	<u>Loan Balance</u>
Old loan	\$95,000	11%	30 yrs..	\$904.71	\$87,648.82*
New loan	92,306	10%	25 yrs..	<u>838.79</u>	<u>86,918.44</u>
				65.92	\$730.38

\* Balance after 5 *additional* years or 10 years total.

Looking at the refinancing cash outflows as an investment we have:

i (n, PV, PMT, FV)

$$\begin{aligned} n &= 60 \\ \text{PMT} &= \$65.92 \\ \text{PV} &= -\$4,769.19 \\ \text{FV} &= \$730.38 \\ \text{Solve for the } \textit{annual} \text{ interest rate:} \\ i &= -0.60\% \end{aligned}$$

Solving for the IRR we obtain -0.60%.

The negative return tells you this is a *bad investment* if the new loan is paid off so quickly. The reason for the negative return, is that you pay for the refinancing up-front, but do not benefit from the lower monthly payments on the new financing for a period of time long enough to cover and/or justify the cost of refinancing.

#### **Alternative solution:**

The effective cost is now as follows:

i(n,PV,PMT,FV)

$$\begin{aligned} n &= 60 \\ \text{PMT} &= \$838.79 \\ \text{PV} &= -\$87,536.81 \\ \text{FV} &= \$86,918.44 \\ \text{Solve for the } \textit{annual} \text{ interest rate:} \\ i &= 11.39\% \end{aligned}$$

Solving for the effective cost we obtain 11.39%. The effective cost is now higher than the rate of return on the old loan (11%) so refinancing is not desirable.

#### **Problem 6-4**

Payments on the \$140,000 loan at 10%, 30 years are \$1,228.60 per month.

(a)

Note that there are 25 years remaining.

The balance after 5 years can be found by discounting the remaining payments as follows:

PV (n, i, PMT, FV)

n = 300  
PMT = \$1,228.60  
i = 10%  
FV = \$0

Solve for the *annual* interest rate:

PV = \$135,204.03

The market value of the loan can be found by discounting the payments of \$1,228.60 for 25 years (monthly) using the required rate of 11%. We have:

PV (n, i, PMT, FV)

n = 300  
PMT = \$1,228.60  
i = 11%/12  
FV = \$0

Solve for the *annual* interest rate:

PV = \$125,352.88

This is *lower* than the balance of the loan because payments are discounted at a higher rate than the contract rate on the loan.

(b)

The balance of the original loan after five *additional* years (10 years from origination) is \$127,313.21.

To calculate the market value assuming the loan is repaid after 5 additional years, we have:

PV (n, i, PMT, FV)

n = 300  
PMT = \$1,228.60  
i = 11%  
FV = \$127,313.21

Solve for the *annual* interest rate:

PV = \$130,144.64

### **Problem 6-5**

(a)

Alternative 1: Purchase of \$150,000 home:

	<u>Interest Rate</u>	<u>Loan Term</u>	<u>Loan Amount</u>	<u>Monthly Payments</u>
First mortgage	10.5%	20 yrs..	\$120,000	\$1,198.06

or

Alternative 2: Purchase of \$160,000 home:

	<u>Interest Rate</u>	<u>Loan Term</u>	<u>Loan Amount</u>	<u>Monthly Payments</u>
Assumption	9%	20 yrs..	\$100,000	\$899.73
Second mortgage	13%	20 yrs..	<u>20,000</u>	<u>234.32</u>
			\$120,000	\$1,134.05

The loan amounts are the same under the two alternatives. The second alternative has lower total payments resulting in savings of \$64.01 per month (\$1,198.06 - \$1,134.05), but requires an additional \$10,000 cash outflow as an additional down payment.

i (n, PV, PMT, FV)

n = 240  
PMT = \$64.01  
PV = -\$10,000

$$\begin{array}{rcl} \text{FV} & = & \$0 \\ \text{Solve for the } \textit{annual} \text{ interest rate:} & & \\ i & = & 4.64\% \end{array}$$

The IRR is 4.64%. This does not make sense if the investor can earn more than this on the \$10,000. This appears to be too low to justify the additional \$10,000 equity - especially with mortgage interest rates at 10.5%. Note that the borrower could take the \$150,000 home and use the extra \$10,000 to borrow less money, e.g. \$110,000 instead of \$120,000 which results in interest savings of 10.5% (the rate on the loan).

The point is that the investor's opportunity cost is 10.5%, which is higher than the 4.64% that would be earned by taking the second alternative.

**Note to instructors:**

It is informative to calculate exactly how much more the borrower could pay for alternative 2. This is found by discounting the payment savings at 10.5%. We have:

$$\begin{array}{rcl} \text{PV (n, i, PMT, FV)} & & \\ n & = & 240 \\ \text{PMT} & = & \$64.01 \\ i & = & 10.50\%/12 \\ \text{FV} & = & \$0 \\ \text{Solve for the } \textit{annual} \text{ interest rate:} & & \\ \text{PV} & = & \$6,411.39 \end{array}$$

Thus, the borrower would be indifferent between alternative 1 and 2 if the price of the home for alternative 2 was \$156,411.

(b)

With the homeowner providing the second mortgage for the additional \$20,000 at 9% (purchase money mortgage) we have:

Alternative 2: Purchase of \$160,000 home:

	<u>Interest Rate</u>	<u>Loan Term</u>	<u>Loan Amount</u>	<u>Monthly Payments</u>
Assumption	9%	20 yrs..	\$100,000	\$899.73
Second mortgage	9%	20 yrs..	<u>20,000</u>	<u>179.95</u>
			\$120,000	\$1,079.68

Savings are now \$1,198.06 - \$1,079.68 = \$118.38 per month. An additional down payment of \$10,000 is still required.

The IRR is now 13.17%

(c)

Alternative 2: Purchase of \$160,000 home:

	<u>Interest Rate</u>	<u>Loan Term</u>	<u>Loan Amount</u>	<u>Monthly Payments</u>
Assumption	9%	20 yrs..	\$100,000	\$899.73
Second mortgage	9%	20 yrs..	<u>30,000</u>	<u>269.92</u>
			\$130,000	\$1,169.65

The savings are now \$1,198.06 - \$1,169.65 or \$28.41 per month. Because of the additional amount of the second mortgage, there is no additional down payment even though \$10,000 more is paid for the home. Thus, the borrower saves \$28.41 under alternative 2 with no additional cash outlay- which is clearly desirable.

**Problem 6-6**

<u>Loan</u>	<u>Amount</u>	<u>Payment</u>	<u>Term</u>
Wraparound	\$150,000	\$1,800.25	15 yrs.
Existing	<u>100,000</u>	<u>1,100.25</u>	15 yrs. (remaining)
Difference	\$50,000	\$700.25	



$$\$700.25 \times (\text{MPVIFA}, 7\%, 15 \text{ yrs.}) = \$50,000$$

i (n, PV, PMT, FV)

$$\begin{array}{rcl} n & = & 180 \\ \text{PMT} & = & \$700.25 \\ \text{PV} & = & -\$50,000 \\ \text{FV} & = & \$0 \end{array}$$

Solve for the *annual* interest rate:

$$i = 15.01\%$$

Solving for the IRR we obtain 15.01%. This is the incremental return on the wraparound. Because this is greater than the 14% rate on a second mortgage, the second mortgage is better.

**Alternative solution:**

<u>Loan</u>	<u>Amount</u>	<u>Payment</u>	<u>Term</u>
Second mortgage	\$50,000	\$665.87	15 yrs.
<u>Existing loan</u>	<u>100,000</u>	<u>1,100.00</u>	15 yrs. (remaining)
Total	\$150,000	\$1765.87	

The total payments on the existing loan plus a second mortgage is \$1,765.87, which is less than the payments on the wraparound. Furthermore, the effective cost of the combined loans is as follows:

i (n, PV, PMT, FV)

$$\begin{array}{rcl} n & = & 180 \\ \text{PMT} & = & \$1,765.87 \\ \text{PV} & = & -\$150,000 \\ \text{FV} & = & \$0 \end{array}$$

Solve for the *annual* interest rate:

$$i = 11.64\%$$

The IRR is 11.64%. Thus, the effective cost of the combined loans is less than the wraparound.

Thus, the combined loans are better. Note: we can only compare payments when the loan terms are the same. However, we can compare effective costs when they differ. As a result, the effective cost is more general than simply comparing payments.

**Problem 6-7**

(a)

Payments on a \$100,000 loan at 9% for 25 years is \$839.20.

The present value of \$839.20 at 9.5% for 25 years is \$96,051.64.

The difference between the contract loan amount (\$100,000) and the value of the loan (\$96,051.64) is \$3,948. This must be added on to the home price. Thus, the home would have to be sold for \$110,000 + \$3,948 or \$113,948.

**Alternative solution:**

Payments on a loan for \$100,000 at 9.5%:	\$873.70
Payments on a loan for \$100,000 at 9%:	<u>839.20</u>
Savings by getting the loan at 9%:	\$34.50

Present value of the saving discounted at 9.5%:

PV (n, i, PMT, FV)

$$\begin{array}{rcl} n & = & 300 \\ \text{PMT} & = & \$34.50 \end{array}$$

$$\begin{aligned}
 i &= 9.50\% \\
 FV &= \$0 \\
 \text{Solve for the } \textit{annual} \text{ interest rate:} \\
 PV &= \$3,948
 \end{aligned}$$

This is the amount that has to be added to the home as before.

(b)

The balance of the \$100,000 loan (9%, 25 yrs.) after 10 years is \$82,739.23. We now discount the payments on the \$100,000 loan which are \$839.20 and the balance after 10 years which is 82,739.23. Both are discounted at the market rate of 9.5%.

We have:

$$\begin{aligned}
 &PV(n, i, PMT, FV) \\
 n &= 300 \\
 PMT &= \$839.20 \\
 i &= 9.50\% \\
 FV &= \$82,739.23 \\
 \text{Solve for the } \textit{annual} \text{ interest rate:} \\
 PV &= \$96,973
 \end{aligned}$$

Subtracting this from the loan amount of \$100,000 we have \$100,000 - \$96,973.69 or \$3,027. This is the amount that must be added to the home price. Thus, the home price must be \$110,000 + \$3,027 or \$113,027. Not as much has to be added relative to (a) because the borrower would not have to be given the interest savings for as many years.

#### Alternative solution:

The difference in payments for a \$100,000 loan at 9% and \$100,000 at 9.5% is \$34.50 (same as alternative solution to part a.) We must also consider the difference in loan balances after 10 years.

Balance of \$100,000 loan at 9.5% after 10 years:	\$83,668.75
Balance of \$100,000 loan at 9% after 10 years:	<u>82,739.23</u>
Savings	\$929.52

We now discount the payment savings and the savings after 10 years.

$$\begin{aligned}
 &PV(n, i, PMT, FV) \\
 n &= 120 \\
 PMT &= \$34.50 \\
 i &= 9.50\% \\
 FV &= \$929.52 \\
 \text{Solve for the } \textit{annual} \text{ interest rate:} \\
 PV &= \$3,027
 \end{aligned}$$

Thus \$3,027 must be added to the home price as above.

#### Problem 6-8

(a)

Monthly payment reduction during the first year (50% of \$726.96):  
 Monthly payment reduction during the second year (25% of \$726.96):  
 Discounting the payment reduction at 10% per annum (10%/12 per month)

	Amount of Reduction	Payment will be	Months
Monthly payment reduction during the first year (50% of \$726.96):	\$363.48	\$363.48	12
Monthly payment reduction during the second year (25% of \$726.96):	\$181.74	\$545.22	12
Discounting the payment reduction at 10% per annum (10%/12 per month)	-	\$726.96	276

Solve for PV of all future monthly payments:

$$\begin{aligned}
 &PV(n, i, PMT, FV) \\
 CF_j &= 363.48 \\
 n_j &= 12 \\
 CF_j &= 181.74 \\
 n_j &= 12 \\
 \text{Discount at } i &= 10\% \div 12 \\
 \text{And find PV} &= \$6005.66
 \end{aligned}$$

Note that the second year payment reduction is an annuity that starts after one year i.e. period 13.

Thus, the builder would have to give the bank \$6,005.66 up front.

(b)

Based on the results from (a), the buydown loan is worth \$6,005.66 in present value terms. We would expect the home to sell for \$6,005.66 more than a comparable home that did not have this loan available. Thus, if the home could be purchased for \$5,000 more, the borrower would gain in present value terms by \$6,006 - \$5,000 or \$1,006.

### Problem 6-9

(a) Step 1, Calculate the dollar monthly difference between the two financing options.

Original loan payment:

$$\begin{array}{lll} \text{PV} & = & -\$140,000 \\ i & = & 7/12 \text{ or } 0.58 \\ n & = & 15 \times 12 \text{ or } 180 \\ \text{FV} & = & 0 \end{array}$$

Solve for the payment:

$$\text{PMT} = \$1,258.36$$

Find present value of the payments at the market rate of 8%

$$\begin{array}{lll} i & = & 8\%/12 \\ n & = & 15 \times 12 \text{ or } 180 \\ \text{FV} & = & 0 \\ \text{PMT} & = & \$1,258.36 \end{array}$$

Solve for PV:

$$\text{PV} = \$131,675.49$$

This is the market (cash equivalent) value of the loan.

The buyer made a cash down payment of \$60,000.

Cash equivalent value of loan	\$131,675.49
Cash down payment	<u>60,000.00</u>
Cash equivalent value of property	\$191,675.49

(b) If it is assumed that the buyer only expected to benefit from the favorable financing for five years:

Loan balance after 5 years is \$108,378

Find present value of payments for 5 years and loan balance at the end of the 5<sup>th</sup> year.

$$\begin{array}{lll} i & = & 8\%/12 \\ n & = & 5 \times 12 \text{ or } 60 \\ \text{FV} & = & \$108,378 \\ \text{PMT} & = & \$1,258.36 \end{array}$$

Solve for PV:

$$\text{PV} = \$134,804.72$$

Cash equivalent value of loan	\$134,804.72
Cash down payment	<u>60,000.00</u>
Cash equivalent value of property	\$194,804.72

The cash equivalent value is higher because the buyer was not assumed to have discounted the loan by as much.

### Problem 6-10

Question: A borrower is making a choice between a mortgage with monthly payment or bi-weekly payments; the loan will be \$200,000@6% interest for 20 years.

A) How would you analyze these alternatives?

B) What if the bi-weekly loan was available for 5.75%? How would your answer change?

A. Calculate Monthly Payments:

$$PV = <\$200,000>$$

$$FV = 0$$

$$n = 240 \text{ (12*20)}$$

$$i = 6\%$$

$$\text{Solve: PMT} = \$1,432.86$$

B. Calculate Bi-Weekly Payments:  $\$1,432.86 \div 2 = \$716.43$ .

Remember: bi-weekly payments total 26 per year

C. Calculate maturity period:

$$PV = <\$200,000>$$

$$FV = 0$$

$$i = 6\% \div 12$$

$$\text{PMT} = \$716.43 \text{ (1432.86/2)}$$

$$\text{Solve: } n = 17.3 \text{ years (449 payments / 26 payments per year)}$$

D. Compare Total Payments:

$$\$1,432.86 * 240 = \$343,866.40$$

$$\$716.43 * 449 = \$321,677.07$$

- Bi-weekly payments would be less costly by \$22,209.33 ( $343,886.40 - 321,977.07$ ).

E. Recalculate the above based on 5.75% interest:

$$PV = <\$200,000>$$

$$FV = - 0$$

$$i = 5.75\% \div 12$$

$$\text{PMT} = 716.43$$

$$n = ?? \rightarrow 16.73 \text{ years (435 payments / 26 payments per year)}$$

$$\$1,432.86 * 240 = \$343,886.40$$

$$\$716.43 * 435 = \$311,647.05$$

Conclusion: Bi-weekly payments would be even less costly by \$32,239.35 ( $343,886.40 - 311,647.05$ ).