Problem Statement

• X_t = Reward at round t

• Objective: Maximize Expected total no. of heads:

$$\mathbb{E}[X_1 + X_2 + \cdots + X_{100}]$$

- \bullet Maximum attainable reward in expectation = Rs 100×9
- Maximizing expected total reward is equivalent to Minimizing the regret

$$100 \times 9 - \mathbb{E}[X_1 + X_2 + \cdots + X_{100}]$$

Simplifying Regret



Mean reward upon head

Loss w.r.t. best coin (Red in this case)

No. of times tossed

$$10 \times p_1 = \mathbf{Rs} \ 9$$

$$N_1 = 5$$

$$10 \times p_2 = \text{Rs } 1$$

$$N_2 = 3$$

$$10 \times p_3 = \mathbf{Rs} \ 3$$

$$N_3 = 5$$

Total expected reward =
$$9 \times N_1 + 1 \times N_2 + 3 \times N_3$$

Total expected regret = $0 \times N_1 + 8 \times N_2 + 6 \times N_3$

Regret is suffered only for pulling the sub-optimal arms (blue and magenta in this case)