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1 The Standard Model of particle physics

The formulation of a relativistic quantum field theory and of spontaneous symmetry breaking (SSB) by the Brout-Englert-Higgs mechanism, allowed to built a theory which is capable to explain almost all observations of particle physics until today [1]. This theory is known as the Standard Model of particle physics (SM). The existence of its last missing piece, the Higgs boson, could be proven at the LHC in the year 2012 [2, 3].

The Standard Model is a $SU(3)_C \times SU(2)_L \times SU(1)_Y$ non-abelian gauge theory. “After” spontaneous symmetry breaking, its symmetries are reduced to $SU(3)_C \times U(1)_{EM}$. All particles that were found until today are contained in it¹. Furthermore, it is able to describe three of the four fundamental forces: the strong, weak and electromagnetic force.

In the following, a small introduction to the theory and phenomenology of the Standard Model is given. It is not meant as a complete description. The reader is referred to [4–6], for a thorough and extensive introduction.

1.1 The particle content

It should be first noted, since the Standard Model is a quantum field theory, every field can be considered also as a particle and vice versa.

The Standard Model of particle physics contains three different particle types, or three different types of fields. First, there are the so-called “matter particles”, which are all spin 1/2 particles in the SM. Second, the forces are described by spin 1 vector bosons. And finally, in order to give masses to all particles the Standard Model embeds the Higgs boson, a scalar spin 0 particle.

Fermions in the Standard Model

The fermionic content can be further subdivided into leptons and quarks. In contrast to quarks, leptons are not strongly interacting, thus they only couple electromagnetically and weakly to other particles. Both, the quarks and the leptons are ordered into three different families. Across these families, all quantum numbers are conserved. They only differ by their mass.

¹One can argue, that the right-handed neutrino, which is proven to exist, is not contained. But as at least the left-handed neutrino is embedded, we want to ignore that for a moment.

Each family forms a $SU(2)_L$ doublet, which causes the coupling via the weak force. The right-handed partners form $SU(2)$ singlets, thus, don't couple via the weak interaction. As quarks carry one further quantum number, the colour, they are, additionally, grouped into $SU(3)_C$ triplets.

Vector bosons in the Standard Model

As mentioned before, the vector bosons describe three of the four fundamental forces. There is one gauge boson corresponding to every generator of the above mentioned gauge groups. For $U(1)_Y$, it is the B_μ , for $SU(2)_L$, there are three gauge bosons $W_\mu^{1,2,3}$ and finally eight gauge bosons $G_\mu^{1\dots 8}$ for $SU(3)_C$, which are called gluons. As the B -field and the neutral W_μ^3 -field can mix, "after" SSB the basis can be changed and lead to the well known photon and Z -boson.

The Higgs boson

A somehow extraordinary role plays the Higgs boson, that was predicted already 50 years ago by Peter Higgs [7, 8] and could be proven existent by the LHC experiments CMS and Atlas in 2012 [2, 3]. This particle is a consequence of the spontaneous symmetry breaking after rotating three of the four degrees of freedom to masses of the W - and Z -bosons. It is the only known fundamental scalar particle.

An overview of all Standard Model particles and their transformation properties are shown in Table 1.1. If particles transform as singlet under $SU(2)_L$ or $SU(3)_C$, they don't couple via the corresponding force. The hypercharges Y are determined by $Q = Y + I_3$, where Q is the electric charge and I_3 is the third component of the weak isospin with $I^a = \sigma^a/2$ (σ^a are the Pauli matrices).

1.2 The Lagrangian density

In particle physics, the probability of a decay or an interaction between particles can be calculated with the help of the Lagrangian density. The Lagrangian density of the Standard Model is the smallest set of possible Lagrangian terms, that are renormalisable and contain all up to date known particles as well as the above mentioned gauge symmetries.

Table 1.1: All particles contained in the Standard Model and their transformation properties under $SU(3)_C \times SU(2)_L \times SU(1)_Y$.

	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$
Fermions:			
$(\nu_L, e_L)^T$	1	2	-1
e_R	1	1	-2
$(u_L, d_L)^T$	3	2	$+\frac{1}{3}$
u_R	3	1	$+\frac{4}{3}$
d_R	3	1	$-\frac{2}{3}$
Vector bosons:			
B_μ	1	1	0
W_μ^a	1	3	0
G_μ^a	8	1	0
Higgs boson: H	1	2	-1

70 It is the following:

$$\begin{aligned}
\mathcal{L} = & (D_\mu \Phi)^\dagger (D^\mu \Phi) - \mu^2 \Phi^\dagger \Phi - \frac{\lambda}{4} (\Phi^\dagger \Phi)^2 \\
& + \bar{L}_i^L i \not{D} L_i^L + \bar{e}_i^R i \not{D} e_i^R + \bar{Q}_{ib}^L i \not{D} Q_{ib}^L + \bar{u}_{ib}^R i \not{D} u_{ib}^R + \bar{d}_{ib}^R i \not{D} d_{ib}^R \\
& - \left(Y_{ij}^e \bar{L}_i^L \Phi e_j^R + Y_{ij}^u \bar{Q}_{ib}^L \Phi u_{jb}^R + Y_{ij}^d \bar{Q}_{ib}^L \Phi d_{jb}^R + h.c. \right) \\
& - \frac{1}{4} (B_{\mu\nu} B^{\mu\nu} + W_{\mu\nu}^a W^{a\mu\nu} + G_{\mu\nu}^a G^{a\mu\nu}),
\end{aligned} \tag{1.1}$$

71 with $\not{D} = \gamma_\mu D^\mu$ and the covariant derivative $D^\mu = \partial^\mu + ig' Y_W B^\mu - ig C_1 I^a W_a^\mu - ig_S C_2 T^a G_a^\mu$.
72 I^a and T^a denote hereby the generators of the $SU(2)_L$ and $SU(3)_C$, respectively. They are
73 connected to the three Pauli matrices and the eight Gell-Mann matrices by $I^a = \frac{\sigma^a}{2}$ and
74 $T^a = \frac{\lambda^a}{2}$. Adding the hypercharge Y_W and the third component of the weak isospin result
75 in the electrical charge $Q = Y_W + I_3$. Furthermore, it is $C_1 = 1$ for doublets and $C_1 = 0$
76 for singlets under $SU(2)_L$, $C_2 = 1$ for triplets and $C_2 = 0$ for singlets under $SU(3)_C$.

77 The first line in Eq. (1.1) correspond to the kinetic terms of the Higgs field and its
78 potential. Via this Higgs field, it is possible to give masses to the Z - and W^\pm -bosons as well

as the fermions. This will be explained in detail in the following Section 1.3. The second line describes the kinetic terms of the leptons and quarks. The index i represents the three different families ($i = 1, 2, 3$). Since they are spin 1/2 particles, they can be described with the help of Dirac spinors. The left-handed leptons and quarks are described as $SU(2)_L$ doublets, $L_I^L = (\nu_{eL}, e_L)_i$, $Q_I^L = (u_L, d_L)_i$, the right-handed as singlets under $SU(2)_L$ e_i^R , u_i^R , d_i^R . Quarks carry a further quantum number, the colour, which is indicated by the index b with $b = 1, 2, 3$. Quarks transform as triplets under the $SU(3)_C$ gauge group. The third line contains the interaction terms between the fermions and the Higgs boson, called Yukawa interactions. These terms lead after SSB to the fermion mass terms, as can be seen later. The last line correspond to the kinetic terms of the gauge fields. These are connected to the field strength tensors by

$$\begin{aligned}
B^{\mu\nu} &\equiv \partial^\mu B^\nu - \partial^\nu B^\mu \\
W^{\mu\nu} &\equiv \partial^\mu W^\nu - \partial^\nu W^\mu - ig [W^\mu, W^\nu] \\
&= \left(\partial^\mu W_i^\nu - \partial^\nu W_i^\mu + g \epsilon_{ijk} W_j^\mu W_k^\nu \right) \frac{\sigma_i}{2} \equiv \frac{\sigma_i}{2} W_a^{\mu\nu} \\
G^{\mu\nu} &\equiv \partial^\mu G^\nu - \partial^\nu G^\mu - ig_S [G^\mu, G^\nu] \\
&= \left(\partial^\mu G_a^\nu - \partial^\nu G_a^\mu + g_S f_{abc} G_b^\mu G_c^\nu \right) \frac{\lambda_a}{2} \equiv \frac{\lambda_a}{2} G_a^{\mu\nu}.
\end{aligned} \tag{1.2}$$

The factors ϵ_{ijk} and f_{abc} are hereby the structure constants of the corresponding lie groups. The summation over all indices that appear twice is included.

1.3 The Brout-Englert-Higgs mechanism

An essential ingredient of the Standard Model is the Brout-Englert-Higgs mechanism (BEH mechanism), earlier also called Higgs mechanism. It was developed by Peter Higgs, Robert Brout and François Englert in 1960s [7–12]. Based on a work from Sheldon Glashow [13], Steven Weinberg and Abdus Salam later applied it on a $SU(2) \times U(1)$ gauge theory [14,15]. By this, a renormalisable theory of the weak and the electromagnetic theory was born. Together with the theory of strong interaction, the Standard Model was thus by this time completely formulated by the theory.

Mass terms of the gauge bosons

Due to the BEH mechanism, it is possible to give masses to the W^\pm - and Z-bosons. A scalar field Φ (Higgs field) is required, which has a non-zero vacuum expectation value. This is possible, when the mass parameter μ in front of the bilinear term in line one of Eq. (1.1) is smaller than zero and $\lambda > 0$ at the same time.

The resulting potential of the Higgs field is then the famous “Mexican hat” potential.

Expanding the Lagrangian density around the minimum of $\Phi = (0, v)$, the gauge symmetries of $SU(2)_L \times U(1)_Y$ are spontaneously broken and only a remaining electrical charge conserving symmetry $U(1)_{EM}$ remains. After an unitary transformation, three of the four degrees of freedom of the Higgs field are absorbed by the gauge fields. Thus, “after” SSB, the part of the Lagrangian containing the scalar field is as follows

$$\mathcal{L}_{Higgs} = \frac{1}{2} (\partial_\mu \phi^0)^\dagger (\partial^\mu \phi^0) - \mu^2 (\phi^0)^2 + \frac{1}{2} v^2 g^2 W_\mu^- W^{+\mu} + \frac{1}{4} v^2 (g^2 + g'^2) Z_\mu Z^\mu + \text{interaction terms} \quad (1.3)$$

One kinetic and one mass term for one of the degrees of freedom of the Higgs fields remains, which is the Higgs boson (ϕ^0). Furthermore, three of the four gauge bosons require a mass. The remaining gauge boson, being the photon remains massless because of the conserved $U(1)_{EM}$ gauge symmetry. The mass eigenstates of the gauge bosons in Eq. (1.3) are obviously different to the interaction eigenstates in Eq. (1.1).

The diagonalisation of the neutral mass matrices is described by the Weinberg angle θ_W

$$\begin{pmatrix} A_\mu \\ Z_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta_W & -\sin \theta_W \\ \sin \theta_W & \cos \theta_W \end{pmatrix} \begin{pmatrix} B_\mu \\ W_\mu^3 \end{pmatrix}. \quad (1.4)$$

For the charged gauge bosons, the relation between $W_{1,2}$ and W^\pm is the following

$$W_\mu^\pm = \frac{1}{\sqrt{2}} [W_\mu^1 \mp W_\mu^2]. \quad (1.5)$$

Consequently, the masses of the gauge boson are the following

$$\begin{aligned} M_H &= \sqrt{2}\mu \\ M_W &= \frac{g}{\sqrt{2}} v \\ M_Z &= \frac{1}{\sqrt{2}} v \sqrt{g^2 + g'^2} \\ M_\gamma &= 0. \end{aligned} \quad (1.6)$$

The first direct observation of the Z - and W^\pm -bosons was made in $p\bar{p}$ -collisions in the year 1983 at the Super Proton Synchrotron (SPS) at CERN [16, 17]. The experimental values of the masses are $m_Z = 91.1876 \pm 0.0021$ GeV and $m_{W^\pm} = 80.385 \pm 0.015$ GeV [18]. Finally, as mentioned several times before, the Higgs boson was found at the LHC in the year 2012 [2, 3]. The mass is measured to $m_{h^0} = 125.09 \pm 0.21(\text{stat.}) \pm 0.11(\text{sys.})$ GeV [19].

125 Mass terms of the fermions

126 Fermion mass terms cannot be easily inserted into the Lagrangian density in Eq. (1.1),
 127 since they would violate the imposed gauge symmetries. With the help of the BEH
 128 mechanism it is possible to generate fermion mass terms via the Yukawa interactions terms
 129 (line three of Eq. (1.1)). After spontaneous symmetry breaking, the Yukawa interactions
 130 lead to the following mass terms (colour indices are suppressed)

$$\begin{aligned} \mathcal{L}_{Yukawa} = & - \left(Y_{ij}^e v \bar{e}_i^L e_j^R + Y_{ij}^u v \bar{u}_i^L u_j^R + Y_{ij}^d v \bar{d}_i^L d_j^R + h.c. \right) \\ & + \text{interaction terms} \end{aligned} \quad (1.7)$$

131 The fermion masses are thus described by the following mass matrices

$$M_{ij}^e = Y_{ij}^e v \quad M_{ij}^u = Y_{ij}^u v \quad M_{ij}^d = Y_{ij}^d v \quad (1.8)$$

132 Since the Standard Model does not contain right-handed neutrinos, there are no gauge
 133 invariant Yukawa interactions, that could produce mass terms for neutrinos.

134 1.4 Limitations of the Standard Model

135 Despite the great success of the Standard Model, there remain observations and theoret-
 136 ical considerations that cannot be answered within the SM. In the following, the most
 137 important of such “limitations” shall be reviewed.

138

139 First of all, the Standard Model suffers of the so-called hierarchy problem. By this,
 140 the problem is addressed that quadratic divergencies occur in the calculation of the Higgs
 141 self-coupling. The appearance of infinities is not uncommon in higher order calculations
 142 and happens for all particles. Still, for scalar particles the infinite term is quadratically
 143 divergent, which makes a huge difference compared to the logarithmic divergencies for
 144 fermion self-energies. When considering the Standard Model valid up to the Planck scale,
 145 an extraordinary fine-tuning would be needed to cancel a large bare mass with large
 146 counter terms

$$m_H^{\text{ren } 2} = m_H^{\text{bare } 2} + \Delta m_H^2. \quad (1.9)$$

147 to end up with a mass of 125 GeV. Thus, this renormalisation procedure, even if math-
 148 ematically possible, is regarded as highly unnatural in physics. The question which is
 149 usually imposed is, why is the Higgs mass so small, when there are such massive correc-
 150 tions to the bare mass? A formulation of naturalness was given by t’Hooft in 1977 [20].
 151 He stated, that a small parameter can be regarded only natural, if the symmetries of the
 152 theory are enhanced by setting this parameter to zero. In the Standard Model, though,

there is no enhancement of the symmetries of the Lagrangian by setting $\mu = 0$, thus the small mass of the Higgs boson compared to the Planck scale is considered as highly unnatural.

A further and probably the most striking shortcoming of the Standard Model is the missing fourth fundamental force, the gravitational force. Within the SM, it is not possible to add renormalisable terms, that can describe the gravitational force. Although, gravity is not important for particle physics at energies that are accessible at current particle colliders (it only becomes important at the Planck scale $\sim 10^{19}$ GeV), the fact that it cannot be embedded into the Standard Model leads to an understanding of the SM as effective theory, only valid for lower energies. Thus, it is obviously not an ultimate theory and something must be beyond.

Furthermore, in particle physics there is always the wish to describe nature with a theory as general as possible. This usually implies the effort to embed the Standard Model into a higher symmetry group. To achieve a simplification by unify the three fundamental forces usually done within so-called Grand-Unified-Theories (GUTs). Calculating the running of the coupling constants in the Standard Model, the couplings seems to match at a scale of $M_{\text{GUT}} \sim 10^{15}$ GeV. Unfortunately, they don't match exactly. Therefore, a unification is not achievable in the Standard Model under the assumption that there are no new particles up to the GUT scale.

Furthermore, there is experimental evidence, which cannot be explained within the Standard Model.

Astrophysical observations suggest that there is a large amount of dark matter (DM) in the universe, that cannot be explained with the particle content of the Standard Model. Measurements of the velocity curves of galaxies, e.g. M33 [21] show discrepancies between the observed velocities and the predicted velocities by the visible matter. The share of non-visible matter to the total amount of matter in the universe is estimated to be 84% [22]. Unfortunately, there is no suitable (only weakly interacting) candidate within the SM, that can make up the full DM contribution.

There are far more questions, not all addressed here. The reader is referred to [?] to get a more detailed overview about the limitations of the SM.

In the following Section 2, a theory is introduced, that can address most of the above mentioned problems. This theory is called Supersymmetry.

187 2 Supersymmetry

188 As noted in the last chapter, the Higgs boson mass suffers from quadratic divergencies
 189 through radiative corrections. The reason for the quadratic divergencies is due to the
 190 fact, that the Lagrangian density does not contain further symmetries for $\mu \rightarrow 0$. This
 191 behaviour is typical for scalar particles. For fermions, on the other hand, there is a
 192 further symmetry for $m_f = 0$. The Lagrangian density becomes invariant under chiral
 193 transformations of the form $\Psi \rightarrow e^{i\vec{\alpha}\frac{\vec{\sigma}}{2}\gamma_5}\Psi$. Although the mass terms of the fermions break
 194 this symmetry, it protects the fermions against large radiative corrections.

195 Due to these considerations, it seems natural to protect also the scalar mass by an
 196 additional symmetry. A work from Golfand and Likhtman in the year 1971 stated that
 197 an extension of the Poincaré algebra is possible via fermionic generators [23]. R. Haag,
 198 J. Lopuszanski and M. Sohnius finalised these considerations by showing that with the
 199 help of fermionic generators a connection between spacetime symmetries and internal
 200 symmetries is possible [24]. The extensions of a symmetry group by fermionic generators
 201 is called Supersymmetry (SUSY). These were the foundation of supersymmetric theories.

202
 203 In the following, few aspects of supersymmetric theories are discussed. For a detailed
 204 introduction the reader is referred to [25–27].

205 In the subsequent sections, the descriptions is restricted to the case of $N = 1$ supersym-
 206 metry, i. e. there is only one supersymmetric generator and thus only one supersymmetric
 207 partner for every particle. A supersymmetric transformation transfers every bosonic state
 208 into a fermionic state and vice versa

$$\begin{aligned} Q |\text{boson}\rangle &= |\text{fermion}\rangle \\ Q |\text{fermion}\rangle &= |\text{boson}\rangle. \end{aligned} \tag{2.1}$$

209 The most important (anti-) commutation relations for SUSY algebra with spinors Q are

$$\begin{aligned} \{Q_\alpha, Q_\beta\} &= \{Q_\alpha^\dagger, Q_\beta^\dagger\} = 0, \\ [Q_\alpha, P_\mu] &= [Q_\alpha^\dagger, P_\mu] = 0, \\ \{Q_\alpha, Q_\alpha^\dagger\} &= 2\sigma_{\alpha\dot{\alpha}}^\mu P_\mu. \end{aligned} \tag{2.2}$$

210 P_μ denotes hereby the four component generator of translations. Additionally, it is $\sigma^\mu =$

211 $(\mathbb{1}, \sigma_i)$ with the pauli matrices σ_i . From the second relation in (2.2) it follows

$$[Q_\alpha, P^2] = [Q_\alpha^\dagger, P^2] = 0. \quad (2.3)$$

212 Equation 2.3 implies, that particles that are transformed into each other with the gen-
 213 erator Q need to have same eigen values of P^2 , thus, also same masses. This impose
 214 obvioulsy a problem, since no “scalar electron” was ever found with a mass of 0.512 MeV.
 215 This problem will be discussed later.

216

217 In Supersymmetry, all particles and their partner particles are discribed by so-called
 218 supermultiplets. Since the generators of the gauge group commute with the generators
 219 of supersymmetry, all particles within one supermultiplet have same quantum numbers,
 220 besides the spin (as shown in Eq. 2.3 they have also same masses). In a renormalisable
 221 theory, there are two different types of supermultiplets: chiral multiplets, which contain a
 222 two-component Weyl spinor and a complex scalar field and vector mulitplets with a vector
 223 boson and a two-component Weyl spinor. With this, the number of degrees of freedom
 224 are for chiral multiplets for on-shell particles

$$\begin{aligned} n_f &= 2, \text{ due to the two-component Weyl spinor} \\ n_b &= 2, \text{ due to the complex scalar field,} \end{aligned}$$

225 and for vector multiplets for on-shell particles

$$\begin{aligned} n_f &= 2, \text{ due to the two-component Weyl spinor} \\ n_b &= 2, \text{ due to the vector field.} \end{aligned}$$

226 As mentioned before, in a realistic extension of the Standard Model, Supersymmetry
 227 cannot be exact, since no supersymmetric particles have been found which have the same
 228 masses as their SM partners. This implies, that SUSY must be broken. There are many
 229 ideas how the breaking can work. However, as up to now, little is known about the extact
 230 breaking mechanism, usually one add by hands term to the Langrangian which breaks
 231 SUSY explicetly. These terms paramterise SUSY breaking without knowing how this
 232 actually can occure. One condition is however imposed on the supersymmetry breaking
 233 terms: they should not spoil the naturalness of the new theory, i. e. no new quadartaic
 234 dievergencies shall occur by these terms. Therefore, they are called sof-breaking terms.
 235 How they actually look, will be explained in the Section 2.1.

236 Finally, it shall be discussed how Supersymmetry can give possible answers to the short-
 237 comings of the Standard Model, discussed in Section 1.4.

238 Radiative corrections by fermions always have a factor -1 compared to bosonic correc-
 239 tions. Thus, calculating radiative corrections of the Higgs boson mass in a supersymmetric

theory leads in addition to the corrections by SM particles also the corrections by SUSY particles. If SUSY were exact, the quadratic divergencies Δm_H^2 would exactly cancel. However, as argued, SUSY must be broken. The cancellation of quadratic divergencies can therefore only be assured, if the breaking is not too drastic and only logarithmic divergencies remain. To avoid a new source of fine-tuning, the soft-breaking parameters should be of the order $M_{\text{soft}} \sim 100 \text{ GeV} - 1000 \text{ GeV}$.

Even though, it is not possible to implement the gravity within a supersymmetric extension of the Standard Model, all possible theories that are able to include gravity (string theory) include also Supersymmetry.

The renormalisation group equations change under a supersymmetric extension of the Standard Model. By this, a unification of the gauge couplings at a GUT scale of about 10^{16} GeV is possible, as can be seen in Fig. 2.1. It can be nicely seen, that all three gauge couplings cross each other within the uncertainties.

Besides these arguments, SUSY can also give an answer to the problem of non-visible matter in the universe. If the conservation of the so-called parity is required, the lightest supersymmetric particle (LSP) is stable. If this particle is only weakly interacting, it can serve as a good candidate to explain fully or partly the sources of the relic density. R-parity is a multiplicative quantum number with

$$\begin{aligned} P_R &= 1 & \text{SM particles} \\ P_R &= -1 & \text{SUSY particles.} \end{aligned}$$

If R-parity is conserved, only terms are allowed in the Lagrangian density, that contain an even number of supersymmetric particles. Therefore, no single SUSY particle can decay into only SM particles and thus, the LSP is stable.

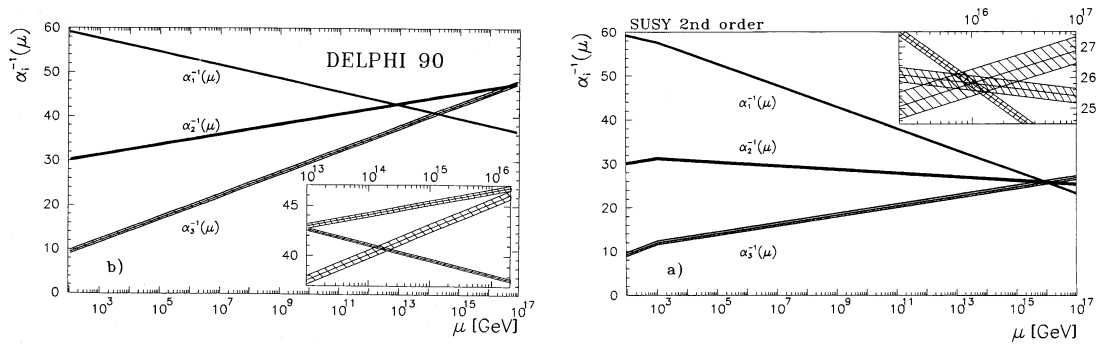


Figure 2.1: The running of the gauge couplings in the Standard Model (left) and in the minimal supersymmetric extension of the SM (right). Taken from [28].

2.1 The MSSM

The supersymmetric extension of the Standard Model with a minimal particle content is called the Minimal Supersymmetric Standard Model (MSSM). In the following section, the particle content of the MSSM is introduced.

2.1.1 The particle content of the MSSM

In $N = 1$ Supersymmetry, every SM particle has exactly one supersymmetric partner particle, which leads to a doubling of the particle content in the MSSM compared to the SM. Additionally, there is a necessity for a second Higgs doublet. The second doublet is needed to ensure the holomorphy of the superpotential when also mass terms for the up-type particles shall be created. Furthermore, the MSSM stays only free from anomalies if there is a further Higgs doublet. This leads to the fact, that in the MSSM, there are five Higgs bosons instead of only one as in the SM. The complete particle content of the MSSM is depicted in Tables ?? and ??.

Table 2.1: Chiral supermultiplets in the MSSM

		spin 0	spin $\frac{1}{2}$	$SU(3)_C, SU(2)_L, U(1)_Y$
squarks/quarks	Q	$(\tilde{u}_L, \tilde{d}_L)$	(u_L, d_L)	3, 2, $\frac{1}{3}$
	\bar{u}	$\tilde{\bar{u}}_L = \tilde{u}_R^\dagger$	$\bar{u}_L = (u_R)^c$	$\bar{3}, 1, -\frac{4}{3}$
	\bar{d}	$\tilde{\bar{d}}_L = \tilde{d}_R^\dagger$	$\bar{d}_L = (d_R)^c$	$\bar{3}, 1, \frac{2}{3}$
sleptons/leptons	L	$(\tilde{\nu}_{eL}, \tilde{e}_L)$	(ν_{eL}, e_L)	1, 2, -1
	\bar{e}	$\tilde{\bar{e}}_L = \tilde{e}_R^\dagger$	$\bar{e}_L = (e_R)^c$	$\bar{1}, 1, 2$
higgs/higgsinos	H_u	(H_u^+, H_u^0)	$(\tilde{H}_u^+, \tilde{H}_u^0)$	1, 2, 1
	H_d	(H_d^0, H_d^-)	$(\tilde{H}_d^0, \tilde{H}_d^-)$	1, 2, -1

Since in supersymmetric theories only left-handed Weyl spinors appear in the Lagrangian density, the right-handed are described as charge conjugated spinors of the left-handed spinors.

Table 2.2: Vector supermultiplets in the MSSM

	spin $\frac{1}{2}$	spin 0	$SU(3)_C, SU(2)_L, U(1)_Y$
gluinos/gluons	\tilde{g}	g	8, 1, 0
winos/ W -bosons	$\tilde{W}^\pm, \tilde{W}^0$	W^\pm, W^0	1, 3, 0
bino/ B -boson	\tilde{B}	B	1, 1, 0

2.1.2 The Lagrangian density of the MSSM

In the following only the most important parts of the MSSM Lagrangian density will be described. The reader is again referred to [?] for a complete description of the Lagrangian density.

The superpotential

The superpotential of the MSSM contains the self interaction terms of the Higgs bosons and generates the interaction terms of the Higgs bosons with the fermions and their super partners. As already noted, it is very common to assume R-parity conservation. Thereby, no terms appear in the Lagrangian that would violate lepton or baryon number conservation and the lightest supersymmetric particle is stable. Thus, all possible terms are

$$W_{\text{MSSM}} = \mu H_u \cdot H_d - Y_u^{ij} H_u \cdot Q_L^i u_R^{cj} + Y_d^{ij} H_d \cdot Q_L^i d_R^{cj} + Y_e^{ij} H_d \cdot L_L^i e_R^{cj}, \quad (2.4)$$

with the dot product defined as in []

$$A \cdot B = \epsilon^{\alpha\beta} A_\alpha B_\beta = A_1 B_2 - A_2 B_1. \quad (2.5)$$

The soft-breaking Lagrangian density

Since Supersymmetry is broken, explicit SUSY breaking terms are added to the Lagrangian density. In order not to introduce new sources of quadratic divergencies, only bilinear and

291 bilinear terms appear in the soft-breaking Lagrangian

$$\begin{aligned}
-\mathcal{L}_{soft}^{MSSM} = & m_{H_u}^2 H_u^\dagger \cdot H_u + m_{H_d}^2 H_d^\dagger \cdot H_d + (B\mu H_u \cdot H_d + h.c.) \\
& + m_{\tilde{Q}}^2 \tilde{Q}_{Li}^\dagger \cdot \tilde{Q}_{Lj} + m_{\tilde{u}}^2 \tilde{u}_{Ri}^{c\dagger} \cdot \tilde{u}_{Rj}^c + m_{\tilde{d}}^2 \tilde{d}_{Ri}^{c\dagger} \cdot \tilde{d}_{Rj}^c \\
& + m_{\tilde{L}}^2 \tilde{L}_{Li}^\dagger \cdot \tilde{L}_{Lj} + m_{\tilde{e}}^2 \tilde{e}_{Ri}^{c\dagger} \cdot \tilde{e}_{Rj}^c \\
& + \left(-(A_u Y_u)_{ij} H_u \cdot \tilde{Q}_{Li} \tilde{u}_{Rj}^c + (A_d Y_d)_{ij} H_d \cdot \tilde{Q}_{Li} \tilde{d}_{Rj}^c \right. \\
& \left. + (A_e Y_e)_{ij} H_d \cdot \tilde{L}_{Li} \tilde{e}_{Rj}^c + h.c. \right) \\
& + \left(M_1 \tilde{B} \tilde{B} + M_2 \tilde{W}_a \tilde{W}_a + M_3 \tilde{g}_i \tilde{g}_i + h.c. \right)
\end{aligned} \tag{2.6}$$

292 The first line contains mass terms for the Higgs bosons, the second and third line for the
 293 sfermions. In the fourth and fifth line the trilinear couplings between the Higgs bosons
 294 and the sfermions appear. Finally, the last line give rise to mass terms for the gauginos.

295 Because of the soft-breaking terms, the MSSM contains more than 100 free parameters.
 296 Constraining the MSSM is thus a difficult task and usually in experimental particle physics,
 297 constrained versions of the MSSM or assumptions at the GUT scale are used to report the
 298 impact of searches on SUSY. In the following a short introduction of the phenomenological
 299 MSSM is given. With its reduced parameter space it allows to elaborate on long-lived
 300 particles in the MSSM in a much easier way.

301 2.1.3 The phenomenological MSSM

302 The phenomenological MSSM (pMSSM) imposes constraints that are reasonable in the
 303 sense to fulfill current observations and still keep the phenomenological richness of the
 304 MSSM [29]. The following assumptions are imposed (in [29] more detailed information
 305 about these assumptions can be found):

- 306 • No new sources of CP violation,
- 307 • No flavour changing neutral currents,
- 308 • First and second generation universality.

309 These assumption reduce the number of new parameters to only 19. The remaining free
 310 parameters are the following:

- 311 • $\tan \beta$ (the ratio of the vacuum expectation values of the two Higgs doublets)
- 312 • M_A (the mass of the pseudo-scalar Higgs boson)
- 313 • μ (the Higgs mass parameter)
- 314 • M_1, M_2, M_3 (bino, wino and gluino mass parameters, respectively)

- 315 • $m_{\tilde{q}}, m_{\tilde{l}}, m_{\tilde{u}}, m_{\tilde{d}}$ and $m_{\tilde{e}}$ (the first and second generation mass parameters)
- 316 • $m_{\tilde{Q}}, m_{\tilde{L}}, m_{\tilde{t}}, m_{\tilde{b}}$ and $m_{\tilde{\tau}}$ (the third generation mass parameters)
- 317 • A_t, A_b and A_{τ} (third generation trilinear couplings).

318 2.2 Supersymmetry breaking

319 As already noted, the mechanism of supersymmetry breaking is unknown. There exists
 320 however, several ideas how to spontaneously break supersymmetry. All mechanisms have
 321 in common that they need to happen at high energies in a hidden sector. “Messenger”
 322 particles are introduced which mediate the breaking to the TeV scale. This, however,
 323 implies that supersymmetry breaking is a question of high-energy physics and one can
 324 always parametrise the breaking by the soft breaking terms introduced in Section 2.1.2.

325 The most popular breaking mechanism is gravity mediated Supersymmetry breaking [?]
 326 and gauge-mediated supersymmetry breaking [?].

327 3 Long-lived particles in the MSSM

- 328 • Mechanism of long lifetimes

329 3.1 Previous searches for long-lived charged particles

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