# Assignment 12

# A.Tejasri

Download all python codes from

https://github.com/tejasri3657/Assignment-12/blob /main/Assignment 12(1).py

and latex-tikz codes from

https://github.com/tejasri3657/Assignment-12/new/ main

## 1 Question No. 2.5

A couple has two children,

- 1) Find the probability that both children are male, if it is known that at least one of the children is male.
- 2) Find the probability that both children are female, if it is known that at least one of the children is female.

### 2 Solution

**Lemma 2.1.** If A and B are two events in a sample space S, then the Conditional Probability of A given B is defined as  $P(A \mid B) = \frac{P(A \cap B)}{P(B)}$ 

From the given information we have,

Events	Description
<i>E</i> 1	Both children are male
<i>F</i> 1	At least one child is male
E2	Both children are female
F2	At least one child is female
$(E1 \cap F1)$	Both children are male
	and at least one child is male
$(E1 \cap F2)$	Both children are female and
	at least one child is female

Let boy be denoted by B and girl be denoted by G respectively.

$$S = \{BB, BG, GB, GG\}$$
 (2.0.1)

1) We need to find  $P = (E1 \mid F1)$ :

$$P(E1) = \frac{1}{4}, P(F1) = \frac{3}{4}$$
 (2.0.2)

$$P(E1 \cap F1) = \frac{1}{4}$$
 (2.0.3)  
 $\therefore P(E1|F2) = \frac{1}{3}$  (2.0.4)

$$\therefore P(E1|F2) = \frac{1}{3}$$
 (2.0.4)

2) We need to find  $P = (E2 \mid F2)$ :

$$P(E2) = \frac{1}{4}, P(F2) = \frac{1}{2}$$
 (2.0.5)

$$P(E2 \cap F2) = \frac{1}{4} \tag{2.0.6}$$

$$\therefore P(E2|F2) = \frac{1}{2}$$
 (2.0.7)