



Chapter 9: Information Retrieval

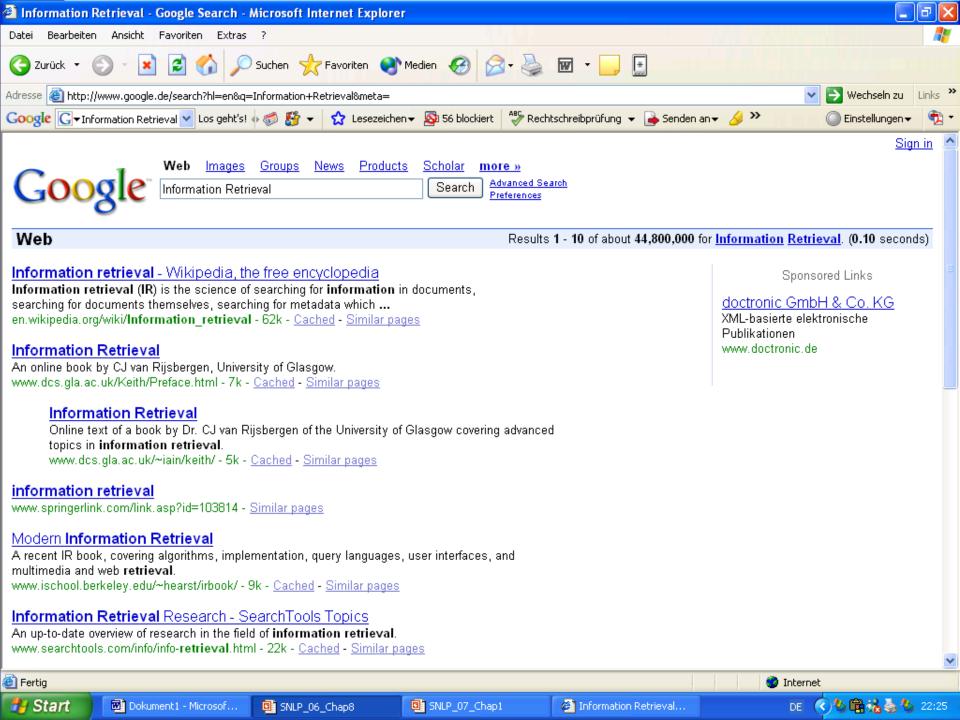
See corresponding chapter in Manning&Schütze







- In IR there is a much larger variety of possible metrics
- For different tasks, different metrics might be appropriate







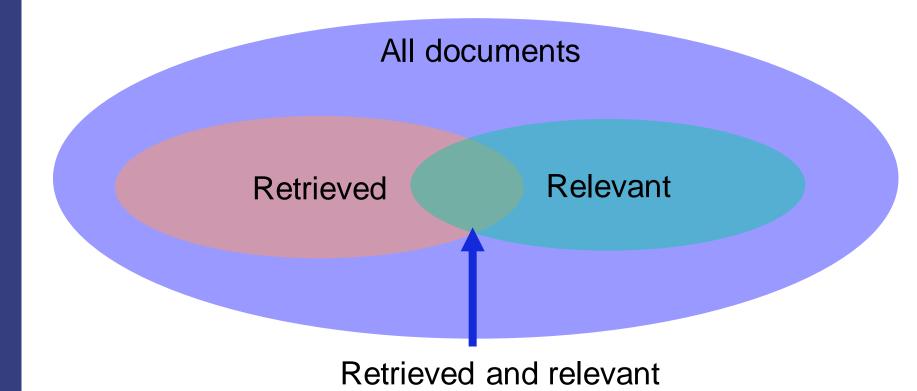
Evaluation Metrics in IR

Reading: corresponding section in Manning&Schütze









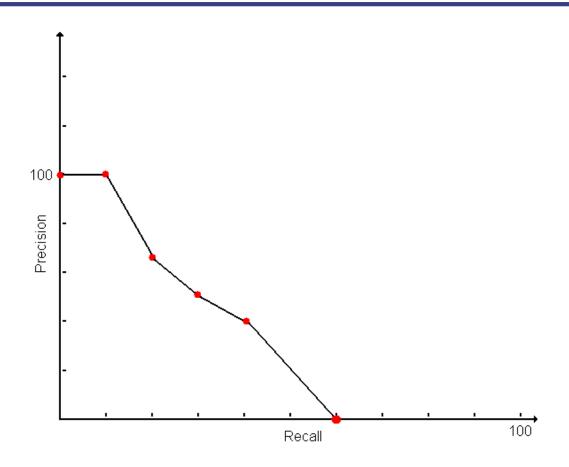
Recall=#(retrieved and relevant)/#(relevant)

Precision=#(retrieved and relevant)/#(retrieved)





Precision vs. Recall



- Standard approach in IR
- Curves can cross!





Average precision

Goal:

- don't focus on a specific recall level
- still get one number
- Each of the numbers below depends on query Q

$$AvgP = \frac{\sum_{r=1}^{N} P(r)rel(r)}{\sum_{r=1}^{N} rel(r)}$$

P(r): precision at rank r

rel(r): indicator function;

1 if document at rank r is relevant







 Problem: average precision still specific to query

$$MAP = \frac{1}{Q} \sum_{q=1}^{Q} AvgP(q)$$

Q: number of queries







Mean reciprocal rank (MRR)

$$MRR = \frac{1}{Q} \sum_{q=1}^{Q} \frac{1}{rank(q)}$$

rank(q): rank of the first match for query q

• F-Score
$$\frac{1}{F} = \frac{1}{P} + \frac{1}{R}$$

Precision at r





Vector Space Model and tf-idf

Reading: corresponding section in Manning&Schütze







- Precursor: boolean search
- Vector space mode: a simple and fast retrieval algorithm that allows for ranking
- Introduced by Karen Spärck Jones in 1972





Preprocessing

- Stemming ("going" → "go"; "fishes" → "fish", …)
- Stop words (remove "and", "to", "the", ...)
- Longer units ("New York" → "New_York")

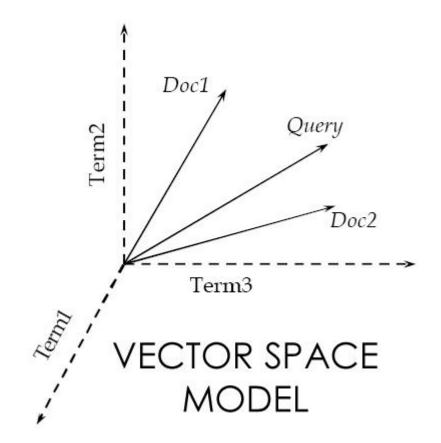
What to do depends to task and retrieval algorithm that is used







 Key idea: represent each document and also the query as a vector









- Considering every document as vector
 - The vector contains the weights of the index terms as components
 - In case of t index terms the dimension of the vector-space is also t
 - Similarity of querie to a document is the correlation between the their vectors
 - Correlation quantified by cosine of the angle between the vectors





Vector-space-model

Index term weights

$$tf_{i,j} = \frac{freq_{i,j}}{\max_{l} freq_{l,j}}$$
with $freq_{i,j}$ the frequency that termi occurs in document j

$$idf_i = \log \frac{N}{n_i}$$

with n_i number of documents (ignoring query) that contain term i and N total number of documents





Vector-space-model

- Index term weights
 - The weight of a term in a document is then calculated as product of the tf factor and the idf factor

$$w_{i,j} = tf_{i,j} \times idf_i$$

Or for the query

$$w_{i,q} = \left(0.5 + \frac{0.5 freq_{i,q}}{\max_{l} freq_{l,q}}\right) \times idf_{i}$$





Distance Metrics

- Pick an L-norm
- Angel/cosine between vectors

$$\cos(\vec{q}, \vec{d}) = \frac{\sum_{i=1}^{n} q_i d_i}{\sqrt{\sum_{i=1}^{n} q_i^2} \sqrt{\sum_{i=1}^{n} d_i^2}}$$







- Advantages
 - Improves retrieval performance as compared to Boolean retrieval
 - Partial matching allowed
 - Sort according to similarity
- Disadvantages
 - Assumes that index terms are independent





Models of Term Distribution

Reading: corresponding section in Manning&Schütze







Goal:

 Understand the statistical properties of key words in a documents collection

Assumptions

- Probability for a term is proportional to the length of the document
- Short text: each word occurs only once
- Two neighboring occurrences of the same term are statistically independent



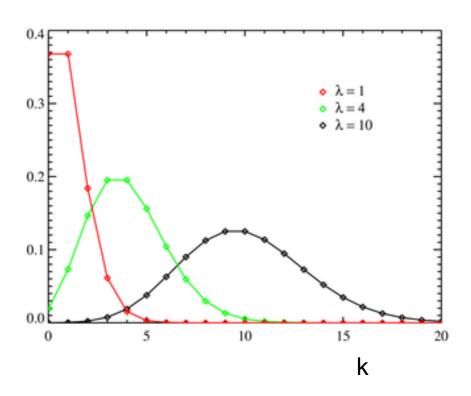




Probabiliity that the i-th term occurs k times in the document

$$P_{\lambda_i}(k) = e^{-\lambda_i} \frac{{\lambda_i}^k}{k!}$$

 λ_i parameter of the distribution





Processes described by Poisson Distribution (Wikipedia)



- The number of cars that pass through a certain point on a road (sufficiently distant from traffic lights) during a given period of time.
- The number of spelling mistakes one makes while typing a single page.
- The number of phone calls at a <u>call center</u> per minute.
- The number of times a <u>web server</u> is accessed per minute.
- The number of <u>roadkill</u> (animals killed) found per unit length of road.
- The number of <u>mutations</u> in a given stretch of <u>DNA</u> after a certain amount of radiation.
- The number of unstable <u>nuclei</u> that decayed within a given period of time in a piece of <u>radioactive substance</u>. The radioactivity of the substance will weaken with time, so the total time interval used in the model should be significantly less than the <u>mean lifetime</u> of the substance.
- The number of pine trees per unit area of mixed forest.
- The number of <u>stars</u> in a given volume of space.
- The number of <u>V2 rocket</u> attacks per area in England, according to the fictionalized account in <u>Thomas Pynchon's Gravity's Rainbow</u>.
- The number of light bulbs that burn out in a certain amount of time.
- The number of viruses that can infect a cell in cell culture.
- The number of hematopoietic stem cells in a sample of unfractionated bone marrow cells.
- The <u>inventivity</u> of an inventor over their career.
- The number of particles that "scatter" off of a target in a nuclear or high energy physics experiment.





Check normalization and expectation value → see white board







Expectation value: how often is the term i expected to occur in a document \mapsto

$$N E_i(k) = N \lambda_i = :cf_i$$
 (collection frequency)

Term present at least once →

$$N(1-P_{\lambda_i}(0)) =: df_i$$
 (document frequency)

N: the number of documents in the corpus





Experimental Test of Poisson Model

Word	cfi	λ_{i}	N(1-P(0))	df _i	Overestimation
follows	23533	0.2968	20363	21744	0.94
transformed	840	0.0106	845	807	1.03
soviet	35337	0.4457	28515	8204	3.48
students	15925	0.2008	14425	4953	2.91
james	11175	0.1409	10421	9191	1.13
freshly	611	0.0077	609	395	1,54

- Model often works
- Some terms like "soviet" are bursty
- •independence assumption is not valid





Probabilistic Retrieval

Reading: corresponding section in Manning&Schütze







Attempt to justify tf-idf for retrieval





Probabilistic Retrieval

→ See white board





Language Model based Retrieval

Reading:

- Chapter 12, "Language models for information retrieval" of Manning, Raghavan, and Schutze, Introduction to Information Retrieval, 2009
- Ponte and Croft, "A Language Model, Approach to IR", SIGIR, 1998







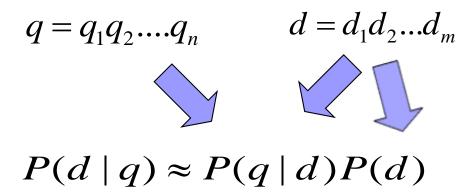
Practical way of using the probabilistic ideas for retrieval





Language Modeling

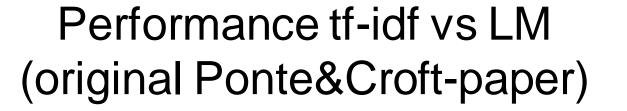
 The probability that a query q was generated by a probabilistic model based on a document.



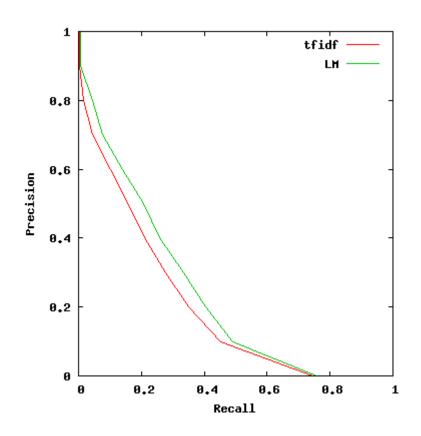
Unigram model and ignoring prior P(d):

$$P(q \mid d) = \prod_{i=1}^{n} P(q_i \mid d)$$









Results on TREC 10 collection

→ LM outperforms tf-idf







- Jelinek-mercer method:
- a linear interpolation

$$P_{\lambda}(w \mid d) = (1 - \lambda)P_{ml}(w \mid d) + \lambda P(w \mid C)$$

of the ML model

$$P_{ml}(w|d)$$

with the collection model (trained on all documents) $P(w \mid C)$





Smoothing Methods

Absolute discounting:

decrease the probability of seen words byc substracting a constant from their counts

$$P_{s}(w \mid d) = \frac{\max(c(w;d) - \delta, 0)}{\sum_{w^{*} \in V} c(w^{*};d)} + \sigma P(w \mid C)$$

See chapter 5 (notation differs in IR!)





Smoothing Methods

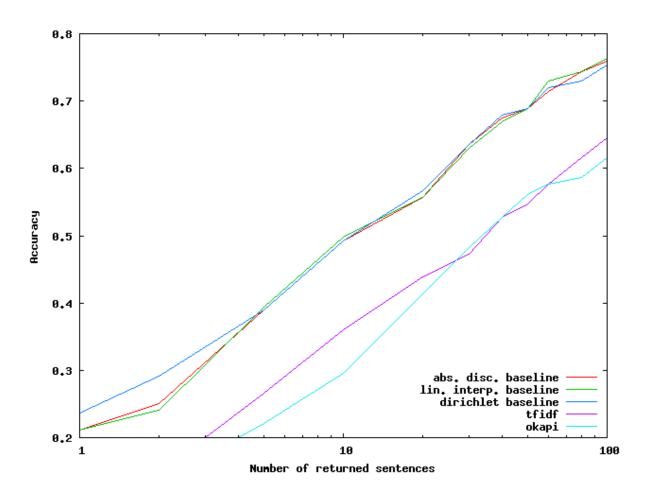
Bayesian smoothing using Dirichlet priors:
 A multinomial distribution, for which the conjugate prior for bayesian analysis is the dirichlet distribution:

$$P_{\mu}(w|d) = \frac{c(w;d) + \mu P(w|C)}{\sum_{w \in V} c(w^{*};d) + \mu}$$



Comparing different smoothing methods: sentence retrieval in question answering









Improved Language Models for IR

- Bigrams
- Class LMs
- Grammar
- Prior knowledge (document length)
- Other resources (e.g. WordNet)





Latent Semantic Analysis (LSA)

Reading: corresponding section in Manning&Schütze







Overcome semantic mismatch between terms in the query and the documents (e.g. cosmonaut vs. astronaut)





Term Document Matrix Structure

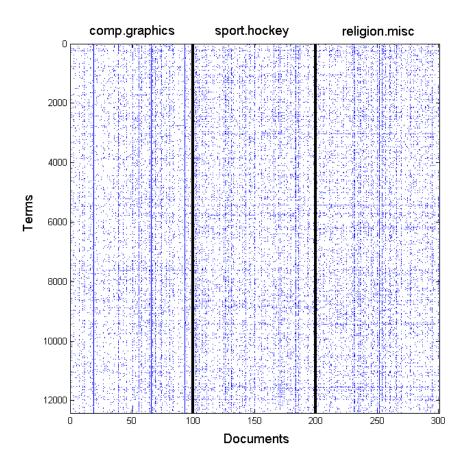
- 100 documents from 3 distinct newsgroups
- Indexed using standard stop word list
- 12418 distinct terms
- Term × Document Matrix (12418 × 300)





Term Document Matrix Structure

Idea: derive semantic relatedness from co-occurance in term document matrix









Whiteboard





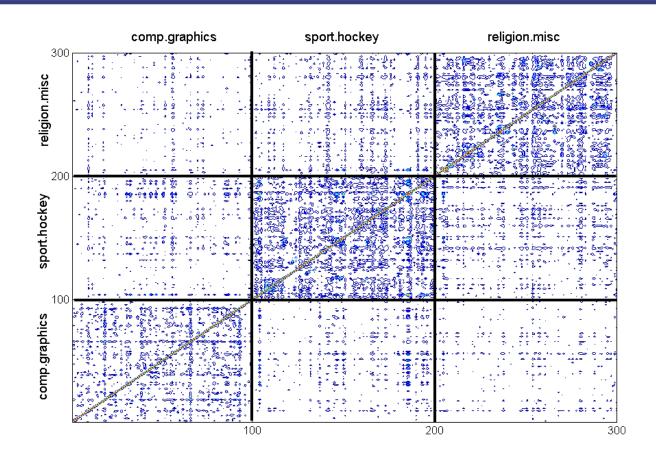
Latent Semantic Analysis

- Word usage defined by term and document cooccurrence – matrix structure
- Latent structure / semantics in word usage
- Clustering documents or words Singular Value Decomposition
- Cubic Computational Scaling



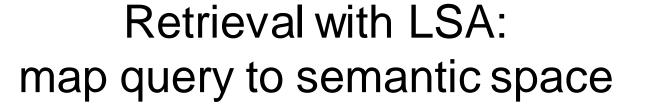


Term Document Matrix Structure

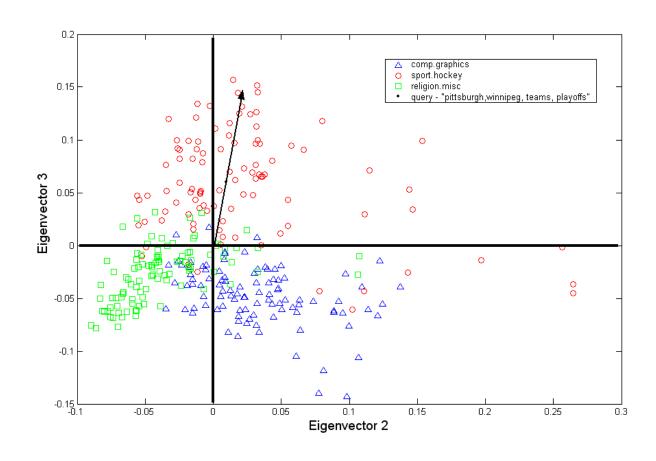


→ clearly visible similarity within a topic









→ Plausible mapping of query





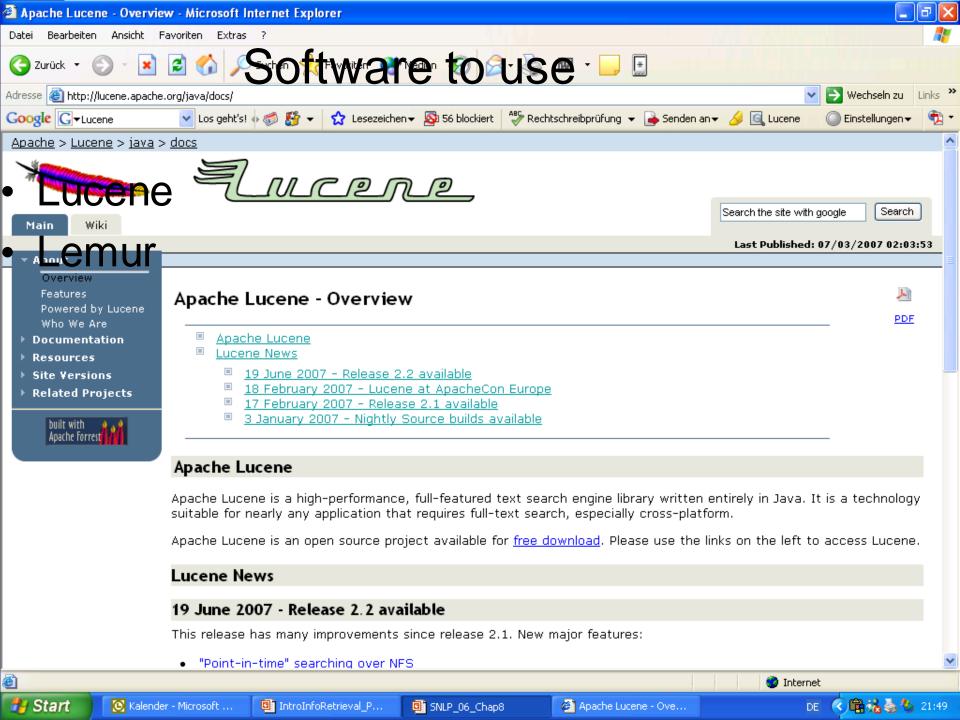


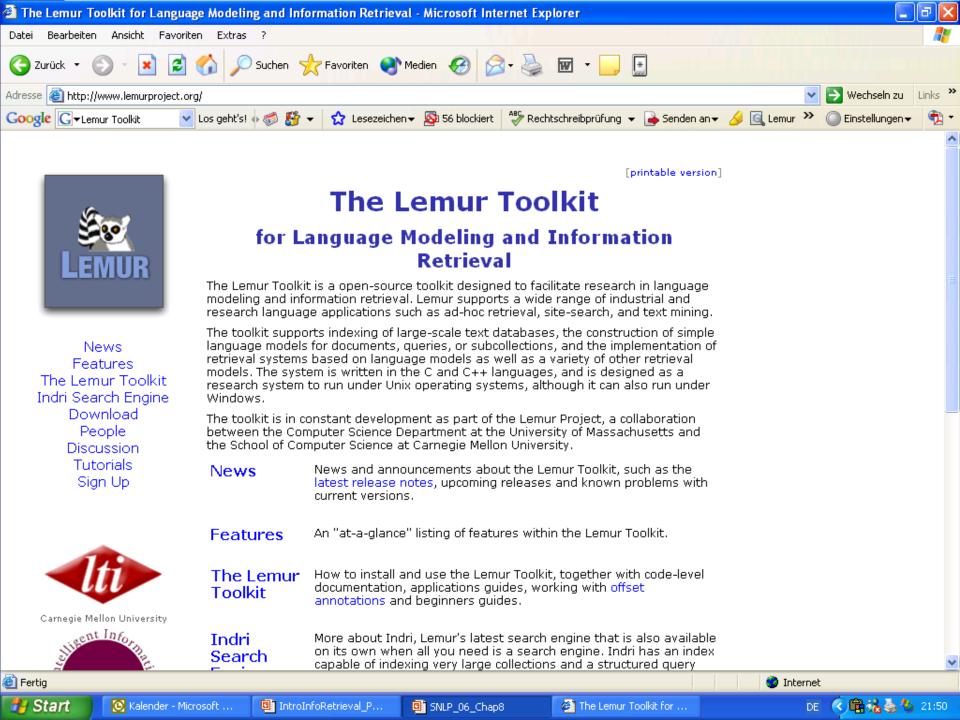
- LSA consistently improves recall on standard test collections (precision/recall generally improved)
- Variable performance on larger TREC collections
- Dimensionality of Latent Space a magic number – 300 – 1000 seems to work fine
- Computational cost high (~cubic)





Toolkits











- Evaluation measures
- Vector space model
- Models of term distribution
- Probabilistic retrieval
- Latent semantic analysis
- Language models for IR