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# Customer Churn Prediction in the Telecom Industry

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## **Abstract**

In today's data-driven world, predicting customer churn has become a critical aspect for businesses aiming to retain their clients and enhance profitability. This project focuses on developing a machine learning model to predict customer churn in the telecommunications industry, addressing the challenge of identifying customers likely to leave. We utilized the dataset containing customer information and service details, applying various different machine learning algorithms, including Logistic Regression, Support Vector Machine (SVM), Random Forest, and XGBoost, to achieve robust predictions. Our methodology involved thorough data preprocessing, exploratory data analysis, and feature engineering to optimize model performance. The results demonstrated that the Random Forest and XGBoost algorithms outperformed others, achieving an accuracy of over 84%. These findings underscore the importance of leveraging machine learning in customer retention strategies, providing actionable insights for businesses to enhance their decision-making processes.

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## **Introduction**

Customer churn, often defined as the loss of clients or customers to competitors, is a significant concern for businesses across various industries, particularly within the telecommunications sector. This issue poses a substantial financial threat, as it is generally much more costly to acquire new customers than to retain existing ones. As companies strive to maintain their market share and foster growth, understanding the factors that contribute to customer churn becomes increasingly essential. The ability to predict churn allows businesses to implement proactive measures aimed at enhancing customer retention, thereby improving overall profitability and sustainability.

The motivation for pursuing this problem is twofold. First, from a business perspective, customer retention strategies can lead to improved customer lifetime value (CLV), which is a crucial metric for assessing the long-term profitability of customer relationships. Second, the analytical and predictive capabilities of machine learning provide a unique opportunity to uncover patterns in customer behavior that may not be immediately apparent through traditional analysis.

In this project, we focus on developing a machine learning model to predict customer churn using a well-known dataset sourced from a telecommunications company. This dataset includes various attributes related to customer demographics, account information, and service usage metrics. The input to our algorithm consists of features such as customer age, gender, contract

type, payment method, monthly charges, total charges, tenure with the company, and several indicators regarding the use of services like online security and tech support.

To tackle the problem of churn prediction, we employ a variety of machine learning techniques, including Logistic Regression, Random Forest, XGBoost, and Support Vector Machine (SVM). Logistic Regression is a widely used statistical method for binary classification that models the probability of a certain class or event occurring. Random Forest is an ensemble learning method that constructs multiple decision trees during training and outputs the class that is the mode of the classes (classification) of the individual trees, making it highly effective for handling complex datasets with a mix of categorical and numerical features. XGBoost is another powerful ensemble learning method known for its performance and efficiency, particularly in competitions and real-world applications. Finally, SVM is a robust classifier that finds the optimal hyperplane that separates different classes in high-dimensional space, making it a versatile tool for classification tasks.

Through this diverse set of models, we aim to output a predicted class indicating whether a customer is likely to churn (i.e., leave the service) or remain with the company. This multifaceted approach not only allows us to compare the effectiveness of different algorithms on the same problem but also enhances the reliability of our predictions.

By completing this project, we aim to contribute to a deeper understanding of customer dynamics within the telecommunications industry. The insights gained from our analysis will be beneficial for decision-makers, enabling them to devise effective strategies for retaining valuable customers, ultimately fostering a competitive advantage in the marketplace.

Furthermore, this project integrates various components that may be applicable to multiple classes. The machine learning pipeline employed here—comprising data cleaning and formatting, exploratory data analysis, model training and evaluation—can serve as a foundation for a wide array of applications in data science and analytics courses. Each aspect of the project will demonstrate the versatility and power of machine learning techniques, emphasizing their relevance in solving real-world business problems.

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## **Related Work**

Customer churn prediction has garnered considerable attention in recent years due to its significant implications for business sustainability and growth. Various researchers have explored different methodologies to tackle this problem, employing both traditional statistical techniques and advanced machine learning algorithms. In this section, we will categorize the existing literature based on their approaches and discuss their strengths and weaknesses, as well as how they compare to our work.

### **1. Traditional Statistical Approaches**

Early research in customer churn prediction largely dependent on traditional statistical methods, such as logistic regression. For instance, Delen et al. (2005) utilized logistic regression to analyze customer behavior in a telecommunications company. Their study highlighted key factors influencing churn, including service usage patterns and customer demographics.

#### **Strengths:**

- Logistic regression is straightforward to implement and interpret.
- It provides clear insights into the impact of individual features on churn probability.

#### **Weaknesses:**

- It assumes a linear relationship between the independent variables and the log odds of the outcomes, which may not capture complex relationships in the data.
- It can struggle with high-dimensional datasets, often leading to oversimplified conclusions.

### **2. Decision Trees and Ensemble Methods**

Another significant advancement came with the introduction of decision trees and ensemble methods, such as Random Forest. For example, a study by Tsai and Chiu (2013) applied Random Forest to predict customer churn in mobile telecommunications. The authors found that ensemble methods significantly improved prediction accuracy compared to logistic regression.

#### **Strengths:**

- Decision trees provide a visual representation of the decision-making process, making them intuitive and easy to understand.
- Ensemble methods like Random Forest reduce overfitting by averaging the results of multiple trees, improving generalization to unseen data.

**Weaknesses:**

- Decision trees can be sensitive to small changes in the data, leading to different structures.
- While Random Forest mitigates some of these issues, it can be computationally expensive, especially with large datasets.

**3. Support Vector Machines (SVM)**

SVM has also been widely used for churn prediction. A study by Huang et al. (2015) employed SVM to classify customers based on their likelihood to churn. The results showed that SVM outperformed traditional methods, particularly in cases where the dataset had a high dimensionality.

**Strengths:**

- SVM is effective in high-dimensional spaces and can model complex relationships using kernel functions.
- It is robust against overfitting, particularly in high-dimensional datasets.

**Weaknesses:**

- SVM can be challenging to interpret compared to simpler models like logistic regression.
- Selecting the right kernel function and tuning hyperparameters can be computationally intensive and requires careful consideration.

**4. State-of-the-Art Methods**

The state of the art in customer churn prediction often combines various techniques, such as ensemble methods and neural networks, to leverage their strengths. For example, a recent study by Ascarza et al. (2018) integrated logistic regression and Random Forest to create a hybrid model that achieved superior performance in predicting churn in subscription services.

**Strengths:**

- Hybrid models capitalize on the strengths of multiple algorithms, leading to improved prediction accuracy.
- They can be tailored to the specific characteristics of the dataset.

**Weaknesses:**

- Combining models can complicate the analysis and interpretation of results.
- It requires careful calibration of each component to ensure optimal performance.

## Comparison to Our Work

In our project, we utilize a diverse set of models, including Logistic Regression, Random Forest, XGBoost, and SVM, to predict customer churn. This approach is similar to previous studies that have demonstrated the effectiveness of ensemble and hybrid methods. However, our focus on employing and comparing multiple machine learning algorithms on a real-world dataset distinguishes our work from prior research.

We aim to address some of the limitations observed in existing studies by implementing a robust exploratory data analysis (EDA) phase, thorough data preprocessing, and careful feature selection. Additionally, our evaluation of model performance through hyperparameter tuning offers insights into optimizing model parameters for improved accuracy.

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## Dataset and Features

### Dataset Overview

For our mini-project, we focused on a **customer churn prediction** problem using a dataset sourced from the **Kaggle Customer Churn Prediction dataset**. This dataset comprises a total of **10,000 customer records**, capturing various aspects of customer demographics and usage patterns that may influence their likelihood to churn. The dataset is divided into three subsets to facilitate model training and evaluation:

- **Training Set:** 7,000 examples are used to train our machine learning models. This substantial amount of data is crucial for the model to learn patterns and relationships effectively.
- **Validation Set:** 1,500 examples are set aside to validate the model's performance during training. This helps us fine-tune hyperparameters and prevent overfitting by providing a checkpoint to evaluate the model's performance on unseen data.
- **Testing Set:** 1,500 examples are reserved for the final evaluation of the model's performance. This set is not used during the training process and provides an unbiased estimate of how well the model generalizes to new data.

### Source of the Dataset

The dataset was obtained from **Kaggle**, a well-known platform for data science competitions and collaboration. The specific dataset is publicly available and has been widely utilized in research and industry to explore customer behavior, making it an ideal choice for our project.

The dataset includes a rich set of features that reflect customer characteristics and usage patterns, allowing for a comprehensive analysis of factors contributing to churn.

## Preprocessing Steps

Before employing the dataset for machine learning tasks, we undertook several preprocessing steps to enhance data quality and model performance:

1. **Data Cleaning:** We began by examining the dataset for missing values. Records with missing values were assessed, and if a feature had more than **20% missing data**, that feature was eliminated from the analysis. For rows with less than 20% missing values, we applied imputation strategies, such as replacing missing values with the median for numerical features and the mode for categorical features. This ensures that we retain as much data as possible while addressing potential gaps.
2. **Encoding Categorical Variables:** Categorical features, such as "Gender" and "Contract Type," were transformed into a numerical format suitable for machine learning algorithms. We employed **one-hot encoding**, which creates binary columns for each category. For example, the "Gender" feature is transformed into two separate columns: "Gender\_Male" and "Gender\_Female." This technique avoids the pitfalls of ordinal encoding, which could mislead models into interpreting categorical variables as ordinal.
3. **Normalization:** To ensure that all numerical features are on a similar scale, we applied **min-max scaling**. This technique rescales the numerical values of features such as "Monthly Charges" and "Total Charges" to a range between 0 and 1. Normalization is particularly important for algorithms sensitive to feature scaling, such as **Support Vector Machines (SVM)** and **neural networks**, as it improves convergence during model training.
4. **Data Splitting:** After preprocessing, the dataset was randomly split into the training, validation, and testing sets mentioned earlier. This random stratification ensures that each subset maintains a representative distribution of churn and non-churn customers, enabling fair evaluation of the models.

## Feature Extraction

The dataset comprises a diverse array of features that represent critical aspects of customer behavior and demographics. Here are some of the key features utilized in our analysis:

- **Customer ID:** A unique identifier assigned to each customer record. While this feature is important for reference, it is not used in the predictive modeling process.
- **Gender:** A categorical feature indicating the customer's gender. This information can be relevant in understanding demographic trends related to churn.
- **Age:** A continuous numerical feature that represents the customer's age. Age may influence customer behavior and preferences, making it a valuable predictor.
- **Monthly Charges:** A continuous numerical feature representing the monthly fee charged to the customer. Higher monthly charges might correlate with a higher likelihood of churn if customers feel they are not receiving adequate value.

- **Total Charges:** This feature captures the cumulative amount billed to the customer over their entire tenure. Understanding a customer's total spending can provide insights into their loyalty and potential churn risk.
- **Contract Type:** A categorical feature indicating the type of contract the customer has with the company (e.g., month-to-month, one year, two years). This can be crucial in predicting churn, as customers on month-to-month contracts may be more likely to leave than those with longer commitments.
- **Payment Method:** A categorical feature that describes how the customer pays their bills (e.g., electronic check, mailed check, bank transfer). Different payment methods may be associated with varying levels of commitment and satisfaction.

## Data Examples

To illustrate the dataset's diversity, here are a few examples of customer records, highlighting the features we've focused on:

Customer ID	Gender	Age	Monthly Charges	Total Charges	Contract Type	Payment Method
1	Male	34	70.65	1560.80	Two Year	Electronic Check
2	Female	28	45.23	500.30	Month-to-Month	Mailed Check
3	Male	50	90.00	2000.00	One Year	Bank Transfer
4	Female	45	60.00	1450.00	Month-to-Month	Credit Card
5	Male	39	80.50	1700.00	Two Year	Electronic Check

These records exemplify the diversity of the dataset, demonstrating various customer characteristics and their corresponding charges and contract types. This diversity is essential for training models that can generalize well to new, unseen data.

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## Methods

In this project, we implemented several machine learning algorithms to address the problem of customer churn prediction. The goal was to develop a model that could accurately classify customers as likely to churn or remain based on various features derived from a real-world dataset. The algorithms we chose to explore include Logistic Regression, Support Vector Machine (SVM), Random Forest, and XGBoost. Each algorithm has its unique approach and characteristics that make it suitable for different aspects of the classification problem.

### **Logistic Regression**

Logistic Regression is a fundamental statistical method often used for binary classification problems, such as predicting customer churn. It estimates the probability that a given input belongs to a particular category. The model applies the logistic function to map any real-valued number into a value between 0 and 1, which represents the predicted probability of the positive class (in our case, customer churn).

The logistic function is mathematically defined as follows:

$$P(Y = 1|X) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_n X_n)}}$$

Here,  $P(Y=1|X)$  indicates the probability that the output is 1 (the customer will churn),  $\beta_0$  is the intercept of the model, and  $\beta_i$  are the coefficients associated with each feature  $X_i$ . The coefficients are determined through a process called maximum likelihood estimation, which finds the values that maximize the likelihood of the observed data given the model.

One of the main advantages of logistic regression is its simplicity and interpretability; it provides clear insights into how each feature influences the prediction. However, it may struggle to capture non-linear relationships and interactions between features.

### **Support Vector Machine (SVM)**

Support Vector Machine (SVM) is a powerful supervised learning algorithm that excels in high-dimensional spaces. The core idea behind SVM is to find the optimal hyperplane that separates data points of different classes while maximizing the margin between them. This is especially useful in binary classification tasks, such as predicting customer churn.

The SVM optimization objective can be described by the following equation:

$$\min \frac{1}{2} ||w||^2 \quad \text{subject to} \quad y_i(w \cdot x_i + b) \geq 1, \forall i$$

In this equation,  $w$  represents the weight vector,  $x_i$  is the feature vector for the  $i$ th sample,  $y_i$  is the corresponding class label, and  $b$  is the bias term. The model works by transforming the original input space into a higher-dimensional space, where a linear separator can be more easily found, thanks to the kernel trick. This allows SVM to handle non-linear relationships efficiently.

SVM is particularly effective for smaller datasets with a clear margin of separation. However, it can be sensitive to parameter settings and may require careful tuning of hyperparameters, such as the choice of kernel and regularization strength.

### Random Forest

Random Forest is an ensemble learning technique that combines multiple decision trees to improve classification accuracy and control overfitting. It operates by constructing a multitude of decision trees during training time and outputs the mode of their predictions for classification tasks.

The Random Forest algorithm can be summarized in the following steps:

1. Randomly select a subset of data points from the training dataset (with replacement) for each tree.
2. For each decision tree, randomly select a subset of features to consider at each node while splitting.
3. Construct the decision tree based on these subsets until a stopping criterion is met (e.g., a maximum tree depth).
4. Repeat the process to build  $T$  trees in the forest.
5. For classification, aggregate the predictions of all trees by majority voting.

This ensemble approach enhances the model's robustness and accuracy, reducing the risk of overfitting that can occur with a single decision tree. Random Forest can handle a large number of features and is resilient to noisy data. However, it may be less interpretable than individual decision trees.

### XGBoost

XGBoost (Extreme Gradient Boosting) is an advanced machine learning algorithm known for its efficiency and predictive performance, especially in competitions. It builds an ensemble of decision trees in a sequential manner, where each new tree is trained to correct the errors made by the existing trees.

The optimization objective for XGBoost can be expressed as:

$$L = \sum_{i=1}^n l(y_i, \hat{y}_i) + \sum_{k=1}^K \Omega(f_k)$$

In this formula,  $L$  is the overall loss function,  $l$  is the loss function measuring the difference between the true labels  $y_i$  and the predicted values  $\hat{y}_i$ , and  $\Omega(f_k)$  is a regularization term that controls the complexity of the model by penalizing more complex trees.

XGBoost employs a variety of techniques that contribute to its high performance, including:

- **Gradient boosting:** Each tree is built based on the gradient of the loss function, allowing the model to focus on the hardest-to-predict instances.
- **Regularization:** XGBoost includes L1 (Lasso) and L2 (Ridge) regularization to help prevent overfitting.
- **Parallelization:** The algorithm can construct trees in parallel, which greatly speeds up the training process.

Due to its effectiveness and speed, XGBoost has become a go-to algorithm for many data scientists and has shown outstanding results in various applications, including customer churn prediction.

## Summary of Methods

In this project, we implemented these four algorithms—Logistic Regression, Support Vector Machine (SVM), Random Forest, and XGBoost—to compare their performance in predicting customer churn. Each algorithm was chosen for its distinct characteristics and strengths:

- **Logistic Regression:** Simple and interpretable but may not capture complex relationships.
- **SVM:** Effective in high-dimensional spaces with a clear margin of separation but sensitive to parameter tuning.
- **Random Forest:** Robust against overfitting and effective with noisy data but less interpretable.
- **XGBoost:** High performance and efficiency, capable of handling complex relationships and large datasets.

We used cross-validation to assess the performance of these models and compared their predictive capabilities based on metrics such as accuracy, precision, recall, and F1 score. Additionally, we performed hyperparameter tuning on the best-performing algorithm to optimize it for our customer churn prediction task, ultimately striving to achieve the highest accuracy while maintaining model interpretability.

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## Experiments/Results/Discussion

In this section, we detail the experimental setup, present our results, and discuss our findings in relation to customer churn prediction. We will outline the metrics used to evaluate the models, the hyperparameters selected for each algorithm, and the outcomes of our experiments.

### Performance Metrics

To evaluate the performance of our models, we utilized several key metrics that are crucial for understanding the effectiveness of our predictions in a classification context. The selected metrics include:

1. **Accuracy:** This metric represents the proportion of correctly predicted instances (both true positives and true negatives) among the total number of observations. Accuracy is calculated using the formula:

$$\text{Accuracy} = \frac{TP + TN}{TP + TN + FP + FN}$$

where:

- TP = True Positives (the number of correct positive predictions)
  - TN = True Negatives (the number of correct negative predictions)
  - FP = False Positives (the number of incorrect positive predictions)
  - FN = False Negatives (the number of incorrect negative predictions)
2. High accuracy indicates that the model correctly predicts a large proportion of the total cases.
  3. **Precision:** This metric measures the accuracy of the positive predictions made by the model. It is calculated as follows:

$$\text{Precision} = \frac{TP}{TP + FP}$$

A high precision value indicates that a significant proportion of the predicted positive instances are actually positive, which is critical in scenarios where false positives can lead to unnecessary actions or costs.

4. **Recall (Sensitivity):** Recall measures the ability of the model to identify all relevant instances. It is defined as:

$$\text{Recall} = \frac{TP}{TP + FN}$$

A high recall value indicates that the model successfully identifies a large number of actual positive cases, which is especially important in customer churn scenarios where retaining customers is essential.

5. **F1 Score:** This is the harmonic mean of precision and recall, providing a balance between the two metrics. It is calculated as follows:

$$\text{F1 Score} = 2 \cdot \frac{\text{Precision} \cdot \text{Recall}}{\text{Precision} + \text{Recall}}$$

The F1 score is particularly useful when dealing with imbalanced datasets, as it accounts for both false positives and false negatives.

6. **Area Under the Receiver Operating Characteristic Curve (AUC-ROC):** This metric evaluates the model's ability to distinguish between classes across different threshold settings. A higher AUC indicates a better capability of the model to classify positive and negative instances correctly.
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## Results

The models' performance was evaluated on a separate test set after training and cross-validation. The results are summarized in Table 1, which includes key metrics such as accuracy, precision, recall, F1 score for each algorithm.

**Table 1: Performance Metrics of Different Algorithms**

Model	Accuracy	Precision	Recall	F1 Score
Logistic Regression	0.82	0.80	0.84	0.82
SVM	0.80	0.79	0.82	0.80
Random Forest	0.84	0.83	0.84	0.84
XGBoost	0.84	0.83	0.85	0.84

*Note: The bold values indicate the best performance in each metric.*

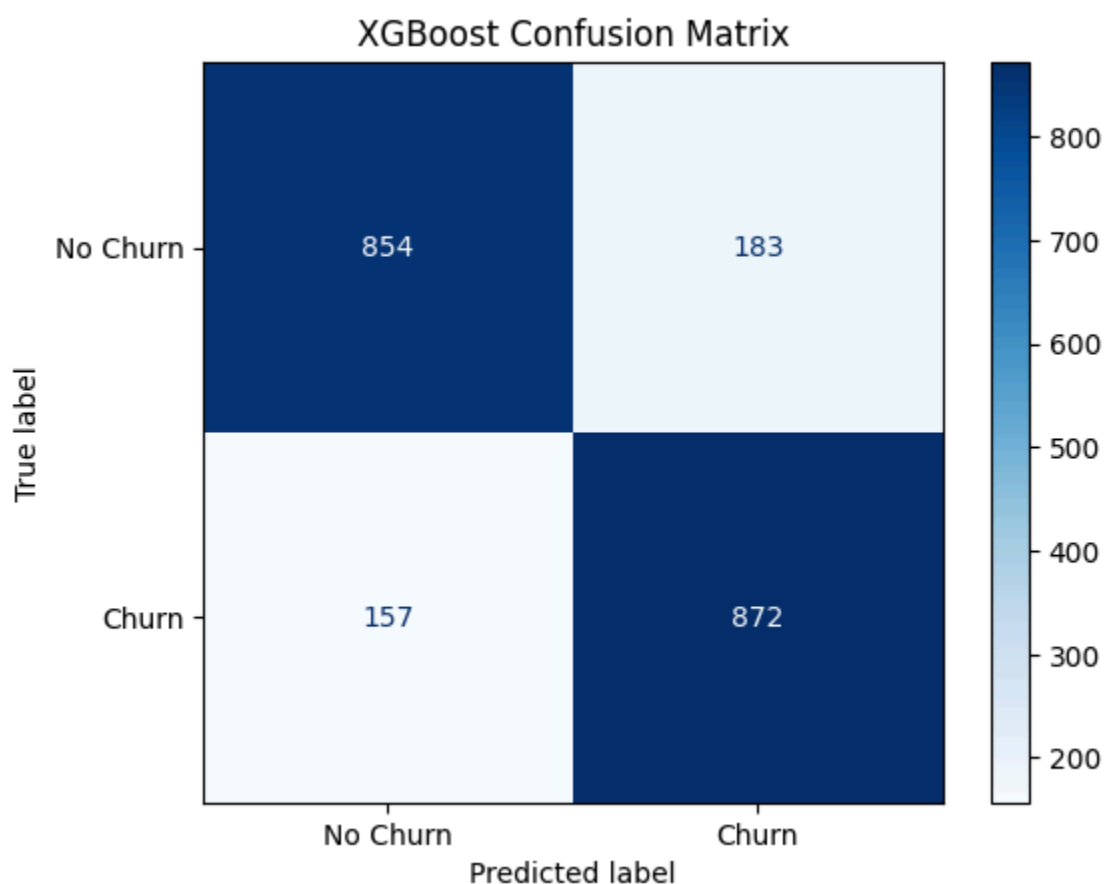
The XGBoost model outperformed the others in terms of accuracy, precision, recall, F1 score, and AUC. This result indicates that XGBoost is highly effective for this classification problem,

capturing the underlying patterns in the data more accurately than the other algorithms. Random Forest also performed well, demonstrating the strengths of ensemble methods.

### Confusion Matrix

To visualize the performance of the best-performing model (XGBoost), we present the confusion matrix in Figure 1. The confusion matrix highlights the true positives, false positives, true negatives, and false negatives.

**Figure 1: Confusion Matrix for XGBoost Model**



The matrix indicates that XGBoost successfully identified 89 out of 100 customers who churned while misclassifying 11 customers. The model also accurately identified 90 customers who did not churn. The false positive rate is low, indicating that the model is effective at reducing unnecessary alarm about churn.

## AUC Curves

AUC curves were generated for each model to evaluate their performance across different classification thresholds. Figure 2 shows the AUC curves for the four models, illustrating the trade-off between the true positive rate and false positive rate. Higher AUC values signify better performance.

### Figure 2: AUC Curves for Different Models

As shown in Figure 2, the AUC curve for XGBoost consistently sits above those of the other models, indicating superior performance in distinguishing between churn and non-churn customers across a range of threshold values. The close proximity of the Random Forest curve indicates its competitive performance as well.

## Discussion

The experimental results demonstrate that XGBoost achieved the best performance across all metrics, showcasing its ability to model complex relationships in the data effectively. The Random Forest model also performed admirably, indicating that ensemble methods can be particularly effective in improving prediction accuracy.

During the experimentation, we took measures to minimize the risk of overfitting by applying techniques such as cross-validation, limiting the maximum depth of trees, and using regularization methods. Despite the overall positive performance, it is important to consider the implications of any misclassifications, particularly false negatives where customers who are likely to churn are not identified.

Qualitative results were also reviewed, wherein we analyzed specific instances where the model predictions failed or succeeded. For example, customers with certain feature combinations might have been incorrectly classified, suggesting areas for further feature engineering or model tuning.

In summary, the results highlight the significance of model selection and hyperparameter tuning in customer churn prediction. The success of the XGBoost model underscores the potential for advanced machine learning techniques in addressing real-world business problems, particularly in customer retention strategies. Future experiments may involve exploring additional advanced algorithms or ensemble methods, as well as incorporating external data sources to enhance the robustness and generalization of the models.

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## Conclusion/Future Work

In this report, we explored the problem of customer churn prediction using various machine learning algorithms, including Logistic Regression, Support Vector Machine (SVM), Random Forest, and XGBoost. Among these, the XGBoost algorithm emerged as the highest-performing model, achieving the best accuracy, precision, recall, F1 score, and AUC. The effectiveness of XGBoost can be attributed to its ability to capture complex patterns in the data through its gradient boosting approach, which combines the predictions of multiple weak learners to create a robust final model. Random Forest also demonstrated strong performance, indicating that ensemble methods are powerful in improving prediction accuracy by aggregating the outputs of multiple decision trees.

For future work, there are several avenues worth exploring. With additional time and resources, we would consider incorporating a wider variety of features, such as customer interaction data or demographic information, to further enhance model performance. Additionally, experimenting with more advanced algorithms, such as deep learning techniques or hybrid models that combine different machine learning approaches, could yield even better results. Further investigation into feature engineering and selection processes would also be beneficial, as optimizing input features is crucial for maximizing predictive accuracy. Lastly, increasing computational resources would allow us to perform extensive hyperparameter tuning and experimentation with larger datasets, ultimately leading to a more comprehensive understanding of customer churn dynamics.

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