ASSIGNMENT 4

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Download all python codes from

https://github.com/tejasri3657/Assignment-4/blob/ main/Assignment-4.py

and latex-tikz codes from

https://github.com/tejasri3657/Assignment-4/blob/ main/main.tex

1 Question No 2.39

Find the equation of the plane through the intersection of the planes (3 -1 2)x = 4 and

$$\begin{pmatrix} 1 & 1 & 1 \end{pmatrix} \mathbf{x} = -2$$
 and the point $\begin{pmatrix} 2 \\ 2 \\ 1 \end{pmatrix}$.

2 SOLUTION

Given,

$$(3 -1 2)\mathbf{x} = 4$$
 (2.0.1)
 $(1 1 1)\mathbf{x} = -2$ (2.0.2)

$$(1 \quad 1 \quad 1) \mathbf{x} = -2$$
 (2.0.2)

$$\mathbf{A} = \begin{pmatrix} 2\\2\\1 \end{pmatrix} \tag{2.0.3}$$

Equation can be written as,

$$\mathbf{n_1^T} \mathbf{x} = c_1 \tag{2.0.4}$$

$$\mathbf{n_2^T} \mathbf{x} = c_2 \tag{2.0.5}$$

Where,

$$\mathbf{n_1} = \begin{pmatrix} 3 \\ -1 \\ 2 \end{pmatrix}, \mathbf{n_2} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} \tag{2.0.6}$$

$$c_1 = 4, c_2 = -2 \tag{2.0.7}$$

Required equation of the plane containing (2.0.4) and (2.0.5) is,

$$\mathbf{n_1^T} \mathbf{x} + \lambda \mathbf{n_2^T} \mathbf{x} = c_1 + \lambda c_2 \tag{2.0.8}$$

$$\implies (\mathbf{n_1^T} + \lambda \mathbf{n_2^T})\mathbf{x} = c_1 + \lambda c_2 \tag{2.0.9}$$

By substituting the intersection of the plane of the point (2.0.3).so,

$$\implies \lambda = \frac{-2}{3} \tag{2.0.10}$$

 \therefore By substituting $\lambda, n_1, n_2, c_1, c_2$ values in (2.0.9) we get required plane equation as,

$$(7 -5 4)\mathbf{x} = 8$$
 (2.0.11)

Plot of the plane:

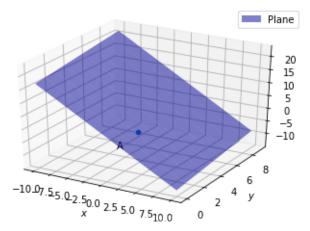


Fig. 2.1: Plot of the plane