

## Statistics and Probability Assignment

1. Karina makes mistakes in class according to Poisson process with an average rate of 1.2 mistakes per class.

- What is the probability that Karina makes at least 3 mistakes during one class?

$$\lambda = 1.2 \text{ [for 1 class]}$$

This is following poisson Distribution

$$P(X=x) = \frac{\lambda^x \cdot e^{-\lambda}}{x!}$$

So here Karina makes at least 3 mistakes during one class

$$\text{i.e., } P(X \geq 3)$$

$$P(X \geq 3) = 1 - [P(X=0) + P(X=1) + P(X=2)]$$

$$= 1 - \left[ \frac{1.2^0 \cdot e^{-1.2}}{0!} + \frac{1.2^1 \cdot e^{-1.2}}{1!} + \frac{1.2^2 \cdot e^{-1.2}}{2!} \right]$$

$$= 1 - [0.3012 + 0.3614 + 0.2169]$$

$$= 1 - 0.8795$$

$$= 0.1205$$

$$P(X \geq 3) = 0.1205$$

- What is the probability that Karina makes exactly 10 mistakes during two weeks of classes?

b) Karina makes exactly 10 mistakes during two weeks of class

∴ for two weeks 12 classes

$$\lambda = 1.2(12)$$

$$= 14.4$$

$$P(X=10) = \frac{(14.4)^{10} \cdot e^{-14.4}}{10!}$$

$$= \frac{213690909}{3628800}$$

$$P(X=10) = 0.0588$$

suppose if we assume Karina teaches MWF lecture

$$\text{then } \lambda = 1.2(6)$$

$$= 7.2$$

$$P(X=10) = \frac{(7.2)^{10} \cdot e^{-7.2}}{10!}$$

$$P(X=10) = 0.0770 \rightarrow \text{for MWF lecture}$$

M - Monday

W - Wednesday

F - Friday

2. When Stephan plays chess against his favourite computer program, he wins with probability 0.60, loses with probability 0.10, and 30% of the games result is a draw. Assume that the event is independent.

- Find the probability that he wins 7 games and draws 5 games.

a) here it is following multinomial distribution

$$P(X_1 = n_1, X_2 = n_2, X_3 = n_3, \dots, X_m = n_m) = \frac{n!}{n_1! n_2! n_3! \dots n_m!} p_1^{n_1} p_2^{n_2} p_3^{n_3} \dots p_m^{n_m}$$

$$= \frac{12!}{7! 0! 5!} \cdot (0.60)^7 \cdot (0.10)^0 \cdot (0.30)^5$$

$$= 0.05387$$

- Find the probability that Stephane's fifth win happens when he plays his eighth

b) here the condition is stephen's fifth win happens when he plays his eighth game

so it is following negative binomial (n trials, give success)

$$= \binom{n-1}{r-1} p^r (1-p)^{n-r}$$

$$= {}^7C_4 \cdot (0.6)^5 \cdot (0.4)^3$$

$$= 0.17118$$

Finance: 14, 12, 13, 12, 11 Purchase: 18, 19, 20, 18, 16 Sales: 10, 12, 17, 11, 13

[illegible]

4. A normal distribution has standard deviation 16. We have null hypothesis ( $H_0$ ): mean = 5 and alternative hypothesis ( $H_1$ ): mean = k.

We reject the null hypothesis when  $> k-2$

Find k and sample size (n) when  $P(\text{Type 1 error}) = 0.228$  and  $P(\text{Type 2 error}) = 0.1587$

5. A computer manufacturing company has three plants at X, Y and Z. To measure how many employees at these plants know about total quality management, a random sample of six employees was selected and a quality awareness test was administered. The test scores are given below:

Observation NO	Test Scores		
	Plant X	Plant Y	Plant Z
1	85	71	59
2	75	75	64
3	82	73	62
4	76	74	69
5	71	69	75
6	85	82	67

(a) Test the null hypothesis that the average test scores are the same for all three plants.

Assume that the variances of the score in the plants are the same

(b) Obtain a 95% confidence interval of the population mean for the plant at X.

Hint: For ANOVA, use excel for now.



Answer:-

Observation Number	Test Scores		
	Plant X	Plant Y	Plant Z
1	85	71	59
2	75	75	64
3	82	73	62
4	76	74	69
5	71	69	75
6	85	82	67

  

Anova: Single Factor				
Groups	Count	Sum	Average	Variance
Column 1	6	474	79	34
Column 2	6	444	74	20
Column 3	6	396	66	32

  

ANOVA						
Source of Variation	SS	df	MS	F	P-value	F crit
Between Groups	516	2	258	9	0.002702899	3.682320344
Within Groups	430	15	28.66666667			
Total	946	17				

  

a) Here (F-cal > F-crit) and (P-value is <0.05) so we reject NULL hypothesis(H0)

  

b) The formula for the 95% confidence interval for the population mean is  $\mu \pm 2(S.D)$  &  $\mu - 2(S.D)$

  

For plant-X			
Standard Deviation =	5.830951895		
Mean for Plant-X ( $\mu$ ) =	79		
Confidence Interval =	90.66190379	&	67.33809621