# **Relational and Logical Operations**

#### **Contents**

Another Way to Display Text

2 Relational and Logical Operators

8 Examples

4 Exercises

# Another Way to Display Text

#### FPRINTF: Alternate Displaying Function

#### Combine literal text with numeric data.

Number of digits to display

```
fprintf('There are %d days in a year.\n', 365)
```

Complex number

```
z = exp(li*pi/4);
fprintf('%f+%fi\n', real(z), imag(z));
```

#### FPRINTF: Formatting Operator

```
%[field width][precision][conversion character]
```

*e.g.* %12.5f.

- %: marks the beginning of a formatting operator
- [field width]: maximum number of characters to print; optional
- [precision] number of digits to the right of the decimal point; optional
- [conversion character]

%d	integer	
%f	fixed-point notation	
%e	exponential notation	
%g	the more compact of %f or %e	
%S	string array	
%X	hexadecimal	

# **Relational and Logical Operators**

## **Relational Operators**

How are two numbers X and Y related?

- [X>Y] Is X greater than Y?
- [X<Y] Is X less than Y?</p>
- [X>=Y] Is X greater than or equal to Y?
- [X<=Y] Is X less than or equal to Y?
- [X==Y] Is X equal to Y?
- [X~=Y] Is X not equal to Y?

The symbols used between X and Y are called the **relational operators**.

## **Logical Variables and Logical Operators**

- A relational statement evaluates to either True(1) or False(0); these are called logical variables or boolean variables.
- As arithmetic operators (+, -, \*, /) put together two numbers and produce other numbers, logical operators combine two logical variables to produce other logical variables.
- Logical Operators: and, or, not, xor

#### Logical Operator: & & (AND)

Let  ${\tt A}$  and  ${\tt B}$  be two logical variables. The && operation is completely defined by the following truth table:

A	В	A && B
F	F	F
F	Т	F
Т	F	F
Т	Т	Т

Note that  $\mathbb{A} \& \& \mathbb{B}$  is true if and only if both  $\mathbb{A}$  and  $\mathbb{B}$  are true.

## Logical Operator: | | (OR)

Let  ${\tt A}$  and  ${\tt B}$  be two logical variables. The  $|\ |$  operation is completely defined by the following truth table:

А	В	Α  B
F	F	F
F	Т	Т
Т	F	Т
Т	Т	T <

Note that  $A \mid \ \mid \ B$  is false if and only if both A and B are false.

## Logical Operator: xor (exclusive or)

This is a special variant of the  $|\cdot|$  operator.

А	В	xor(A,B)
F	F	F
F	Т	Т
Т	F	Т
Т	Т	F

Note that xor(A, B) is true if only one of A or B is true.

# Logical Operator: ~ (NOT)

many operator (acts on one variable)

This is a negation operator.

# **Combination of Logical Operations**

7 De Morgan's Law

Let A and B be logical variables. Then ~ (A && B) and ~A | | ~B are equivalent:

А	В	A && B	~(A && B)
F	F	F	T
F	Т	£	T
Т	F	<del>-</del>	_
Т	Т	<u> </u>	

. 
$$\sim$$
 (AIIB)  $\equiv$   $\sim$  A &&  $\sim$ B is the other half of De Morgan's Law.

# **Examples**

## **Quadratics Revisited**

Consider a monic quadratic function  $q(x)=x^2+bx+c$  on a close interval [L,R].

- Critical point:  $x_c = -b/2$
- If  $x_c \in (L, R)$ , q(x) attains the (global) minimum at  $x_c$ ; otherwise, the minimum occurs at one of the endpoints x = L or x = R.

#### Question

Write a program which determines whether the critical point of q(x) falls on the interval.

#### Initialization

```
b = input('Enter b: ');
c = input('Enter c: ');
L = input('Enter L: ');
R = input('Enter R (L<R): ');
clc
fprintf('Function: x^2 + bx + c, b = %5.2f, c = %5.2f\n', b, c)
fprintf('Interval: [L, R], L = %5.2f, R = %5.2f\n', L, R)
xc = -b/2;</pre>
```

#### Main Fragment

```
if L < xc && xc < R
    fprintf('Interior critical point at x_c = %5.2f\n', xc)
else
    disp('Either xc <= L or xc >= R')
end
```

## Main Fragment – another way

```
if xc <= L || xc >= R
    disp('Either xc <= L or xc >= R')
else
    fprintf('Interior critical point at x_c = %5.2f\n', xc)
end
```

## Main Fragment – yet another way

```
if ~(xc <= L || xc >= R)
    fprintf('Interior critical point at x_c = %5.2f\n', xc)
else
    disp('Either xc <= L or xc >= R')
end
```

## The simplest if statement?

#### So far, we have seen

- if-else **statement**
- if-elseif-else statement

#### The simplest if statement is of the form

```
if [condition]
  [statements to run]
end
```

#### **Input Errors**

If a user mistakenly provides L that is larger than R, fix it silently by swapping L and R.

```
if L > R
    tmp = L;
    L = R;
    R = tmp;
end
```

I will show you how to send an error message and halt a program later.

# **Exercises**

## **Exercise 1: Simple Minimization Problem**

#### Question

Write a program that finds  $x_{\min} \in [L, R]$  at which q(x) is minimized and the minimum value  $q(x_{\min})$ .

• This can be done with if-elseif-else

## Exercise 2: Leap Year

#### Question

Write a script which determines whether a given year is a leap year or not. A year is a leap year if

- it is a multiple of 4;
- it is not a multiple of 100;
- it is a multiple of 400.

**Useful:** mod function.

#### Pseudocode

```
if [YEAR] is not divisible by 4
   it is a common year
elseif [YEAR] is not divisible by 100
   it is a leap year
elseif [YEAR] is not divisible by 400
   it is a common year
else
   it is a leap year
end
```

## Exercise 3: Angle Finder

#### Question

Let x and y be given, not both zero. Determine the angle  $\theta \in (-\pi, \pi]$  between the positive x-axis and the line segment connecting the origin to (x, y).

#### Four quandrants:

- 1st or 4th (x >= 0):  $\theta = \tan^{-1}(y/x)$
- 2nd (x < 0, y >= 0):  $\theta = \tan^{-1}(y/x) + \pi$
- 3rd (x < 0, y < 0):  $\theta = \tan^{-1}(y/x) \pi$

**Useful:** at an (inverse tangent function)

## **Extended Inverse Tangent**

```
if x > 0
    theta = atan(y/x)
elseif y >= 0
    theta = atan(y/x) + pi
else
    theta = atan(y/x) - pi
end
```

- MATLAB provides a function that exactly does this: atan2 (x, y).
- Further Exploration: What would you do if you are asked to find the angle  $\theta \in [0, 2\pi)$ , with atan alone or with atan2?