

## Algebra of Set Operations

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# Not an Element

## Proposition 1 (:B<sub>proposition</sub>.)

Let  $A$  and  $B$  be sets and let  $x$  be any object. Then:

- 1  $x \notin A \cup B$  iff  $x \notin A$  and  $x \notin B$ .
- 2  $x \notin A \cap B$  iff  $x \notin A$  or  $x \notin B$ .
- 3  $x \notin A \setminus B$  iff  $x \notin A$  or  $x \in B$ .

# De Morgan's Laws for Sets

## Theorem 1 (De Morgan's Laws for Sets)

*Let  $S$ ,  $A$ , and  $B$  be sets. Then:*

①  $S \setminus (A \cup B) = (S \setminus A) \cap (S \setminus B).$

②  $S \setminus (A \cap B) = (S \setminus A) \cup (S \setminus B).$

# Distributive Laws for Unions and Intersections

## Theorem 2 (Distributive Laws for Unions and Intersections)

*Let  $S$ ,  $A$ , and  $B$  be sets. Then:*

- ①  $S \cap (A \cup B) = (S \cap A) \cup (S \cap B).$
- ②  $S \cup (A \cap B) = (S \cup A) \cap (S \cup B).$

# Associative Laws for Unions and Intersections

## Proposition 2 (Associative Laws for Unions and Intersections)

*Let  $A$ ,  $B$ , and  $C$  be sets. Then:*

$$\textcircled{1} (A \cup B) \cup C = A \cup (B \cup C)$$

$$\textcircled{2} (A \cap B) \cap C = A \cap (B \cap C)$$

# Commutative Laws for Unions and Intersections

## Proposition 3 (Commutative Laws for Unions and Intersections)

*Let  $A$  and  $B$  be sets. Then:*

①  $A \cup B = B \cup A$

②  $A \cap B = B \cap A$