Math 3607: Homework 3

Due: 11:59PM, Monday, February 1, 2021

- 1. (Guess-The-Number) Write the following game in which a user is to guess the integer randomly generated by the computer. In the program:
 - User inputs the lower and the upper bounds of the range.
 - The program generates a random integer within the specified range and stores it in a variable.
 - Use a while-loop for repeated guessing.
 - If the user guessed a number larger than the generated number, print out "Your guess is too high. Try again!".
 - If the user guessed a number smaller than the generated number, print out "Your guess is too low. Try again!".
 - If the user guessed the number correctly, print out "Congratulations!" and terminate the program.

Below is an example run of the program.

>> guess

Enter the lower bound: 1
Enter the upper bound: 100

Guess a number: 50

Your guess is too low. Try again!

Guess a number: 75

Your guess is too low. Try again!

Guess a number: 87

Your guess is too high. Try again!

Guess a number: 81

Your guess is too low. Try again!

Guess a number: 84

Your guess is too high. Try again!

Guess a number: 82 Congratulations!

- 2. (**Gap of 10**, Lecture 5) Simulate the tossing of a *biased* coin whose tails is 3 times more likely to be showing than its heads, until the gap between the number of heads and that of tails reaches 10.
- 3. (Construction of Arrays) Do the following problems ¹.

- LM: Learning MATLAB, Problem Solving, and Numerical Analysis Through Examples (Overman)
- NCM: Numerical Computing with MATLB (Moler)
- FNC: Fundamentals of Numerical Computation (Driscoll and Braun)

¹Reference Keys:

- LM 3.1-3(b,c,e,g)
- LM 3.1–4(c,e)
- **LM** 3.1–5(d,f)

Please read the notes at the beginning of Section 3.1 exercises on p. 382. In addition, pay attention to **Note** found at the end of individual problems, if there is any.

- 4. Do **LM** 3.1–16.
- 5. Do **LM** 3.2–7.

For this problem, assume that A is already stored in MATLAB and simply provide MATLAB statements generating B, C, and D; use of the $Code\ Examples$ environment is recommended. (Obviously, in the development stage, you may define A so that you can check your work.)

- 6. (Birthday Problem, Lecture 7) In a group of *n* randomly chosen people, what is the probability that everyone has a different birthday?
 - (a) Find this probability by hand.
 - (b) Let n = 30. Write a script that generates a group of n people randomly and determines if there are any matches.
 - (c) Modify the script above to run a number of simulations and numerically calculate the sought-after probability. Try 1000, 10000, and 100000 simulations. Compare the result with the analytical calculation done in 1.