

**CMPT310**

**Classification Project:**

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| **Perceptron vs Naïve Bayes vs Mira** .  **Table of Contents**  Introduction Q1: Perceptron  Q2: Perceptron Analysis Q3: MIRA  Q4: Naïve Bayes  Q5: Digit Feature Design Q  **Introduction**  In this project, you will design three classifiers: a naïve Bayes Classifier, a perceptron classifier, and a large-margin (MIRA) classifier. You will test these classifiers on a set of scanned handwritten digit images. Even with simple features, your classifiers will be able to do quite well on these tasks when given enough training data.  Optical character recognition ([OCR](http://en.wikipedia.org/wiki/Optical_character_recognition)) is the task of extracting text from image sources. The data set on which you will run your classifiers is a collection of handwritten numerical digits (0-9). This is a very commercially useful technology, like the technique used by the US post office to route mail by zip codes. There are systems that can perform with over 99% classification accuracy (see [LeNet-5](http://yann.lecun.com/exdb/lenet/index.html) for an example system in action).  The code for this project includes the following files and data, available as a [zip file](classificationAssignment.zip).  **Data file**  digitdata Data file, including the digit images  **Files you will edit** | | | | | | | | | | |

naiveBayes.py The location where you will write your naive Bayes classifier.

perceptron.py The location where you will write your perceptron classifier.

mira.py The location where you will write your MIRA classifier.

dataClassifier.py

The wrapper code that will call your classifiers. You will also write your enhanced feature extractor here. You will also use this code to analyze the behavior of your classifier.

answers.py Answer to Question 2 goes here.

### Files you should read but NOT edit

classificationMethod.py

Abstract super class for the classifiers you will write.

(You **should** read this file carefully to see how the infrastructure is set up.)

samples.py I/O code to read in the classification data.

util.py

Code defining some useful tools. You may be familiar with some of these by now, and they will save you a lot of time.

mostFrequent.py A simple baseline classifier that just labels every instance as the most frequent class.

**Files to Edit and Submit:** You will fill in portions of perceptron.py, mira.py, answers.py, and dataClassifier.py (only) during the assignment, and submit them. You should submit these files with your code and comments. Please *do not* change the other files in this distribution or submit any of our original files other than this file.

**Evaluation:** Your code will be graded for technical correctness. Please *do not* change the names of any provided functions or classes within the code. You will not need to add any new file or functions or classes. So it is very important to stay in this boundary to make the grading standard and fair to everyone. Grading is out of 100 for total mark. The breakup of the grades per sections follows bellow.

**Academic Dishonesty:** We will be checking your code against other submissions in the class for logical redundancy. If you copy someone else's code and submit it with minor changes, we will know. These cheat detectors are quite hard to fool, so please don't try. We trust you all to submit your own work only; *please* don't let us down. If you do, we will pursue the strongest consequences available to us.

**Getting Help:** You are not alone! If you find yourself stuck on something, contact the course staff for help. Office hours, section, and the discussion forum are there for your support; please use them.

**Discussion:** Please be careful not to post spoilers.

# Question 1 (30 points): Perceptron

A skeleton implementation of a perceptron classifier is provided for you in perceptron.py. In this part, you will fill in the train function.

Unlike the naive Bayes classifier, a perceptron does not use probabilities to make its decisions. Instead, it keeps a weight vector wy of each class y ( y is an identifier, not an exponent). Given a feature list f, the perceptron compute the class y whose weight vector is most similar to the input vector f. Formally, given a feature vector f (in our case, a map from pixel locations to indicators of whether they are on), we score each class with:

score(f, y) = ∑ fiwy

i

i

Then we choose the class with highest score as the predicted label for that data instance. In the code, we will represent wy as a Counter.

## Learning weights

In the basic multi-class perceptron, we scan over the data, one instance at a time. When we come to an instance (f, y), we find the label with highest score:

y′ = arg max score(f, y′′)

y′′

We compare y′ to the true label y. If y′ = y, we've gotten the instance correct, and we do nothing. Otherwise, we guessed y′ but we

should have guessed y. That means that wy should have scored f higher, and wy′ should have scored f lower, in order to prevent this error in the future. We update these two weight vectors accordingly:

wy = wy + f

wy′ = wy′ − f

Using the addition, subtraction, and multiplication functionality of the Counter class in util.py, the perceptron updates should be relatively easy to code. Certain implementation issues have been taken care of for you in perceptron.py, such as handling iterations over the training data and ordering the update trials. Furthermore, the code sets up the weights data structure for you. Each legal label needs its own Counter full of weights.

## Question

Fill in the train method in perceptron.py. Run your code in PyCharm (with Python 3.9) using the run configuration named Percept\_k2.5. Here k the

Value used for smoothening. More about this later.

### Hints and observations:

The command above should yield validation accuracies around 82% and test accuracy about 75% (with the default 3 iterations). These ranges are wide because the perceptron is a lot more sensitive to the specific choice of tie-breaking than naive Bayes.

One of the problems with the perceptron is that its performance is sensitive to several practical details, such as how many iterations you train it for, and the order you use for the training examples (in practice, using a randomized order works better than a fixed order). The current code uses a default value of 3 training iterations and the order of processing the samples is fixed. You can change the number of iterations for the perceptron with the -i iterations option. Try different numbers of iterations and see how it influences performance. In practice, you would use the performance on the validation set to figure out when to stop training, but you don't need to implement this stopping criterion for this assignment.

# Question 2 (10 point): Perceptron Analysis

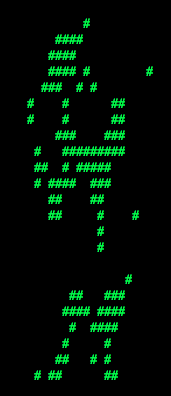
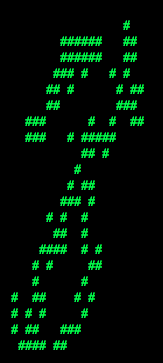
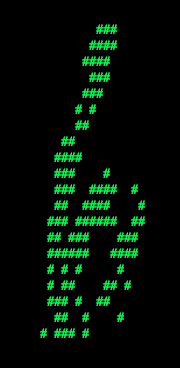
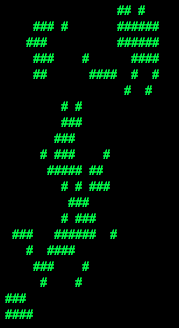
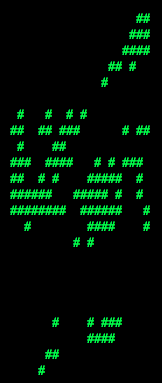
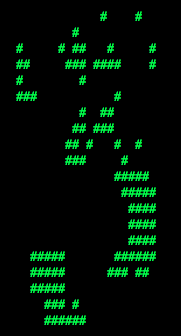
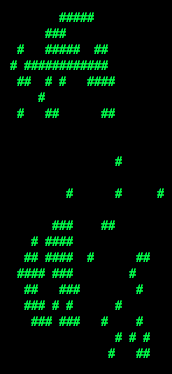
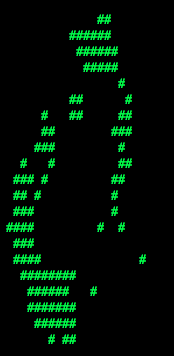
## Visualizing weights

Perceptron classifiers, and other discriminative methods, are often criticized because the parameters they learn are hard to interpret. To see a demonstration of this issue, we can write a function to find features that are characteristic of one class. (Note that, because of the way perceptrons are trained, it is not as crucial to find odds ratios.)

## Question

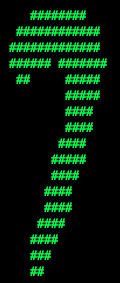
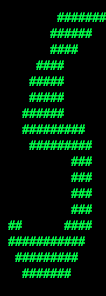
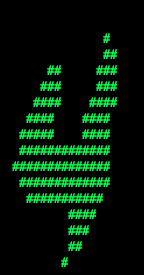
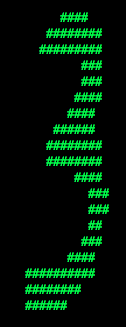
Fill in findHighWeightFeatures(self, label) in perceptron.py. It should return a list of the 100 features with highest weight for that label. You can display the 100 pixels with the largest weights using the configuration Percept\_w\_k2.5

Use this command to look at the weights’s image in the output terminal, and answer the following question. Which of the following sequence of weights is most representative of the perceptron?



### (a)

**(b)**



Answer the question answers.py in the method q2, returning either 'a' or 'b'.

# Question 3 (20 points): MIRA

A skeleton implementation of the MIRA classifier is provided for you in mira.py. MIRA is an online learner which is closely related to both the support vector machine and perceptron classifiers. You will fill in the trainAndTune function.

Note: If you have done Question 2 above, you should reproduce the same code for findHighWeightFeatures(self, label) this time in Mira.py. Otherwise ignore it.

## Theory

Similar to a multi-class perceptron classifier, multi-class MIRA classifier also keeps a weight vector wy of each label y. We also scan over the data, one instance at a time. When we come to an instance (f, y), we find the label with highest score:

y′ = arg max score(f, y′′)

y′′

We compare y′ to the true label y. If y′ = y, we've gotten the instance correct, and we do nothing. Otherwise, we guessed y′ but we should have guessed y. Unlike the perceptron, we update the weight vectors of these labels with a variable step size:

wy = wy + τf

wy′ = wy′ − τf

where τ ≥ 0 is chosen such that it minimizes

min 1 ∑ ||(w′)c − wc ||2

w′ 2 c 2

subject to the condition that (w′)yf ≥ (w′)y′ f + 1

which is equivalent to

min ||τf||2 subject to τ ≥

2

τ

(wy ′ −wy)f+1 2||f||2

and τ ≥ 0

Note that, wy′ f ≥ wyf, so the condition τ ≥ 0 is always true given τ ≥

2

2

(wy ′ −wy)f+1 2||f||2

Solving this simple problem, we then have

(wy ′ −wy)f+1

τ = 2||f||2

2

However, we would like to cap the maximum possible value of τ by a positive constant C, which leads us to

τ = min(C,

2

(wy ′ −wy)f+1 2||f||2 )

## Question

Implement trainAndTune in mira.py. This method should train a MIRA classifier using each value of *C* in Cgrid. Evaluate accuracy on the

held-out validation set for each *C* and choose the *C* with the highest validation accuracy. In case of ties, prefer the *lowest* value of *C*. Test your MIRA implementation with running configuration Mira . This configuration runs Mira with fixed C=0.001. You must also be able to run tuning using the sequence of C’s (as outlined in the code and report on each C’s accuracy. Try to interpret the accuracy’s any dependence on C value. To try your code in autotuning mode run the configuration mira\_autotune.

### Hints and observations:

Pass through the data self.max\_iterations times during training.

Store the weights learned using the best value of *C* at the end in self.weights, so that these weights can be used to test your classifier. To use a fixed value of *C=0.001*, remove the --autotune option from the command above.

The same code for returning high odds features in your perceptron implementation should also work for MIRA if you're curious what your classifier is learning.

# Question 4 (20+5 + 5 points): Naïve Bayes

A skeleton implementation of the Naïve Bayes classifier is provided for you in naiveBayes.py. We covered the theory of Naïve Bayes statistical classifier in detail in class. The provided code for this classifier is more complete, compared the other classifiers in this assignment. You will only need to fill a small part in the trainAndTune function, and in calculateLogJointProbabilities

-15 points is for trainAndTune and its related function calculateLogJointProbabilities. To run your code, use the configuration NB\_k2.5. This configuration use Laplace smoothening with factor k=2.5

-5 point for implementing findHighOddsFeatures(): A good way to see what features are prominent in one label vs another, is to implement the function FindHighOddsFeatures(label1, label2). This function returns a list of top 100 features prominent in label 1 compared to label2. This can help in theory to improve on our algorithm further. To test this part, you can run configuration NB\_k2.5\_Odd.

-5 point for autotuning: We also going to run autotuning on K with running NB\_Autotune. In this mode you should report accuracy for each k, to see what value of k gives the best accuracy.

# Question 5 (7+5 points): Digit Feature Design

Building classifiers is only a small part of getting a good system working for a task. Indeed, the main difference between a good classification system and a bad one is usually not the classifier itself (e.g. perceptron vs. naive Bayes), but rather the quality of the features used. So far, we have used the simplest possible features: the identity of each pixel (being on/off).

To increase your classifier's accuracy further, you will need to extract more useful features from the data. The EnhancedFeatureExtractorDigit in dataClassifier.py is your new playground. When analyzing your classifiers' results, you should look at some of your errors and look for characteristics of the input that would give the classifier useful information about the label. You can add code to the analysis function in dataClassifier.py to inspect what your classifier is doing. For instance, in the digit data, consider the number of separate, connected regions of white pixels, which varies by digit type. 1, 2, 3, 5, 7 tend to have one contiguous region of white space while the loops in 6, 8, 9 create more. The number of white regions in a 4 depends on the writer. This is an example of a feature that is not directly available to the classifier from the per-pixel information. If your feature extractor adds new features that encode these properties, the classifier will be able exploit them. Note that some features may require non-trivial computation to extract, so write efficient and correct code.

*Note: You will be working with digits, so make sure you are using DIGIT\_DATUM\_WIDTH and DIGIT\_DATUM\_HEIGHT, instead of FACE\_DATUM\_WIDTH and FACE\_DATUM\_HEIGHT.*

## Question

Add new binary features for the digit dataset in the EnhancedFeatureExtractorDigit function. Note that you can encode a feature which takes 3 values [1,2,3] by using 3 binary features, of which only one is on at the time, to indicate which of the three possibilities you have. In theory, features aren't conditionally independent as naive Bayes requires, but your classifier can still work well in practice. We will test your classifier with running the configuration NB\_Feature.

With the basic features (without the -f option), your optimal choice of smoothing parameter should yield 82% on the validation set with a test performance of 78%. You will receive 7 points for implementing new feature(s) which yield any improvement at all on your basic feature case. You will receive 5 additional points if your new feature(s) give you a test performance greater than or equal to 85% with the above command.

# Submission

Make sure you submit only those files specified at the beginning of this file.