
Question 1 Perceptron

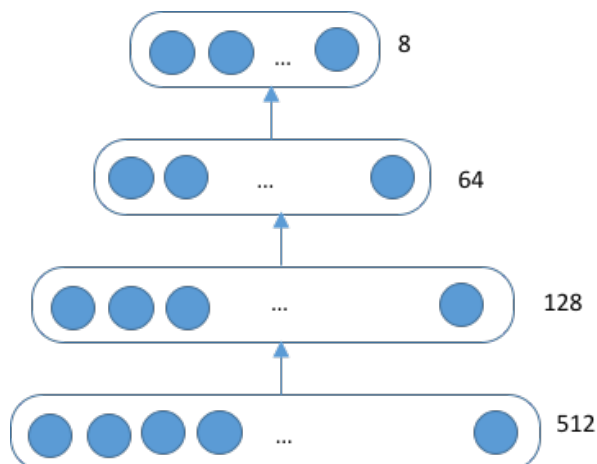
Consider a binary classifier implemented with a single neuron modelled by two weights $w_1=0.2$ and $w_2=0.8$ and a bias $b=-1$.

Consider the activation function to be a sigmoid $f(x) = 1 / (1+e^{-x})$.

- a) Draw a scheme of the model.
- b) Compute the output of the logistic regressor for a given input $x=[1,1]$.
- c) Considering a classification threshold of $y_{th}=0$ ($y_{th}>0$ for class A, and $y_{th}<0$ for class B), which class would be predicted for the considered input $x=[1,1]$?

Question 2 Multilayer Perceptron

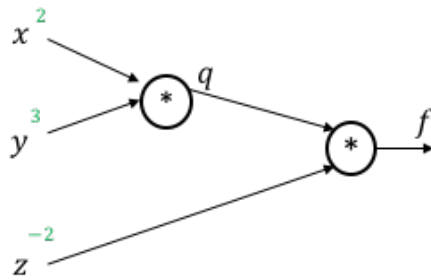
How many parameters do you need to compute in the following Multilayer Perceptron?
(justify your answer, indicate the operation you have to carry out)



Question 3 Backpropagation

Compute $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$ for the following Computational Graph

$$f(x, y, z) = (xy)z \quad (x=2, y=-3, z=-2)$$



Answer: (justify your answer)

- a) $\frac{\partial f}{\partial x} =$
- b) $\frac{\partial f}{\partial y} =$
- c) $\frac{\partial f}{\partial z} =$

Question 4 Optimization

Consider the following types of *critical points* of a smooth function where the gradient is a zero vector: a *minima* is a point where all eigenvalues of the Hessian are positive, and a *saddle point* is point at which there is at least one positive and one negative eigenvalue. Now, answer the following questions

- a) A numerical optimization technique to find the minima of a high dimensional function is more likely to encounter which of the two types of critical points? Give reason(s).

- b) Is finding the global minimum of a neural network's training loss function important? Give reason(s).

- c) Which one of the two escapes a saddle point more easily – gradient descent or stochastic gradient descent? Give reason(s).

Question 5 Convolutional Neural Networks

- a) A 2D convolutional network has an input of size $N \times N \times C$ (N = width, N = height, C channels). The first layer is a convolutional layer with K filters of size F , with stride 1 and padding P .

a1) Give a formula for the size of the feature maps

a2) Give a formula for the number of parameters

- b) What is the use of 1×1 convolutions?

- c) What is pooling, where is it used, and what is its purpose?

- d) Explain how the size of a feature map between two convolutional layers can be reduced just like pooling but without using pooling.

Question 6 Loss functions

Assume a network that has been trained to classify images into 3 classes. Consider the following three vectors when evaluating the network on a test image input.

$$(a) \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \quad (b) \begin{bmatrix} 2.0 \\ 1.0 \\ 0.1 \end{bmatrix} \quad (c) \begin{bmatrix} 0.7 \\ 0.2 \\ 0.1 \end{bmatrix} \quad (d) 0.3567$$

Justify which vector correspond to (A) the scores (logits) of the network, (B) The softmax output, (C) the one-hot encoding of the labels and (D) the cross-entropy loss

Question 7 Transfer Learning and domain adaptation

In a NN, explain the concept of finetuning, the advantages it offers over a full re-train on the target task. Explain also when it can be applied.