1

Assignment 1

A.Tejasri

Download all python codes from

https://github.com/teja3657/Assignment1/tree/ master/CODES

and latex-tikz codes from

https://github.com/teja3657/Assignment1/blob/ master/Assignment1.tex

1 Question No.2.16

Construct an isosceles triangle in which the lengths of the equal sides is 6.5 and the angle between them is 110°.

2 SOLUTION

The vertices are:

$$\mathbf{L} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{D} = \begin{pmatrix} ld \\ 0 \end{pmatrix}, \mathbf{O} = \begin{pmatrix} p1 \\ q1 \end{pmatrix}$$
 (2.0.1)

Finding $\angle O$ and $\angle D$ In $\triangle OLD$,

$$\angle O + \angle L + \angle D = 180^{\circ} \tag{2.0.2}$$

$$\angle O = \angle D = x \tag{2.0.3}$$

$$x + 110^{\circ} + x = 180^{\circ}$$
 (2.0.4)

$$2x = 180^{\circ} - 110^{\circ} \tag{2.0.5}$$

$$2x = 70^{\circ}$$
 (2.0.6)

$$x = 35^{\circ}$$
 (2.0.7)

$$\implies x = \angle O = \angle L = 35^{\circ}$$
 (2.0.8)

Now, Lines od, ol and ld Can be plotted.

$$\mathbf{OD} = 2a\cos(35) \tag{2.0.9}$$

$$(here, a = ol = 6.5)$$
 (2.0.10)

$$\mathbf{OD} = (13)\cos(35) = 10.6 \tag{2.0.11}$$

Coordinates of O(p1,q1)

$$\mathbf{p1} = \frac{ld^2 + ol^2 - od^2}{2(ld)}$$
 (2.0.12)

$$\mathbf{p1} = \frac{(6.5)^2 + (6.5)^2 - (10.6)^2}{2(6.5)}$$

$$\mathbf{p1} = \frac{42.25 + 42.25 - 112.36}{13}$$
(2.0.13)

$$\mathbf{p1} = \frac{42.25 + 42.25 - 112.36}{13} \tag{2.0.14}$$

$$\implies p1 = -2.14$$
 (2.0.15)

$$\mathbf{q1} = \sqrt{(ol)^2 - (p1)^2} \tag{2.0.16}$$

$$\mathbf{q1} = \sqrt{(6.5)^2 - (-2.14)^2} \tag{2.0.17}$$

$$\implies q1 = 6.13$$
 (2.0.18)

The vertex O can be expressed in polar coordinate form as

$$\mathbf{O} = ol \begin{pmatrix} \cos \theta \\ \sin \theta \end{pmatrix} \tag{2.0.19}$$

O can be expressed as

$$\mathbf{O} = ol \begin{pmatrix} cosO\\ sinO \end{pmatrix} \tag{2.0.20}$$

$$Here, ol = 6.5$$
 (2.0.21)

$$\mathbf{O} = 6.5 \begin{pmatrix} \cos 35 \\ \sin 35 \end{pmatrix} \tag{2.0.22}$$

$$\mathbf{O} = 6.5 \begin{pmatrix} 0.819 \\ 0.573 \end{pmatrix} \tag{2.0.23}$$

$$\mathbf{O} = \begin{pmatrix} 5.324 \\ 3.728 \end{pmatrix} \tag{2.0.24}$$

So, the vertices of $\triangle OLD$ are

$$\mathbf{L} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{D} = \begin{pmatrix} 6.5 \\ 0 \end{pmatrix}, \mathbf{O} = \begin{pmatrix} 5.324 \\ 3.728 \end{pmatrix} \tag{2.0.25}$$

Now, Isosceles $\triangle OLD$ can be plotted using vertices LD, OL and DO.

Plot of the Isosceles $\triangle OLD$ is required.

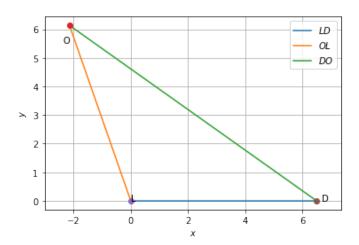


Fig. 2.1: Isosceles triangle $\triangle OLD$