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1 The Standard Model of particle physics

The formulation of a relativistic quantum field theory and of spontaneous symmetry breaking (SSB) by the Brout-Englert-Higgs mechanism, allowed to built a theory which is capable to explain almost all observations of particle physics until today [1]. This theory is known as the Standard Model of particle physics (SM). The existence of its last missing piece, the Higgs boson, could be proven at the LHC in the year 2012 [2, 3].

The Standard Model is a $SU(3)_C \times SU(2)_L \times SU(1)_Y$ non-abelian gauge theory. “After” spontaneous symmetry breaking, its symmetries are reduced to $SU(3)_C \times U(1)_{EM}$. All particles that were found until today are contained in it¹. Furthermore, it is able to describe three of the four fundamental forces: the strong, weak and electromagnetic force.

In the following, a small introduction to the theory and phenomenology of the Standard Model is given. It is not meant as a complete description. The reader is referred to [4–6], for a thorough and extensive introduction.

1.1 The particle content

It should be first noted, since the Standard Model is a quantum field theory, every field can be considered also as a particle and vice versa.

The Standard Model of particle physics contains three different particle types, or three different types of fields. First, there are the so-called “matter particles”, which are all spin 1/2 particles in the SM. Second, the forces are described by spin 1 vector bosons. And finally, in order to give masses to all particles the Standard Model embeds the Higgs boson, a scalar spin 0 particle.

Fermions in the Standard Model

The fermionic content can be further subdivided into leptons and quarks. In contrast to quarks, leptons are not strongly interacting, thus they only couple electromagnetically and weakly to other particles. Both, the quarks and the leptons are ordered into three different families. Across these families, all quantum numbers are conserved. They only differ by their mass.

¹One can argue, that the right-handed neutrino, which is proven to exist, is not contained. But as at least the left-handed neutrino is embedded, we want to ignore that for a moment.

Each family forms a $SU(2)_L$ doublet, which causes the coupling via the weak force. The right-handed partners form $SU(2)$ singlets, thus, don't couple via the weak interaction. As quarks carry one further quantum number, the colour, they are, additionally, grouped into $SU(3)_C$ triplets. All fermions form singlets under $U(1)_Y$ with different hypercharges.

Vector bosons in the Standard Model

As mentioned before, the vector bosons describe three of the four fundamental forces. There is one gauge boson corresponding to every generator of the above mentioned gauge groups. For $U(1)_Y$, it is the B_μ , for $SU(2)_L$, there are three gauge bosons $W_\mu^{1,2,3}$ and finally eight gauge bosons $G_\mu^{1\dots 8}$ for $SU(3)_C$, which are called gluons. As the B -field and the neutral W_μ^3 -field can mix, "after" SSB the basis can be changed and lead to the well known photon and Z -boson.

The Higgs boson

A somehow extraordinary role plays the Higgs boson, that was predicted already 50 years ago by Peter Higgs [7, 8] and could be proven existent by the LHC experiments CMS and Atlas in 2012 [2, 3]. This particle is a consequence of the spontaneous symmetry breaking after rotating three of the four degrees of freedom to masses of the W - and Z -bosons. It is the only known fundamental scalar particle.

An overview of all Standard Model particles and their transformation properties are shown in Table 1.1. If particles transform as singlet under $SU(2)_L$ or $SU(3)_C$, they don't couple via the corresponding force. The hypercharges Y are determined by $Q = Y + I_3$, where Q is the electric charge and I_3 is the third component of the weak isospin with $I^a = \sigma^a/2$ (σ^a are the Pauli matrices).

1.2 The Lagrangian density

In particle physics, the probability of a decay or an interaction between particles can be calculated with the help of the Lagrangian density. The Lagrangian density of the Standard Model is the smallest set of possible Lagrangian terms, that are renormalisable and contain all up to date known particles as well as the above mentioned gauge symmetries.

Table 1.1: All particles contained in the Standard Model and their transformation properties under $SU(3)_C \times SU(2)_L \times SU(1)_Y$.

	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$
Fermions:			
$(\nu_L, e_L)^T$	1	2	-1
e_R	1	1	-2
$(u_L, d_L)^T$	3	2	$+\frac{1}{3}$
u_R	3	1	$+\frac{4}{3}$
d_R	3	1	$-\frac{2}{3}$
Vector bosons:			
B_μ	1	1	0
W_μ^a	1	3	0
G_μ^a	8	1	0
Higgs boson: H	1	2	-1

73 It is the following:

$$\begin{aligned}
\mathcal{L} = & (D_\mu \Phi)^\dagger (D^\mu \Phi) - \mu^2 \Phi^\dagger \Phi - \frac{\lambda}{4} (\Phi^\dagger \Phi)^2 \\
& + \bar{L}_i^L i \not{D} L_i^L + \bar{e}_i^R i \not{D} e_i^R + \bar{Q}_{ib}^L i \not{D} Q_{ib}^L + \bar{u}_{ib}^R i \not{D} u_{ib}^R + \bar{d}_{ib}^R i \not{D} d_{ib}^R \\
& - \left(Y_{ij}^e \bar{L}_i^L \Phi e_j^R + Y_{ij}^u \bar{Q}_{ib}^L \Phi^c u_{jb}^R + Y_{ij}^d \bar{Q}_{ib}^L \Phi d_{jb}^R + h.c. \right) \\
& - \frac{1}{4} (B_{\mu\nu} B^{\mu\nu} + W_{\mu\nu}^a W^{a\mu\nu} + G_{\mu\nu}^a G^{a\mu\nu}),
\end{aligned} \tag{1.1}$$

74 with $\not{D} = \gamma_\mu D^\mu$ and the covariant derivative $D^\mu = \partial^\mu + ig' Y_W B^\mu - ig C_1 I^a W_a^\mu - ig_S C_2 T^a G_a^\mu$.
75 I^a and T^a denote hereby the generators of the $SU(2)_L$ and $SU(3)_C$, respectively. They
76 are connected to the three Pauli matrices and the eight Gell-Mann matrices by $I^a = \frac{\sigma^a}{2}$
77 and $T^a = \frac{\lambda^a}{2}$. Adding the hypercharge Y_W and the third component of the weak isospin
78 result in the electrical charge $Q = Y_W + I_3$. Furthermore, it is $C_1 = 1$ for doublets and
79 $C_1 = 0$ for singlets under $SU(2)_L$, $C_2 = 1$ for triplets and $C_2 = 0$ for singlets under $SU(3)_C$.

80 The first line in Eq. (1.1) correspond to the kinetic terms of the Higgs field and its
81 potential. Via this Higgs field, it is possible to give masses to the Z - and W^\pm -bosons as well

as the fermions. This will be explained in detail in the following Section 1.3. The second line describes the kinetic terms of the leptons and quarks. The index i represents the three different families ($i = 1, 2, 3$). Since they are spin 1/2 particles, they can be described with the help of Dirac spinors. The left-handed leptons and quarks are described as $SU(2)_L$ doublets, $L_I^L = (\nu_{eL}, e_L)_i$, $Q_I^L = (u_L, d_L)_i$, the right-handed as singlets under $SU(2)_L$ e_i^R , u_i^R , d_i^R . Quarks carry a further quantum number, the colour, which is indicated by the index b with $b = 1, 2, 3$. Quarks transform as triplets under the $SU(3)_C$ gauge group. The third line contains the interaction terms between the fermions and the Higgs boson, called Yukawa interactions. These terms lead after SSB to the fermion mass terms, as can be seen later. The last line correspond to the kinetic terms of the gauge fields. These are connected to the field strength tensors by

$$\begin{aligned}
B^{\mu\nu} &\equiv \partial^\mu B^\nu - \partial^\nu B^\mu \\
W^{\mu\nu} &\equiv \partial^\mu W^\nu - \partial^\nu W^\mu - ig [W^\mu, W^\nu] \\
&= \left(\partial^\mu W_i^\nu - \partial^\nu W_i^\mu + g \epsilon_{ijk} W_j^\mu W_k^\nu \right) \frac{\sigma_i}{2} \equiv \frac{\sigma_i}{2} W_a^{\mu\nu} \\
G^{\mu\nu} &\equiv \partial^\mu G^\nu - \partial^\nu G^\mu - ig_S [G^\mu, G^\nu] \\
&= \left(\partial^\mu G_a^\nu - \partial^\nu G_a^\mu + g_S f_{abc} G_b^\mu G_c^\nu \right) \frac{\lambda_a}{2} \equiv \frac{\lambda_a}{2} G_a^{\mu\nu}.
\end{aligned} \tag{1.2}$$

The factors ϵ_{ijk} and f_{abc} are hereby the structure constants of the corresponding lie groups. The summation over all indices that appear twice is included.

1.3 The Brout-Englert-Higgs mechanism

An essential ingredient of the Standard Model is the Brout-Englert-Higgs mechanism (BEH mechanism), earlier also called Higgs mechanism. It was developed by Peter Higgs, Robert Brout and François Englert in 1960s [7–12]. Based on a work from Sheldon Glashow [13], Steven Weinberg and Abdus Salam later applied it on a $SU(2) \times U(1)$ gauge theory [14,15]. By this, a renormalisable theory of the weak and the electromagnetic theory was born. Together with the theory of strong interaction, the Standard Model was thus by this time completely formulated by the theory.

Mass terms of the gauge bosons

Due to the BEH mechanism, it is possible to give masses to the W^\pm - and Z-bosons. A scalar field Φ (Higgs field) is required, which has a non-zero vacuum expectation value. This is possible, when the mass parameter μ in front of the bilinear term in line one of Eq. (1.1) is smaller than zero and $\lambda > 0$ at the same time.

The resulting potential of the Higgs field is then the famous “Mexican hat” potential.

Expanding the Lagrangian density around the minimum of $\Phi = (0, v)$, the gauge symmetries of $SU(2)_L \times U(1)_Y$ are spontaneously broken and only a remaining electrical charge conserving symmetry $U(1)_{EM}$ remains. After an unitary transformation, three of the four degrees of freedom of the Higgs field are absorbed by the gauge fields. Thus, “after” SSB, the part of the Lagrangian containing the scalar field is as follows

$$\mathcal{L}_{Higgs} = \frac{1}{2} (\partial_\mu \phi^0)^\dagger (\partial^\mu \phi^0) - \mu^2 (\phi^0)^2 + \frac{1}{2} v^2 g^2 W_\mu^- W^{+\mu} + \frac{1}{4} v^2 (g^2 + g'^2) Z_\mu Z^\mu + \text{interaction terms} \quad (1.3)$$

One kinetic and one mass term for one of the degrees of freedom of the Higgs fields remains, which is the Higgs boson (ϕ^0). Furthermore, three of the four gauge bosons require a mass. The remaining gauge boson, being the photon remains massless because of the conserved $U(1)_{EM}$ gauge symmetry. The mass eigenstates of the gauge bosons in Eq. (1.3) are obviously different to the interaction eigenstates in Eq. (1.1).

The diagonalisation of the neutral mass matrices is described by the Weinberg angle θ_W

$$\begin{pmatrix} A_\mu \\ Z_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta_W & -\sin \theta_W \\ \sin \theta_W & \cos \theta_W \end{pmatrix} \begin{pmatrix} B_\mu \\ W_\mu^3 \end{pmatrix}. \quad (1.4)$$

For the charged gauge bosons, the relation between $W_{1,2}$ and W^\pm is the following

$$W_\mu^\pm = \frac{1}{\sqrt{2}} [W_\mu^1 \mp W_\mu^2]. \quad (1.5)$$

Consequently, the masses of the gauge boson are the following

$$\begin{aligned} M_H &= \sqrt{2}\mu \\ M_W &= \frac{g}{\sqrt{2}} v \\ M_Z &= \frac{1}{\sqrt{2}} v \sqrt{g^2 + g'^2} \\ M_\gamma &= 0. \end{aligned} \quad (1.6)$$

The first direct observation of the Z - and W^\pm -bosons was made in $p\bar{p}$ -collisions in the year 1983 at the Super Proton Synchrotron (SPS) at CERN [16, 17]. The experimental values of the masses are $m_Z = 91.1876 \pm 0.0021$ GeV and $m_{W^\pm} = 80.385 \pm 0.015$ GeV [18]. Finally, as mentioned several times before, the Higgs boson was found at the LHC in the year 2012 [2, 3]. The mass is measured to $m_{h^0} = 125.09 \pm 0.21(\text{stat.}) \pm 0.11(\text{sys.})$ GeV [19].

128 Mass terms of the fermions

129 Fermion mass terms cannot be easily inserted into the Lagrangian density in Eq. (1.1),
 130 since they would violate the imposed gauge symmetries. With the help of the BEH
 131 mechanism it is possible to generate fermion mass terms via the Yukawa interactions terms
 132 (line three of Eq. (1.1)). After spontaneous symmetry breaking, the Yukawa interactions
 133 lead to the following mass terms (colour indices are suppressed)

$$\begin{aligned} \mathcal{L}_{Yukawa} = & - \left(Y_{ij}^e v \bar{e}_i^L e_j^R + Y_{ij}^u v \bar{u}_i^L u_j^R + Y_{ij}^d v \bar{d}_i^L d_j^R + h.c. \right) \\ & + \text{interaction terms} \end{aligned} \quad (1.7)$$

134 The fermion masses are thus described by the following mass matrices

$$M_{ij}^e = Y_{ij}^e v \quad M_{ij}^u = Y_{ij}^u v \quad M_{ij}^d = Y_{ij}^d v \quad (1.8)$$

135 Since the Standard Model does not contain right-handed neutrinos, there are no gauge
 136 invariant Yukawa interactions, that could produce mass terms for neutrinos.

137 1.4 Limitations of the Standard Model

138 Despite the great success of the Standard Model, there remain observations and theoret-
 139 ical considerations that cannot be answered within the SM. In the following, the most
 140 important of such “limitations” shall be reviewed.

141
 142 First of all, the Standard Model suffers of the so-called hierarchy problem. By this,
 143 the problem is addressed that the higgs mass is not protected from getting large radiative
 144 corrections to the bare mass ($m_{h^0}^{\text{bare}2}$). The bare mass refers to the parameter of the
 145 higgs mass in the Lagrangian density. It becomes infinite when calculating higher order
 146 contributions to the measured mass. The appearance of infinities, on the other hand, is
 147 not unusual in particle physics and can be mathematically be handled by the concept of
 148 renormalisation. Still, in particle physics ... look it up at home!

$$m_H^{\text{ren}2} = m_H^{\text{bare}2} + \Delta m_H^2. \quad (1.9)$$

149 The most striking shortcoming of the Standard Model is the missing fourth fundamen-
 150 tal force, the gravitacional force. Within the SM, it is not possible to add renormalisable
 151 terms, that can describe the gravitational force. Although, gravity is not important for
 152 particle physics at energies that are accesible at current particle colliders (it only becomes
 153 important at the Planck scale $\sim 10^{19}$ GeV), the fact that it cannot be embedded into
 154 the Standard Model leads to an understanding of the SM as effective theory, only valid

for lower energies. Thus, it is obviously not an ultimate theory and something must be beyond.

Furthermore, there is experimental evidence, which cannot be explained within the Standard Model.

Astrophysical observations suggest that there is a large amount of dark matter (DM) in the universe, that cannot be explained with the particle content of the Standard Model. Measurements of the velocity curves of galaxies, e. g. M33 [20] show discrepancies between the observed velocities and the predicted velocities by the visible matter. The share of non-visible matter to the total amount of energy in the universe is estimated to be 27% [?]. In comparison, baryonic matter contributes only by $\sim 5\%$ to the total amount of energy in the universe. Unfortunately, there is no suitable (only weakly interacting) candidate within the SM, that can make up the full DM contribution.

Finally, the so-called baryon-antibaryon asymmetry is not explainable within the SM. The only source for CP-violation, which is needed to give rise to a matter-antimatter asymmetry is contained via the CKM matrix, which appears in the SM due to the weak interaction in the quark sector. The complex phase in this matrix is however a tiny number, not able to explain such an asymmetry.

There are far more questions, not all addressed. The reader is referred to [1] to get a much detailed overview about the limitations of the SM.

In the following Section 2, a theory is introduced, that can address most of the above mentioned problems. This theory is called Supersymmetry.

2 Supersymmetry

Supersymmetry was developed by xxx.

2.1 The MSSM

The MSSM is the specific model

2.1.1 The particle content of the MSSM

Phenomenology

183 **2.1.2 The phenomenological MSSM**

184 Simple assumptions

185 **2.2 Long-lived particles in the pMSSM**

186 Now explain why they can be lon-lived.

187 **2.3 Supersymmetry breaking**

188 This will be very short

189 **2.3.1 Gauge mediation**

190 **2.3.2 Gravity mediation**

191 **2.3.3 Anomaly-mediated breaking**

192 **3 Long-lived particles in the MSSM**

- 193 • Mechanism of long lifetimes

194 **3.1 Previous searches for long-lived charged particles**

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