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Assignment 1

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Download all python codes from

https://github.com/teja3657/Assignment1/tree/master/CODES

and latex-tikz codes from

https://github.com/teja3657/Assignment1/blob/ master/Assignment1.tex

1 Question No.2.16

Construct an isosceles triangle in which the lengths of the equal sides is 6.5 and the angle between them is 110° .

2 SOLUTION

The vertices are:

$$\mathbf{A} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} a \\ 0 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} p \\ q \end{pmatrix}$$
 (2.0.1)

In $\triangle ABC$,

$$\angle A + \angle B + \angle C = 180^{\circ} \quad (\because \angle B = \angle C) \quad (2.0.2)$$

$$\angle B = \angle C = 35^{\circ} \tag{2.0.3}$$

$$BC = 2(6.5)\cos(35)$$
 (2.0.4)

$$c = 10.64 \tag{2.0.5}$$

The vertex B can be expressed in polar coordinate form as

$$\mathbf{B} = c \begin{pmatrix} \cos A \\ \sin A \end{pmatrix} \tag{2.0.6}$$

From $\triangle ABC$, we use the law of cosines:

$$b^2 = c^2 + a^2 - 2ca\cos B \tag{2.0.7}$$

$$\cos B = \frac{c^2 + a^2 - b^2}{2ca} \tag{2.0.8}$$

$$\cos B = \frac{112.36}{137.8} \tag{2.0.9}$$

$$\cos B = 0.815 \tag{2.0.10}$$

$$\mathbf{B} = 35.412 \tag{2.0.11}$$

B can be expressed as

$$B = 10.6 \begin{pmatrix} -0.34202 \\ 0.93969 \end{pmatrix} \tag{2.0.12}$$

$$= \begin{pmatrix} -2.22313 \\ 6.10798 \end{pmatrix} \tag{2.0.13}$$

So, the vertices of $\triangle ABC$ are

$$\mathbf{A} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 6.5 \\ 0 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} -2.22313 \\ 6.10798 \end{pmatrix}$$
 (2.0.14)

Plot of the Isosceles $\triangle ABC$:

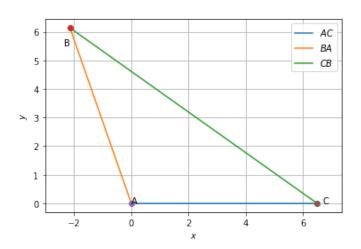


Fig. 2.1: Isosceles triangle $\triangle ABC$