Formal definition of regret

• Over T iterations: $\mu^{\star} = \max \max$ maximum mean among the arms (coins in this case)

• X_t be the outcome of the t-th coin toss

 \bullet Regret over T iterations is

$$Reg_T = T \times \mu^* - Total expected reward$$
$$= T \times \mu^* - \mathbb{E}[X_1 + X_2 + \dots + X_T]$$

Round robin exploration

Algorithm: Uniformly toss the coins in a round robin manner

• For every arm
$$a$$
 , $\mathbb{E}[N_a(T)] = \frac{T}{K}$

$$\operatorname{Reg}_{T} = \frac{T}{K} \sum_{a \neq a^{\star}} \Delta_{a} \quad \text{is linear !}$$