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## **Part 1**

22

**Measurement of the jet**

23

**transverse-momentum resolution**



## 1.1 Introduction

The determination and quantification of the quality of the jet transverse-momentum measurement is of crucial interest for many analyses with jet final states, e. g. the measurement of the dijet cross section [1] or  $t\bar{t}$  production cross sections [2]. Also searches for physics beyond the Standard Model with missing transverse momentum,  $\cancel{p}_T$ , in the final state rely on a good understanding of  $\cancel{p}_T$  originating from wrongly measured jets [3–5]. It is therefore important to determine the jet transverse-momentum resolution, i. e. the detector resolution of the jet  $p_T$  measurement. For analyses relying on information from simulation, it is necessary to correct the simulated resolution to the resolution actually present in data. Therefore, scale factors will be presented to adjust the resolution in simulation to the resolution of the real detector.

In the following sections, a data-based method to measure the jet  $p_T$  resolution in  $\gamma$ +jet events will be presented. A similar method was already applied in earlier analyses [6, 7] of 7 TeV data. It is further developed here and applied to  $19.7 \text{ fb}^{-1}$  of  $\sqrt{s} = 8 \text{ TeV}$  data.

The method is based on the transverse-momentum balance in the  $\gamma$  + jet system. It takes advantage of the high resolution of the electromagnetic calorimeter and hence the excellent measurement of the photon momentum. Without initial and final state radiation, the photon and the jet are balanced in the transverse plane. Thus, measuring the photon  $p_T$  with high accuracy leads to an accurate estimate of the true jet transverse momentum and offers a possibility to quantify the resolution of jet  $p_T$  measurements.

## 1.2 General approach of the resolution measurement using photon+jet events

The quality of the jet transverse-momentum measurement is determined by the jet transverse-momentum response  $\mathcal{R}$ , i. e. by the ratio of the reconstructed to the true jet transverse momentum

$$\mathcal{R} = \frac{p_{\text{T}}^{\text{reco. jet}}}{p_{\text{T}}^{\text{true jet}}}. \quad (1.1)$$

Because of the limited detector resolution, the reconstructed jet  $p_T$  in general differs from the true jet  $p_T$  resulting in a distribution of  $\mathcal{R}$ . In Fig 1.1 (left), an exemplary distribution of  $\mathcal{R}$  in simulation (where the true jet  $p_T$  corresponds to the generator-level jet  $p_T$ ) is depicted. The jet transverse-momentum resolution ( $\text{JER}^1$ ) is defined as the width of the distribution while the mean corresponds to the so-called jet transverse-momentum scale (JES) [8].

It can be seen in Fig. 1.1 (left), that the core of the response distribution shows a typical Gaussian behaviour whereas the tails deviate from that functional form. Physical reasons for the pronounced low response tail are, inter alia, semi-leptonic decays of heavy quarks (c- and b-quarks) where the neutrino cannot be detected and the reconstructed transverse momentum of the jet is too small. This effect is visible in Fig. 1.1 (right) which depicts the response distribution including all jet flavours (blue), as well as the contribution by c- and b-quarks (red), which is the main contribution to the pronounced left tail. Some instrumental effects, such as a non-linear response of the calorimeter, inhomogeneities of the detector material and electronic noise can contribute to both tails, others, like dead calorimeter channels only contribute to the left tail [9].

In order to avoid the coverage of non-Gaussian tails, the resolution is determined using only the core of the response distribution. The resolution is thus defined as the standard

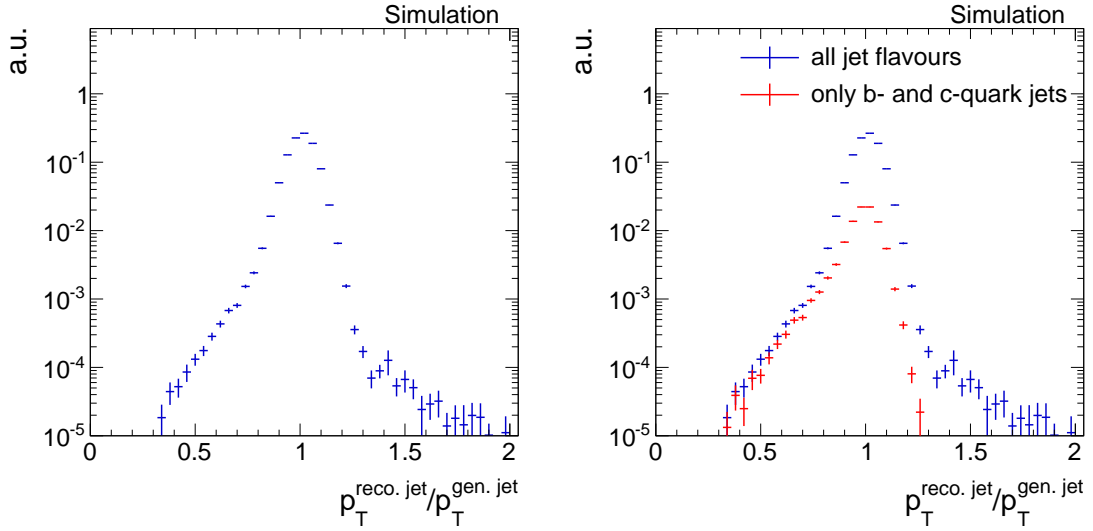


Figure 1.1: Left: Normalised number of events over  $p_T^{\text{reco. jet}}/p_T^{\text{gen. jet}}$  from a simulated  $\gamma$ +jet sample. Right: The response distribution containing all jet flavours (blue) and the contribution by c- and b-quark jets (red).

<sup>1</sup>This abbreviation is a historical relic from experiments where the momentum of jets were only measured in the calorimeters and therefore JER referred to jet energy resolution.

deviation of the 99% truncated response histogram divided by the mean [10]:

$$\sigma_{\text{JER}} = \frac{\sigma_{99\%}}{\mu_{99\%}}.$$

The division by the mean aims at making the resolution independent of the absolute scale (= mean) of the response distribution.

The determination of the 99% range of the histogram is done in several steps. First the mean of the core is found via a Gaussian fit to the histogram in a  $2\sigma$  range<sup>2</sup>. This procedure is done in three iteration steps. Then, a symmetric interval around this mean is determined with its integral equal to 99% of the integral of the full histogram.

As noted earlier, in simulated events, the response distribution can be evaluated by the reconstructed over generator-level jet transverse momentum. A determination of the resolution in data, however, has to rely on a different approach.

The main idea of a resolution measurement using  $\gamma$ +jet events is based on the transverse-momentum balance of the  $\gamma$  + jet system and the excellent electromagnetic calorimeter resolution.

In Fig 1.2, all tree-level processes contributing to an event topology with one photon and one jet in the final state are depicted. Due to momentum conservation, the jet and the photon are back to back in the transverse plane, and therefore,  $\vec{p}_T^\gamma = -\vec{p}_T^{\text{jet}}$ . Because of the high resolution of the electromagnetic calorimeter, photon energies can be measured very accurately (with an resolution between 1.4% and 3.8% in the barrel region for  $\sqrt{s} = 8 \text{ TeV}$  data [11]). Thus, they can serve as an excellent estimator for the true jet transverse-momentum.

Unfortunately, such clean events are very rare processes, and usually, the momentum balance is spoiled by further jet activity from initial and final state radiation (see Fig. 1.3). In order to select events that are balanced to a large extent, a lower bound on the angular distance in the transverse plane between the photon and the jet with the highest transverse momentum (leading jet) is required:  $\Delta\Phi(1^{\text{st}} \text{ jet}, \gamma) > 2.95 \text{ rad}$ .

Additionally, the variable  $\alpha$  is defined as the ratio of the transverse momentum of the

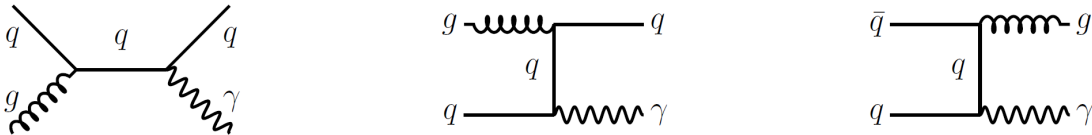


Figure 1.2: Tree-level Feynman diagrams of processes in  $pp$ -collisions with one photon and one jet in the final state.

<sup>2</sup>The  $2\sigma$  range is defined as the range  $[\mu - 2\sigma, \mu + 2\sigma]$ .



Figure 1.3: Tree-level Feynman diagrams with final (left) and initial (right) state radiation.

94 second jet to the transverse momentum of the photon

$$\alpha \doteq \frac{p_{\text{T}}^{2^{\text{nd}} \text{ reco. jet}}}{p_{\text{T}}^{\gamma}}, \quad (1.2)$$

95 and is thus a measure of further jet activity in an event. It is, however, not sufficient to  
 96 require only an upper bound on  $\alpha$ . Instead, the jet transverse-momentum resolution is  
 97 measured in bins of  $\alpha$  with  $\max(\alpha) = 0.2$ , and the extrapolated value to zero further jet  
 98 momentum at  $\alpha = 0$  is taken as the measured resolution of the jet  $p_{\text{T}}$ .

99 More formally, measuring the transverse momentum of the photon instead of taking the  
 100 generator-level jet  $p_{\text{T}}$  leads to the fact that the measured resolution consists of two parts

$$\underbrace{\frac{p_{\text{T}}^{\text{reco. jet}}}{p_{\text{T}}^{\gamma}}}_{\text{measured}} = \underbrace{\frac{p_{\text{T}}^{\text{reco. jet}}}{p_{\text{T}}^{\text{gen. jet}}}}_{\text{intrinsic}} \cdot \underbrace{\frac{p_{\text{T}}^{\text{gen. jet}}}{p_{\text{T}}^{\gamma}}}_{\text{imbalance}}. \quad (1.3)$$

101 The intrinsic part is the resolution of interest which is independent of further jets in the  
 102 event, whereas the imbalance is an artifact of further jet activity and is strongly dependent  
 103 on  $\alpha$ .

104 To account for differences in the jet transverse-momentum resolution for different true  
 105 jet  $p_{\text{T}}$  and different jet pseudorapidity regions, the measurement of the resolution is done  
 106 in  $p_{\text{T}}^{\gamma}$  bins and bins of  $|\eta|$  of the leading jet.

107 As noted before, the resolution measurement is important to correct the resolution  
 108 measured in simulation to the resolution measured in data. Therefore, the measurement  
 109 of the jet transverse-momentum resolution is performed on data and simulation and data-  
 110 to-simulation resolution scale factors ( $\rho_{\text{res}}$ ) are determined



## 1.3 Datasets and event selection

The measurement of the jet transverse-momentum resolution is carried out with  $\gamma + \text{jet}$  data recorded during the year 2012 at a centre-of-mass energy of  $\sqrt{s} = 8 \text{ TeV}$  at the CMS experiment. The datasets and triggers that are exploited for this measurement are introduced in the following Section 1.3.1. The measured resolution in data is compared to the resolution in a simulated  $\gamma + \text{jet}$  sample. Information about the simulated sample is given in Section 1.3.2. In order to select  $\gamma + \text{jet}$  events that are well suited for the resolution measurement, an event selection is applied on top. This event selection is described in Section 1.3.3.

### 1.3.1 Datasets and triggers

This analysis exploits several triggers which were active during the year 2012 at the CMS experiment. Because of the high production cross section of  $\gamma + \text{jet}$  events, especially for low photon  $p_T$ , almost all of these triggers were highly prescaled, i.e. only a fraction of events were actually recorded when the triggers fired. All triggers that are utilised in this measurement are listed in Table 1.1 together with their recorded luminosity. On

Table 1.1: Single-photon triggers together with the recorded luminosity taking the prescales of the triggers into consideration.

Trigger	Integrated luminosity [ fb <sup>-1</sup> ]
HLT_Photon30_CaloIdVL_IsoL	0.0029
HLT_Photon50_CaloIdVL_IsoL	0.0607
HLT_Photon75_CaloIdVL_IsoL	0.123
HLT_Photon90_CaloIdVL_IsoL	0.373
HLT_Photon135	13.77
HLT_Photon150	19.71

level-1 (L1), the triggers rely on single-photon/electron triggers, such as L1SingleEG12 and L1SingleEG30. The L1 triggers require at least one photon or electron candidate that is above a certain  $E_T$  threshold, e.g. 12 GeV or 30 GeV. The high-level triggers require a photon with a certain  $p_T$  (as indicated in the name) and, in case of thresholds below 135 GeV, additional quality and isolation criteria. All triggers with thresholds below 150 GeV were prescaled.

The events that are selected by the above mentioned triggers are contained in the datasets listed in Table 1.2.

Table 1.2: Single-photon data samples used for the resolution measurement with the contained integrated luminosity.

Dataset	Integrated luminosity [ $\text{fb}^{-1}$ ]
/Photon/Run2012A-22Jan2013-v1/AOD	0.876
/SinglePhoton/Run2012B-22Jan2013-v1/AOD	4.412
/SinglePhoton/Run2012C-22Jan2013-v1/AOD	7.055
/SinglePhotonParked/Run2012D-22Jan2013-v1/AOD	7.354

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### 1.3.2 Simulated sample

In order to compare the measured resolution in data to the resolution in simulation, a single-photon sample simulated with PYTHIA6 is used. This sample is generated flat in the photon  $p_T$  to have a good statistical precision also for the high photon  $p_T$  region. In order to recover a physical  $p_T$  spectrum, all simulated events are reweighted. Figure 1.4 shows the photon  $p_T$  spectrum in simulation before and after the reweighting.

Simulated samples come with a pileup scenario which does not necessarily match the pileup scenario in data. To match the measured distribution of interactions, the events are weighted according to their number of pileup vertices. Because almost all of the used triggers were differently prescaled over time, the distributions of pileup interactions differ among the sets of events recorded by each trigger. Thus, the weighting has to be done separately for each trigger. A comparison between the number of primary vertices in data and simulation for all triggers can be found in Appendix A.1.

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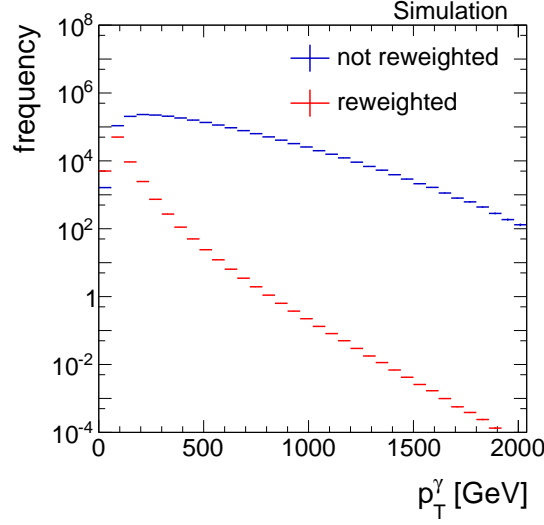


Figure 1.4: The photon  $p_T$  spectrum of the PYTHIA6 simulated single-photon sample before (blue) and after (red) reweighting.

### 1.3.3 Event selection

Events are reconstructed with the particle-flow reconstruction algorithm, which uses information of all detector components to reconstruct individual particles [12]. In the following, the selection of well reconstructed jets and photons will be explained as well as the event selection of  $\gamma + \text{jet}$  events.

#### Jet selection

Particles belonging to a jet are clustered with the anti- $k_t$  jet clustering algorithm [13] with a radius parameter of  $R=0.5$ . Furthermore, all reconstructed jets undergo a so-called “charged hadron subtraction” (CHS) which removes hadrons that are likely caused by pileup events.

To select clean  $\gamma + \text{jet}$  events, it is required that the leading jet meets the “tight ID” selection requirements for jets [14,15]. The tight ID selection ensures a selection efficiency of around 99% and a noise rejection efficiency of 99.98% [14]. It comprises the following selection criteria:

- Neutral hadron fraction  $< 0.90$
- Neutral electromagnetic fraction  $< 0.90$
- Number of constituents  $> 1$

And for jets in the pseudorapidity range  $|\eta| < 2.4$  :

- Charged hadron fraction  $> 0$
- Charged hadron multiplicity  $> 0$
- Charged electromagnetic fraction  $< 0.99$ .

To mitigate effects from pileup, an additional requirement on the transverse momentum is imposed:

- $p_T^{1^{\text{st}} \text{ jet}}, p_T^{2^{\text{nd}} \text{ jet}} > 10 \text{ GeV}$ .

### Photon selection

Concerning the photon, a maximum pseudorapidity of the photon of  $|\eta^\gamma| < 1.3$  is demanded to exploit the high resolution of the ECAL in the barrel region.

Furthermore, the resolution is determined for different ranges in photon  $p_T$  to avoid mixing of different prescales of the various triggers. In Table 1.3 the applied binning is shown with the respective triggers contributing to each  $p_T^\gamma$  bin.

Table 1.3: Photon  $p_T$  bins and corresponding triggers.

$p_T^\gamma$ -bins	Trigger
36-60 GeV	HLT_Photon30_CaloIdVL_IsoL_v*
60-88 GeV	HLT_Photon50_CaloIdVL_IsoL_v*
88-105 GeV	HLT_Photon75_CaloIdVL_IsoL_v*
105-149 GeV	HLT_Photon90_CaloIdVL_IsoL_v*
149-165 GeV	HLT_Photon135_v*
165- $\infty$ GeV	HLT_Photon150_v*

QCD-multijet events constitute an important background to  $\gamma + \text{jet}$  events: A primary photon can be faked by a  $\pi^0$  decaying into two close-by photons. Therefore, a very clean selection of the photons is necessary to suppress this background. The following variables are used (see [16] for further explanation of the variables):

- $\frac{H}{E}$  : The ratio of the measured energy in the hadronic calorimeter over the energy measured in the electromagnetic calorimeter. For photons, this is supposed to be very small as they deposit their energy predominantly in the ECAL.

- $\sigma_{i\eta i\eta}$ : The energy weighted spatial width of the photon energy deposition. The electromagnetic shower of a photon has a small lateral size resulting in small  $\sigma_{i\eta i\eta}$  for prompt photons while showers from fake photons, e.g.  $\pi^0 \rightarrow \gamma\gamma$  have a larger lateral size.
- **Jurassic ECAL isolation:** This isolation criterion uses the information of reconstructed hits “RecHits” (coming from the local reconstruction of the digital signals) in a cone around the photon supercluster of  $R=0.4$ . Those are summed up and an upper criterion is identified to discriminate against background which is typically spatially broader.
- **Tower-based HCAL isolation:** The isolation criterion requires the energy deposited in all HCAL towers around the photon in cone of  $R=0.4$  to be small compared to the photon’s energy.
- **Hollow cone track isolation:** Requires the absence of high-energetic tracks around the photon.
- **Pixel seed veto:** In order to reduce the background from electrons and positrons further, the absence of a pixel-seed in the pixel tracker along the photon trajectory is required.

The upper bounds that are set on these observables can be found in Table 1.4.

Table 1.4: Upper bounds for all photon isolation criteria in the barrel ( $|\eta^\gamma| < 1.4442$ ).

	Barrel
$\frac{H}{E}$	$< 0.05$
$\sigma_{i\eta i\eta}$	$< 0.013$
ECAL isolation	$< 4.2 \text{ GeV} + 0.0060 \cdot p_T^\gamma$
HCAL isolation	$< 2.2 \text{ GeV} + 0.0025 \cdot p_T^\gamma$
Track Isolation	$< 2.0 \text{ GeV} + 0.0010 \cdot p_T^\gamma$
Pixel seed veto	yes

## Photon+jet event selection

Besides the mentioned requirements concerning the objects' attributes, two further criteria related to the event topology are crucial for this analysis:

A lower threshold on  $\Delta\Phi$  between the leading jet and the photon and a maximum value for  $\alpha$

- $\Delta\Phi(1^{\text{st}} \text{ jet}, \gamma) > 2.95 \text{ rad}$

- $\alpha = \frac{p_{\text{T}}^{2^{\text{nd}} \text{ jet}}}{p_{\text{T}}^{\gamma}} < 0.20.$

These requirements are important to suppress events with too much further hadronic activity. A summary of all selection criteria can be found in Appendix A.2.

Finally, the leading jet pseudorapidity interval bounds need to be chosen in order to account for resolution differences in different detector regions. This is done according to [9] with the following binning

$$\begin{aligned} |\eta^{1^{\text{st}} \text{ jet}}| &= 0.0 - 0.5 & |\eta^{1^{\text{st}} \text{ jet}}| &= 1.1 - 1.7 \\ |\eta^{1^{\text{st}} \text{ jet}}| &= 0.5 - 1.1 & |\eta^{1^{\text{st}} \text{ jet}}| &= 1.7 - 2.3. \end{aligned}$$

The binning in the  $p_{\text{T}}^{\gamma}$  dimension is chosen according to the trigger thresholds for  $p_{\text{T}}^{\gamma} < 165 \text{ GeV}$  and ensures sufficient statistical precision for  $p_{\text{T}}^{\gamma} > 165 \text{ GeV}$

$p_{\text{T}}^{\gamma} = 36 - 60 \text{ GeV}$	$p_{\text{T}}^{\gamma} = 149 - 165 \text{ GeV}$	$p_{\text{T}}^{\gamma} = 200 - 300 \text{ GeV}$
$p_{\text{T}}^{\gamma} = 60 - 88 \text{ GeV}$	$p_{\text{T}}^{\gamma} = 165 - 176 \text{ GeV}$	$p_{\text{T}}^{\gamma} = 300 - 400 \text{ GeV}$
$p_{\text{T}}^{\gamma} = 88 - 105 \text{ GeV}$	$p_{\text{T}}^{\gamma} = 176 - 200 \text{ GeV}$	$p_{\text{T}}^{\gamma} > 400 \text{ GeV}$
$p_{\text{T}}^{\gamma} = 105 - 149 \text{ GeV}$	$p_{\text{T}}^{\gamma} = 300 - 400 \text{ GeV}.$	

## 1.4 Methodology of the measurement

The basic methodology of measuring the jet transverse-momentum resolution by exploiting the  $p_{\text{T}}$  balance in  $\gamma + \text{jet}$  events and extrapolating the result to small  $\alpha$ , that was already used in earlier analyses [6, 7], is extended in this measurement in order to explicitly account for the influence of the direction of additional jets on the jet transverse-momentum response.

As already described in Chapter 1.2, the idea behind a resolution measurement with  $\gamma + \text{jet}$  events in data is the usage of the photon  $p_T$  instead of the true jet  $p_T$ . This results in a twofold contribution to the measured response, the intrinsic response and the imbalance:

$$\underbrace{\frac{p_T^{\text{reco. jet}}}{p_T^\gamma}}_{\text{measured}} = \underbrace{\frac{p_T^{\text{reco. jet}}}{p_T^{\text{gen. jet}}}}_{\text{intrinsic}} \cdot \underbrace{\frac{p_T^{\text{gen. jet}}}{p_T^\gamma}}_{\text{imbalance}}. \quad (1.4)$$

Taking the photon  $p_T$  as true jet  $p_T$  estimator instead of the generator-level jet  $p_T$ , and thus measuring the response defined as  $p_T^{\text{reco. jet}}/p_T^\gamma$ , results in a different shape of the response distribution compared to the intrinsic response (Fig. 1.5). The clear difference

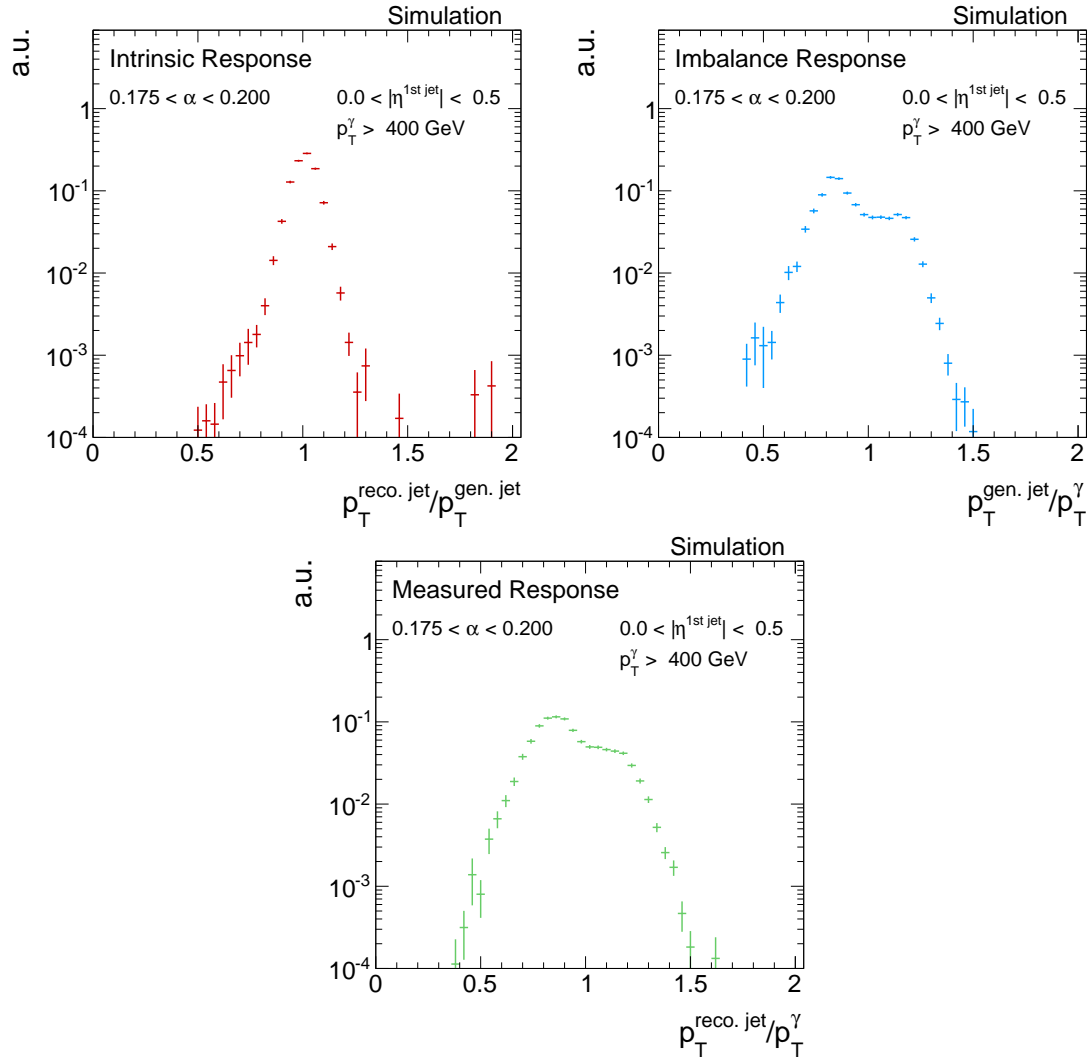


Figure 1.5: The two different contributions, intrinsic (top left) and imbalance (top right), to the measured response (bottom) (cf. Eq. (1.4)) in simulated events.

between the intrinsic response and the imbalance is the double peak structure of the latter one. The measured response is a convolution of the two contributions, where the double peak is consequentially less pronounced.

The occurrence of two peaks is caused by the hard selection in  $\Delta\Phi$  which forces the second jet to be either close to the photon or close to the leading jet due to  $p_T$  conservation. An energetic second jet perpendicular to the leading jet-photon axis would require a balancing third jet for  $p_T$  conservation. This is very unlikely due to the decreasing probability of high jet multiplicities in QCD-multijet events. Events can thus be distinguished by the relative direction of the second jet (see Fig. 1.6 for a schematic sketch), with a hemisphere definition of

$$\begin{aligned} \text{Second jet in 1}^{\text{st}} \text{ jet hemisphere:} \quad & \Delta\Phi\left(1^{\text{st}} \text{ jet}, 2^{\text{nd}} \text{ jet}\right) < \Delta\Phi\left(\gamma, 2^{\text{nd}} \text{ jet}\right), \\ \text{Second jet in photon hemisphere:} \quad & \text{else.} \end{aligned} \quad (1.5)$$

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As can be seen in Fig. 1.7, events containing a second jet in the leading jet hemisphere lead to a response histogram with mean smaller one, while events with a second jet in photon direction result in a distribution with mean larger one. The former occurs more frequently because it contains jets from final and initial state radiation, while the latter mainly consists of jets from initial state radiation.

The two response distributions coming from the different event topologies are separately evaluated. First, the resolution is determined for each of the configurations (cf. Fig. 1.7),

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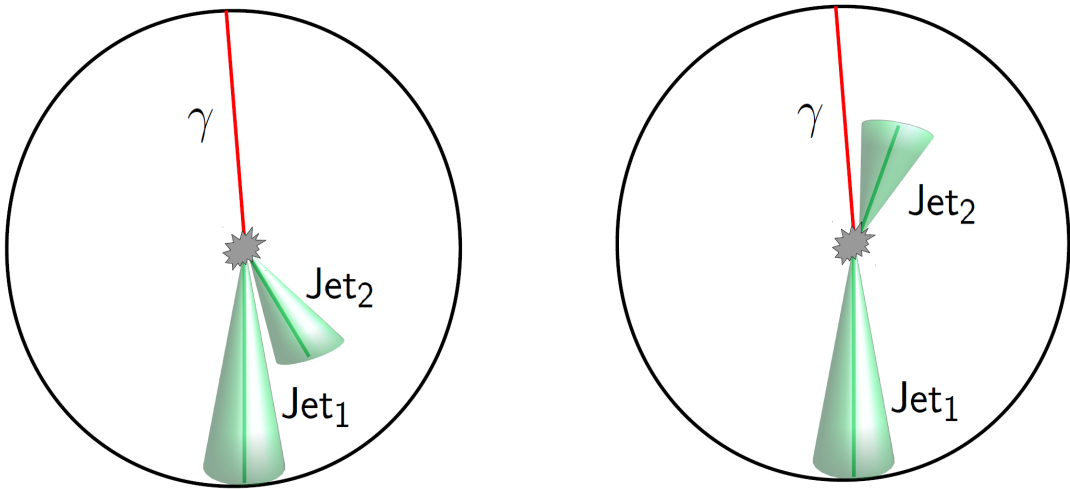


Figure 1.6: A schematic sketch of the two different event topologies where the second jet is in the leading jet (left) or the photon hemisphere (right)



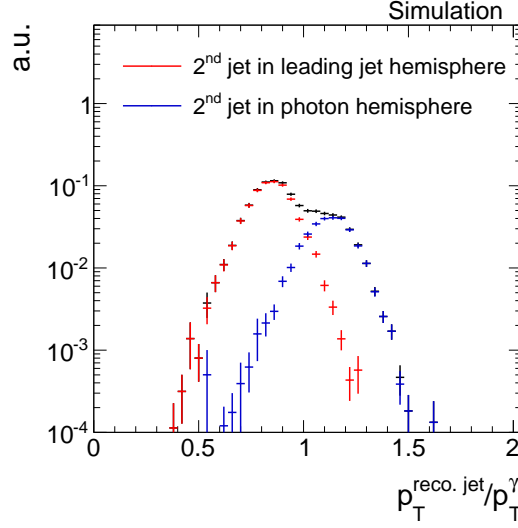


Figure 1.7: The measured jet transverse-momentum response. Events with a second jet in the photon hemisphere (red) lead to a mean response larger one, while events with a second jet in the leading jet hemisphere (green) have a mean smaller one. The sum of both contributions is depicted in black.

and then, the weighted mean of the two contributions is calculated.

With the above presented methodology, it is possible to measure the resolution in simulation and data for different values of  $\alpha$ . Since the quantity of interest is the jet transverse-momentum resolution independent of further jet activity, i.e. the extrapolated value of the measured resolution at  $\alpha = 0$ , the dependency of the measured resolution on alpha,  $\sigma_{\text{measured}}(\alpha)$ , is needed. Simulated events offer the possibility to study the individual contributions to the measured resolution: the intrinsic resolution  $\sigma_{\text{intrinsic}}(\alpha)$  and the imbalance  $\sigma_{\text{imbalance}}(\alpha)$ .

The intrinsic part of the resolution for a given photon  $p_T$  bin is, by definition, independent of secondary jet  $p_T$ , and can be considered as constant in terms of  $\alpha$

$$\sigma_{\text{intrinsic}}(\alpha) = c. \quad (1.6)$$

This is not true for the imbalance part. It was found empirically that the  $\alpha$  dependence of the imbalance can be described by a linear function [7]

$$\sigma_{\text{imbalance}}(\alpha) = q + m \cdot \alpha \quad (1.7)$$

Folding two independent Gaussian functions results in a quadratic addition of the corresponding standard deviations  $\sigma_{\text{intr.}} \oplus \sigma_{\text{imb.}}$  and finally yields the functional expression for

the measured resolution

$$\sigma_{\text{measured}}(\alpha) = \sqrt{c^2 + q^2 + 2qm \cdot \alpha + m^2 \cdot \alpha^2}. \quad (1.8)$$

In Fig. 1.8, the  $\alpha$  dependence of the intrinsic resolution (red dots), the imbalance (blue dots), and the measured resolution (green dots) is shown for two exemplary  $p_T^\gamma$  regions in simulated events. The intrinsic resolution is fitted with Eq. (1.6) (red line), while the imbalance is fitted with Eq. (1.7) (blue line).

It is apparent that the imbalance is not zero for  $\alpha = 0$ . This has two reasons. First and most important, only the photon and the parton are balanced in the transverse plane. But since the transverse momentum of a jet is defined as the sum of all particles' transverse momenta that are clustered within a cone of certain size, the jet  $p_T$  can be lower than the  $p_T$  of the original parton. This effect is called out-of-cone showering and leads to a residual imbalance between the photon  $p_T$  and the generator-level jet  $p_T$  at  $\alpha = 0$  (parameter  $q$  in Eq. (1.7)). Second, the photon  $p_T$  can be wrongly measured and spoil the residual imbalance  $q$ .

Due to the existence of a residual imbalance  $q$ , it is not possible to simply use the measured resolution at  $\alpha = 0$  as an estimator of the intrinsic resolution  $c$ . This is already obvious from Eq. (1.8) which evaluates to  $\sigma_{\text{measured}} = \sqrt{c^2 + q^2}$  at  $\alpha = 0$ .

For the determination of the intrinsic resolution in data, the method relies on the residual

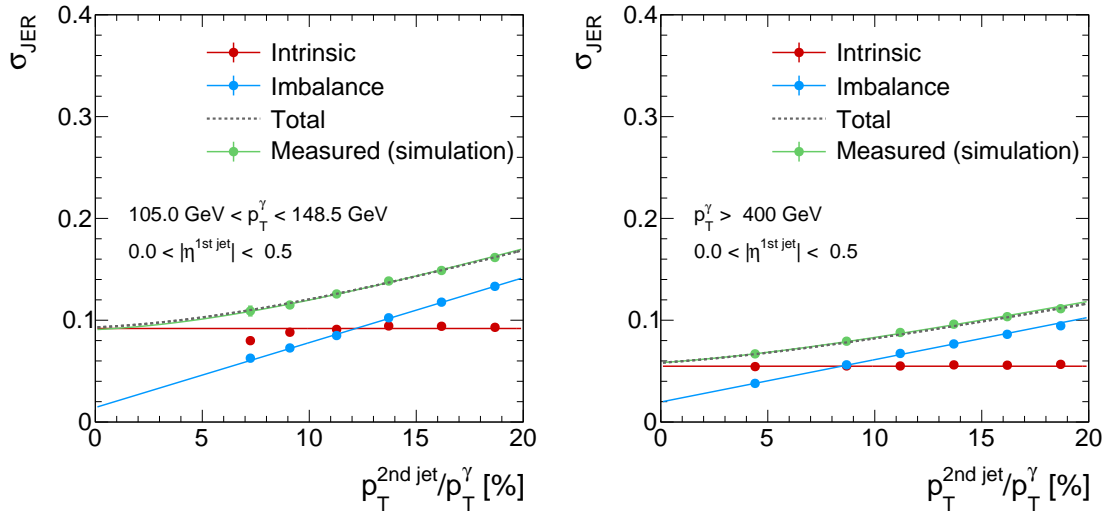


Figure 1.8: The alpha dependency of the various parts of the resolution in the simulated events for  $83 \text{ GeV} < p_T^\gamma < 99 \text{ GeV}$  (left) and  $400 \text{ GeV} < p_T^\gamma$  (right). The total resolution (grey dotted line) is the addition in quadrature of the imbalance (blue line) and the intrinsic (red line) fit functions. It can be compared to the measured resolution in simulation (green dots/line).

imbalance information from simulation. Practically, when fitting the measured resolution (Eq.(1.8)) in data, the residual imbalance  $q$  is fixed to the value obtained from the imbalance fit (Eq 1.7) in simulation. The intrinsic resolution in data can then be obtained by extracting the fit parameter  $c$ . In the following the estimator of the intrinsic resolution (fit parameter  $c$  from the measured resolution) will be referred to as  $\sigma_{\text{JER}}$ .

For consistency, the same approach is used for simulated events. The fitted function of the measured resolution (green line) in Fig. 1.8 corresponds to the fit function of Eq. (1.8) with the parameter  $q$  fixed to the value obtained from the imbalance fit (blue line). Finally, the dotted grey line is the total resolution with the analytic expression of function (1.8) with the parameters set to the fit values of the intrinsic (red) and the imbalance fit (blue). It can be nicely seen that the total resolution and the fit function of the measured resolution (green line) are well in agreement. This implies, that the assumed functional forms of the resolution components and the assumed convolution leads indeed to a good description of the measured resolution. Further validations of the methodology will be described in Section 1.4.1.

In Fig. 1.9, the estimated intrinsic resolution in simulation (green) and data (black) is shown in different photon  $p_T$  bins for two different  $|\eta^{1\text{st jet}}|$  regions. The resolution improves for increasing photon  $p_T$ . For the  $|\eta^{1\text{st jet}}| < 0.5$  region, the resolution is approximately 10% for  $p_T^\gamma \approx 100$  GeV and decreases to values around 7% for  $p_T^\gamma \approx 300$  GeV. The increasing statistical uncertainties for low photon  $p_T$  arise through the requirements of  $\alpha = \frac{p_T^{2\text{nd reco. jet}}}{p_T^\gamma} < 0.2$  and  $p_T^{2\text{nd jet}} > 10$  GeV. This reduces the numbers of events in the

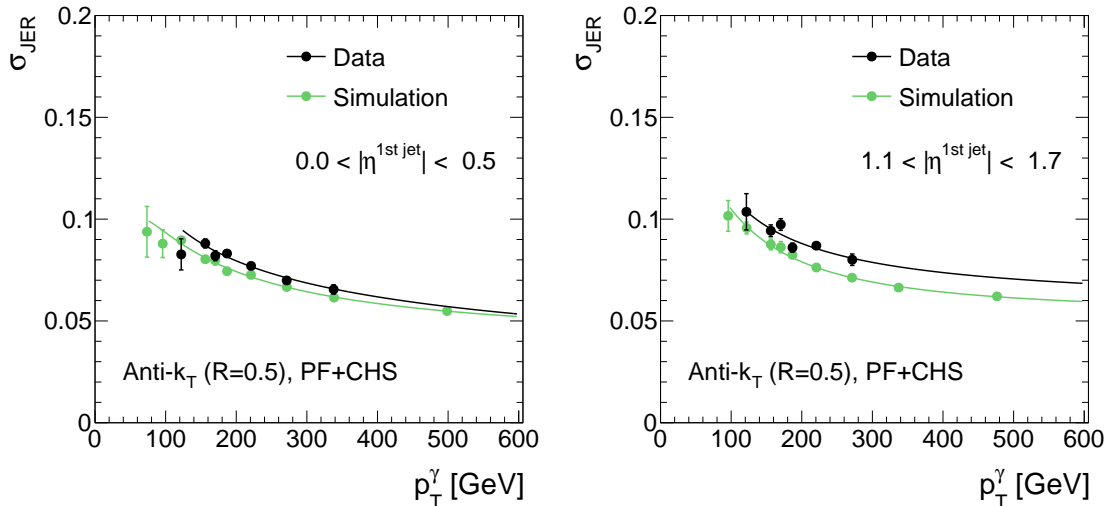


Figure 1.9: Resolution for  $|\eta^{1\text{st jet}}| < 0.5$  (left) and  $1.1 < |\eta^{1\text{st jet}}| < 1.7$  (right) in simulation (green) and data (black). Both are fitted with a particle-flow resolution function introduced in [6].

low photon  $p_T$  bins. For events with  $p_T^\gamma \lesssim 50$  GeV, it is not possible at all to fulfil both requirements at the same time.

From Fig. 1.9, it can be seen that the resolution in data is always worse than the resolution in simulation. Thus, in order to measure data-to-simulation scale factors  $\rho_{\text{res}}$  for the jet transverse-momentum resolution, the measured resolution in data is divided by the resolution in Monte Carlo simulation (MC).

$$\rho_{\text{res}} = \frac{\sigma_{\text{JER}}^{\text{data}}}{\sigma_{\text{JER}}^{\text{MC}}} \quad (1.9)$$

The results will show (Chapter 1.6), that this ratio is independent of  $p_T^\gamma$  and can thus be fitted with a constant in terms of  $p_T^\gamma$ . The measurement of the data-to-simulation scale factors is therefore only done in bins of  $|\eta^{1\text{st jet}}|$ .

How to apply these scale factors and adjust the jet transverse-momentum resolution in simulation to the measured resolution in data is well described in [9].

### 1.4.1 Validation of the method

It has already been shown that the decomposition of the measured resolution into intrinsic resolution and imbalance works well for the two shown  $p_T^\gamma$  bins in Fig. 1.8. In order to further validate the method, a comparison between  $\sigma_{\text{JER}}$  extracted from the measured resolution and the real  $\sigma_{\text{JER}}$  of the intrinsic resolution is performed on simulated events. Figure 1.10 depicts the results of this comparison for one exemplary  $|\eta^{1\text{st jet}}|$  bin. It can be seen that the method has a bias of up to 15% towards an underestimation of the resolution for small  $p_T^\gamma$ . For  $p_T^\gamma > 100$  GeV the bias is less than 5% and reduces to less than 1% for  $p_T^\gamma > 200$  GeV.

The residual bias of the method is caused by the accumulation of high  $p_T^{1\text{st jet}}$  events in the low alpha bins and low  $p_T^{1\text{st jet}}$  events in the high alpha bins. Since the jet transverse-momentum resolution decreases for higher  $p_T^{1\text{st jet}}$ , this leads to an upward slope of the resolution with increasing alpha (cf. red dots in Fig 1.8 (left)).

The intrinsic resolution is not affected by this  $\alpha$  dependency because it is fitted with a constant and thus corresponds to the mean resolution across all  $\alpha$  bins. In contrast, the fit of the measured resolution with an additional free parameter can adopt this increase and can therefore result in an underestimation of the y-intercept and thus of  $\sigma_{\text{JER}}$ . For high photon  $p_T$ , this effect is less pronounced, since the slope of  $\sigma_{\text{JER}}(p_T^\gamma)$  (see Fig. 1.10) flattens out. Thus the method is only biased for small  $p_T^\gamma$ .

The accumulation of high  $p_T^{1\text{st jet}}$  events in low  $\alpha$  bins is stemming from two effects. First, the binning in  $p_T^\gamma$  and the momentum balance between the photon and the first two jets lead to a dependency of the first jet  $p_T$  on the second jet  $p_T$  and therefore alpha: For a fixed

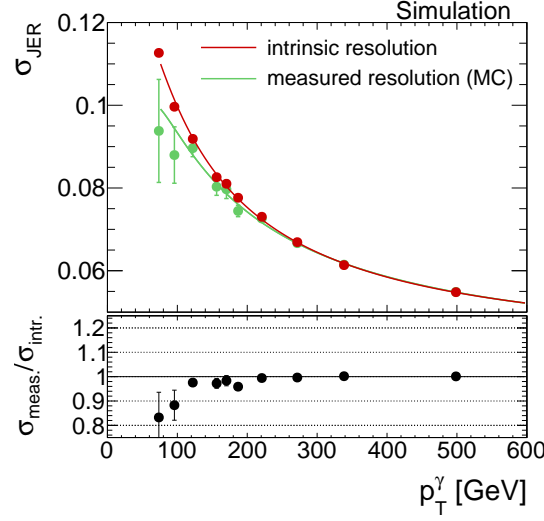


Figure 1.10: Consistency check of the method: Comparison between  $\sigma_{\text{JER}}$  obtained from the measured resolution (Eq. (1.8)) and from the intrinsic resolution (Eq. (1.6)) in simulation.

$p_T^\gamma$ , the  $p_T$  of the first jet gets smaller for larger  $p_T^{2^{\text{nd jet}}}$  in events where the second jet is in the leading jet hemisphere (see Fig. 1.6), leading to a dependency of  $p_T^{1^{\text{st jet}}} \propto -p_T^{2^{\text{nd jet}}}$ . This effect is directly opposite for events with a second jet in the photon hemisphere, where the first jet  $p_T$  gets larger for larger  $p_T^{2^{\text{nd jet}}}$  and thus  $p_T^{1^{\text{st jet}}} \propto p_T^{2^{\text{nd jet}}}$ . In principle, the effect should thus cancel out, but since the topology of a second jet in the leading jet hemisphere is much more frequent, a residual upward trend in the resolution vs.  $\alpha$  is conserved.

The second source of the accumulation of high  $p_T^{1^{\text{st jet}}}$  events in low  $\alpha$  bins arises from the alpha definition  $\alpha = p_T^{2^{\text{nd jet}}}/p_T^\gamma$  and the non-zero width of the  $p_T^\gamma$  bins. Because of the inclusion of  $p_T^\gamma$  in  $\alpha$  with  $\alpha \propto 1/p_T^\gamma$ , the high photon  $p_T$  events accumulate in the low alpha regions. As the selected events are almost balanced, a high  $p_T^\gamma$  is associated with a high jet  $p_T$ , thus also the high jet  $p_T$  events accumulate in the low alpha bins, leading to an upward trend in the resolution vs.  $\alpha$ .

However, since the discussed bias affects the resolution measurement in simulation and data equivalently, the residual bias for low  $p_T^\gamma$  is not of concern for the measurement of data-to-simulation resolution scale factors  $\rho_{\text{res}}$  (Eq. (1.9)). To prove the hypothesis of a cancellation of the bias, a pseudo dataset is generated from the simulated dataset where the jet transverse-momentum resolution is smeared by  $\rho_{\text{res}} = 1.1$  in all  $|\eta^{1^{\text{st jet}}}|$  bins. Subsequently, the resolution scale factors between the smeared pseudo dataset and the original simulated dataset are determined according to the methodology presented in this

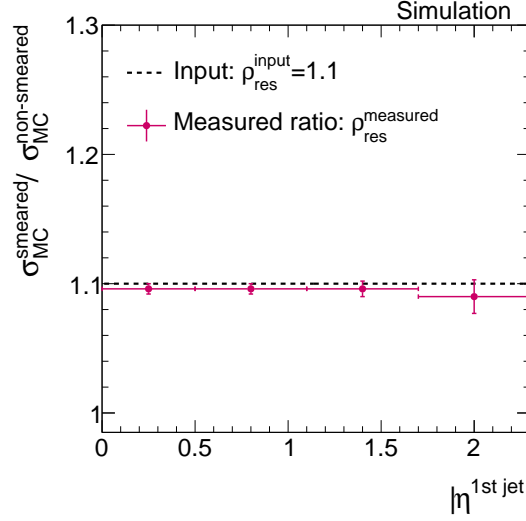


Figure 1.11: Comparison of the resolution ratio  $\sigma_{\text{JER}}^{\text{smeared MC}} / \sigma_{\text{JER}}^{\text{non-smeared MC}}$  measured in simulated events with the input smearing factor  $\rho_{\text{res}} = 1.1$  in all four  $|\eta^{1\text{st jet}}|$  bins.

thesis. The resulting scale factors  $\rho_{\text{res}}$  should reproduce the input values of  $\rho_{\text{res}} = 1.1$ . In Fig. 1.11, the result of this test is shown. In all  $|\eta^{1\text{st jet}}|$  bins, the measurement of the scale factors reproduces the input factors within the statistical uncertainties. The deviation of the measured scale factors to the input value is less than 0.9% in all four  $|\eta^{1\text{st jet}}|$  bins. Thus, the method is expected to also hold for the determination of the data-to-simulation ratio.

After the characterisation and estimation of the associated systematic uncertainties of the jet transverse-momentum resolution measurement with  $\gamma + \text{jet}$  events, the results of the measurement on  $\sqrt{s} = 8 \text{ TeV}$  data will be presented.

## 1.5 Systematic uncertainties

Many systematic uncertainties of the jet transverse-momentum resolution measurement cancel out when focusing on the data-to-simulation ratio  $\sigma_{\text{JER}}^{\text{data}} / \sigma_{\text{JER}}^{\text{MC}}$ . In the following sections, only uncertainties relevant for this ratio will be discussed.

For the final uncertainty, the single uncertainties are added in quadrature, resulting in relative uncertainties between 2.3% to 6.3% for the lowest and highest  $|\eta^{1\text{st jet}}|$  bin, respectively.

371 An overview of all systematic uncertainties can be found in Table 1.5.

Table 1.5: All relative systematic uncertainties on the data-to-simulation ratio  $\sigma_{\text{JER}}^{\text{data}}/\sigma_{\text{JER}}^{\text{MC}}$  listed by sources for the different  $|\eta^{\text{jet}}|$  bins.

	$ \eta^{\text{jet}} $			
	0.0 - 0.5	0.5 - 1.1	1.1 - 1.7	1.7 - 2.3
<b>Multijet contamination</b>	+2.0% −2.0%	+2.0% −2.0%	+2.3% −2.3%	+2.5% −2.5%
<b>Simulation of flavour composition</b>	+0.9% −0.9%	+0.9% −0.9%	+0.8% −0.8%	+0.6% −0.6%
<b>Simulation of out-of-cone showering</b>	+0.5% −0.5%	+2.8% −2.8%	+3.6% −3.6%	+5.7% −5.7%
<b>Jet energy scale</b>	+0.6% −0.5%	+0.6% −0.6%	+0.6% −0.6%	+0.7% −0.6%
<b>Pileup reweighting</b>	+0.1% −0.1%	+0.1% −0.1%	+0.1% −0.2%	+0.2% −0.2%
<b>Total</b>	+2.3% −2.3%	+3.6% −3.6%	+4.4% −4.4%	+6.3% −6.3%

## 372 Uncertainty on the contamination with QCD-multijet events

373 Due to the huge QCD-multijet cross section, a sizable fraction of dijet events can survive  
 374 the strict photon selection (see Section 1.3.3) if a jet is misidentified as a photon. This  
 375 happens, when e.g. a jet hadronises to a  $\pi^0$  that decays to two close-by photons that  
 376 mimic the signature of an isolated photon from a  $\gamma + \text{jet}$  event.

377 The two leading jets in a dijet event are balanced except for initial and final state radi-  
 378 ation and have in principle the same topology as  $\gamma + \text{jet}$  events. Therefore, the presented  
 379 method is in principle insensitive to dijet contamination. Adverse effects of dijet back-  
 380 ground contamination are only expected due to a mismeasurement of the  $p_{\text{T}}$  of the jet  
 381 misidentified as photon, because only the energy of the  $\pi^0$  is counted and not the full jet  
 382 energy. Another aspect is the different flavour composition of a QCD-multijet sample.

Due to the different production mechanism, QCD-dijets are predominantly initiated by gluons while the leading jet in  $\gamma + \text{jet}$  events often stems from a light quark. The number of particles after hadronisation is typically larger for gluon jets, hence the single particles are less energetic and out-of-cone showering is more pronounced. Since the residual imbalance  $q$  in this analysis is taken from simulation considering  $\gamma + \text{jet}$  events only, it is not expected to accurately describe the residual imbalance in the data sample that is contaminated with dijet events.

To investigate the impact of QCD-multijet contamination, a QCD-multijet sample, enriched in jets with a large electromagnetic fraction, is added to the  $\gamma + \text{jet}$  sample and weighted according to the cross section. Subsequently, the resolution measured using both the  $\gamma + \text{jet}$  and the QCD-multijet sample is compared to the resolution measured with the  $\gamma + \text{jet}$  sample only. Since the QCD-multijet sample has very large event weights leading to high statistical uncertainties on the measured jet transverse-momentum resolution, two selection criteria ( $\alpha < 0.4$  and  $\Delta\Phi > 2.7$ ) are relaxed in order to increase the statistical precision of the uncertainty estimation. Additionally, a rougher binning in  $\alpha$ ,  $p_T^\gamma$  and  $|\eta^{1\text{st jet}}|$  is applied. The residual imbalance  $q$  of the resolution measurement including the QCD-multijet sample is fixed to the residual imbalance determined from the  $\gamma + \text{jet}$  only analysis in order to account for a possible error in the evaluation of the  $\sigma_{\text{JER}}^{\text{data}}/\sigma_{\text{JER}}^{\text{MC}}$  ratio for which data is only compared to a  $\gamma + \text{jet}$  sample. It can be seen from Fig. 1.12 that the jet transverse-momentum resolution is worse for low  $p_T^\gamma$  when considering QCD-multijet contamination.

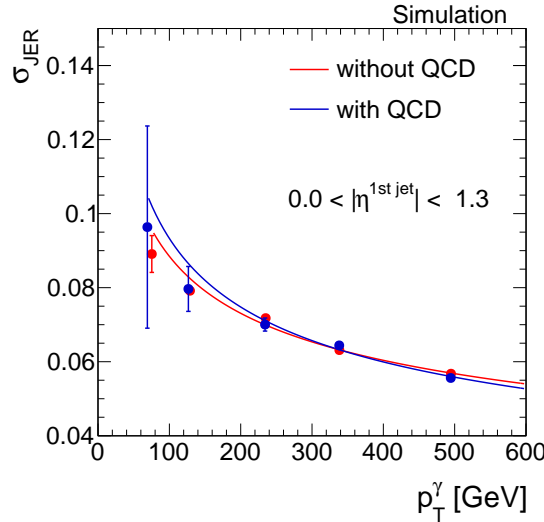


Figure 1.12: The jet transverse-momentum resolution measured in simulation for  $|\eta^{1\text{st jet}}| < 1.3$  with (blue) and without (green) a QCD-multijet sample added to the  $\gamma + \text{jet}$  sample.



The observed difference in the resolution measurement of the two approaches is taken as a systematic uncertainty on the measured resolution in data and propagated to the final data-to-simulation ratio. The resulting uncertainties vary between 2.0 – 2.5% for the different  $|\eta^{1\text{st jet}}|$  regions (cf. Table 1.5).

## Uncertainty on the flavour composition in simulation

A possible difference between the resolution of different jet flavours (e.g. caused by more pronounced out-of-cone showering of gluon jets) should in principle not play a role for the data-to-simulation scale factors  $\rho_{\text{res}}$  as long as the flavour composition in data and simulation is the same.

To account for possible discrepancies in the flavour composition between data and simulation, the gluon and quark flavour fractions of the simulated sample (Fig 1.13) are varied by 10%. To estimate the effect of different flavour compositions, the resolution in simulation is separately evaluated for quarks ( $\sigma_{\text{JER}}^{\text{quarks}}$ ) and gluons ( $\sigma_{\text{JER}}^{\text{gluons}}$ ).

There are various definitions used in the CMS collaboration how to assign the underlying generator-level quark/gluon flavour to a jet. In this measurement the so-called “algorithmic” flavour definition is used (see Appendix A.3 for more details on this definition). The composition in the simulated PYTHIA  $\gamma$ +jet sample is around 60% light quarks and 20% to 35% gluons (see Fig. 1.13). The missing fraction is mainly made up out of charm quarks.

The left panel of Figure 1.14 depicts the intrinsic resolution for all flavours separately

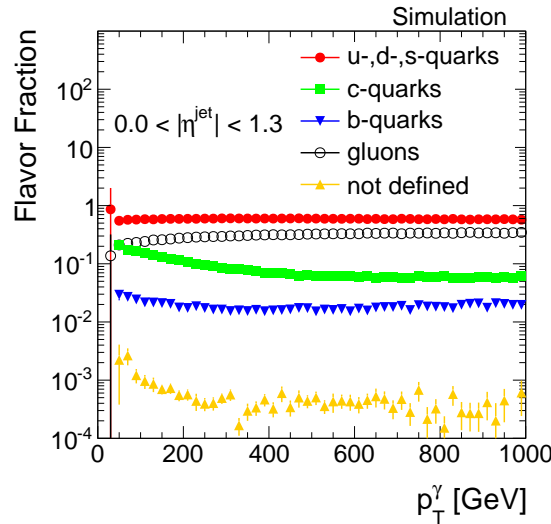


Figure 1.13: The flavour composition in the simulated  $\gamma$ +jet sample in the barrel region of the detector. The “algorithmic” flavour definition is used (see Appendix A.3 for more details).

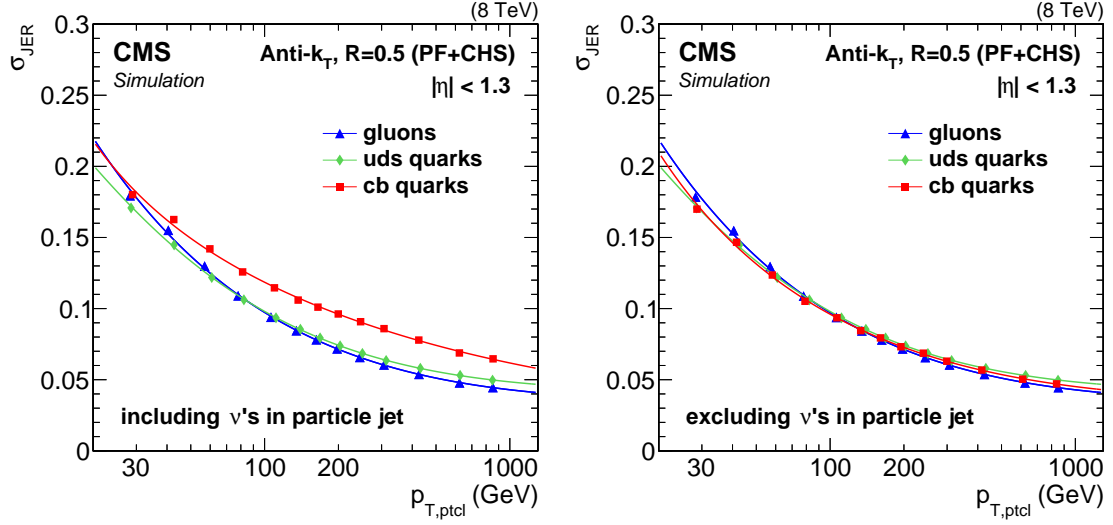


Figure 1.14: The intrinsic resolution  $\sigma_{\text{intr.}}$  for  $|\eta^{\text{1st jet}}| < 1.3$  for different jet flavours with (left) and without (right) including the neutrinos in the generator-level jet. Here, JER refers to  $\sigma_{\text{intr.}}$ , and  $p_{\text{T,ptcl}}$  to the generator-level jet  $p_{\text{T}}$ .

for  $|\eta^{\text{1st jet}}| < 1.3$ . It can be seen that the resolution for gluon and light quark jets is comparable whereas heavier quarks have a worse resolution across the full  $p_{\text{T}}$  range. This is because the decay of heavy quarks can involve the production of neutrinos, whose transverse momentum is not detectable, leading to an underestimation of the reconstructed jet  $p_{\text{T}}$ . Since the neutrino  $p_{\text{T}}$  is included in the jet  $p_{\text{T}}$  on generator level, c- and b-jets have a more pronounced left tail of the jet transverse-momentum response, leading to a worse resolution compared to light quark jets (left part of Fig. 1.14). This is not the case, if the neutrino  $p_{\text{T}}$  is not added to the generator-level jet  $p_{\text{T}}$ , as can be seen in Fig. 1.14 (right).

In order to estimate the uncertainty, the flavour composition in simulation is varied by 10% and the constant fit to the data-to-simulation ratio  $\sigma_{\text{JER}}^{\text{data}}/\sigma_{\text{JER}}^{\text{MC}}$  is reevaluated, leading to a final systematic uncertainty between 0.6 and 0.9%.

## Uncertainty on the simulation of out-of-cone showering

Another source of uncertainty is the use of information from Monte Carlo simulation for determining the residual imbalance  $q$  from the simulated  $\gamma + \text{jet}$  sample (Eq. (1.8)).

Since it cannot be expected that out-of-cone showering is perfectly modelled in simulation, possible differences between real and simulated out-of-cone showering are estimated by the evaluation of the ratio  $\sigma_{\text{JER}}^{\text{data}}/\sigma_{\text{JER}}^{\text{MC}}$  using different jet radii in the jet reconstruction algorithm.

For the primary analysis, jets reconstructed by the anti- $k_t$  algorithm with a radius parameter of  $R = 0.5$  are used (AK5-jets). In order to evaluate the systematic uncertainty on the out-of-cone showering simulation, the measurement of  $\rho_{\text{res}}$  is redone with jets reconstructed with a jet radius of  $R = 0.7$  (AK7-jets).

The data-to-simulation ratio is in all  $|\eta^{1^{\text{st}} \text{ jet}}|$  bins larger for AK7-jets, resulting in uncertainties between 0.5 – 5.7%. The uncertainty on the simulation of out-of-cone showering is thus the largest systematic uncertainty of this measurement.

## Uncertainty on the jet energy scale

A further uncertainty arises from the correction of the jet energy scale. The transverse momentum of each jet is corrected in order to have uniform response over the full  $\eta^{\text{jet}}$ , and  $p_{\text{T}}^{\text{jet}}$  range [8]. In data, it is additionally corrected to account for data-simulation differences. The latter correction can impact the evaluation of the data-to-simulation ratio. To estimate this effect, the uncertainties on the correction factors that are only applied to the data samples are varied up and down within their  $1\sigma$ -uncertainties.

The effect of the jet  $p_{\text{T}}$  variation on the data-to-simulation ratio is of minor importance and range between 0.5 – 0.7%.

## Uncertainty on the pileup reweighting

Finally, an uncertainty due to the adjustment of the simulated events to the pileup distribution in data is evaluated.

To account for this uncertainty, the effect of a 5.0% up- and downward variation of the minimum-bias cross section (69.4 mb) on the resolution is evaluated, following the recommended procedure from [17]. The resulting uncertainties are almost negligible and ranges between 0.1 – 0.2%.

# 1.6 Results

The data-to-simulation resolution scale factors  $\rho_{\text{res}}$  are determined in  $19.7 \text{ fb}^{-1}$  of  $pp$ -collision data at  $\sqrt{s} = 8 \text{ TeV}$  with the methodology described in Chapter 1.4. In each  $\alpha$ -,  $p_{\text{T}}^{\gamma}$ - and  $|\eta^{1^{\text{st}} \text{ jet}}|$ -bin, the width of the 99% truncated response histogram is determined in simulation and data. Afterwards, the extrapolation to zero additional jet activity is carried out, by fixing the imbalance  $q$  in simulation and in data to the value extracted from the imbalance extrapolation in simulation. Exemplary extrapolations for the imbalance,

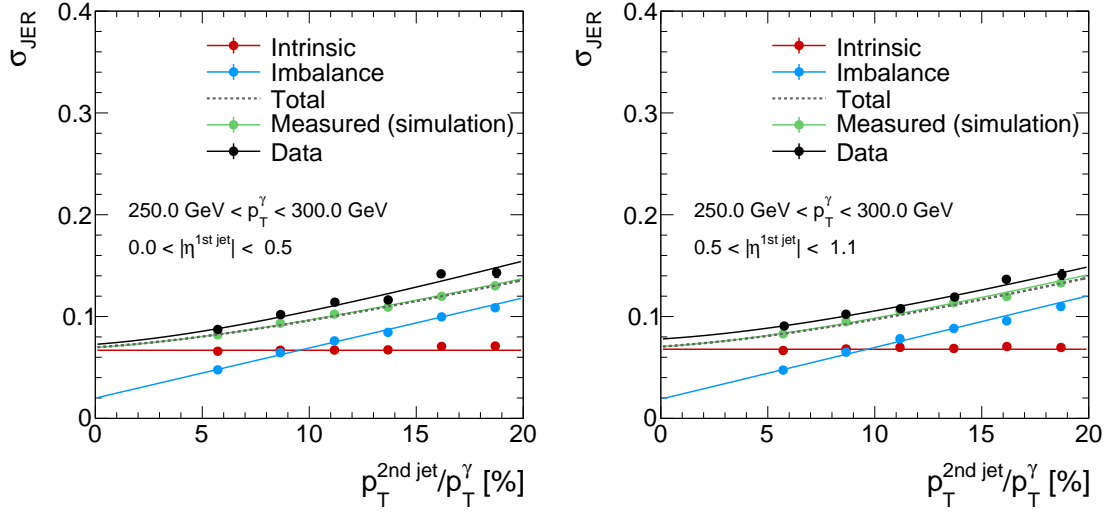


Figure 1.15: Two examples of the alpha dependency of the measured jet transverse-momentum resolution in data (black dots), in simulation (green dots) and of the intrinsic (red dots) and the imbalance (blue dots) part of the resolution in simulated events. All resolutions are fitted with the corresponding functions introduced in Chapter 1.4 (Eqs. (1.6)- (1.8)). The total resolution (grey dotted line) is the addition in quadrature of the imbalance (blue line) and the intrinsic (red line) fit functions.

the intrinsic and the measured resolution in simulation and the measured resolution in data are shown in Fig. 1.15. The full set of figures for each  $p_T^\gamma$  and  $|\eta^{1st \text{ jet}}|$  bin can be found in Appendix A.4.

Finally, the extracted resolutions in data and simulation in every  $p_T^\gamma$  bin are divided and a constant is fitted to this ratio

$$\frac{\sigma_{\text{JER}}^{\text{data}}}{\sigma_{\text{JER}}^{\text{MC}}} (p_T^\gamma) . \quad (1.10)$$

In Fig. 1.16, the results for all four  $|\eta^{1st \text{ jet}}|$ -ranges are depicted. The  $\chi^2/\text{NDF}$ -values for the four fits vary between 0.23 and 2.53. Thus, a constant fit is justified, and one value for every  $|\eta^{1st \text{ jet}}|$ -bin will be reported.

The resulting  $\rho_{\text{res}}$  is always larger than one, which means that the resolution in data is always worse than the resolution in simulation. The values of the fits range from 1.067 (for the first  $\eta^{\text{jet}}$ -bin) to 1.199 (for the last  $\eta^{\text{jet}}$ -bin).

The systematic uncertainties are evaluated as described in the previous chapter. The single uncertainties are taken as upper and lower boundary of the 68% uncertainty band and are added in quadrature to get the total systematic uncertainty. Table 1.6 summarises the data-to-simulation ratio results determined with data collected during the year 2012

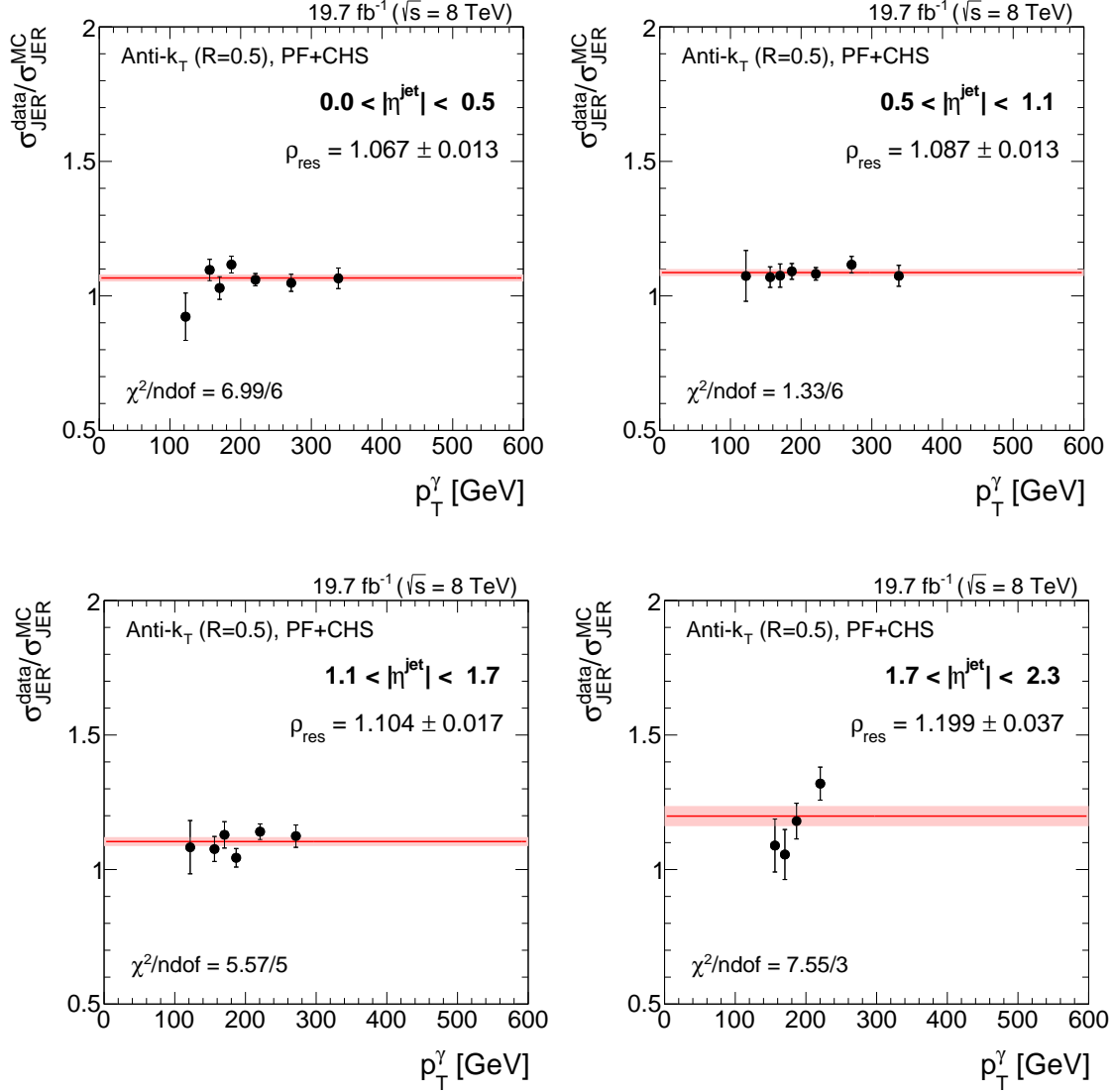


Figure 1.16: Data-to-simulation resolution ratios  $\rho_{\text{res}}$  (black dots), fitted with a horizontal line (red line) for four different  $|\eta^{\text{jet}}|$ -ranges. The fit uncertainties are depicted with light red error bands.

with their statistical and systematic uncertainties. The visualised result can be found in Fig. 1.17.

Though the  $\gamma + \text{jet}$  analysis is known for producing highly precise results, the systematic uncertainties are still dominating. This is mainly caused by the uncertainty on the simulation of out-of-cone showering. The statistical limitation of this analysis is due to the collected data at the CMS detector. The number of simulated events is roughly eight times larger.

Table 1.6: Data-to-simulation resolution scale factors  $\rho_{\text{res}}$  with statistical and systematic uncertainties.

$ \eta^{\text{jet}} $	$\rho_{\text{res}}$	stat.	sys.
0.0 – 0.5	1.067	$\pm 0.013$	$+0.025$ $-0.024$
0.5 – 1.1	1.087	$\pm 0.013$	$+0.039$ $-0.039$
1.1 – 1.7	1.104	$\pm 0.017$	$+0.049$ $-0.049$
1.7 – 2.3	1.199	$\pm 0.037$	$+0.075$ $-0.075$

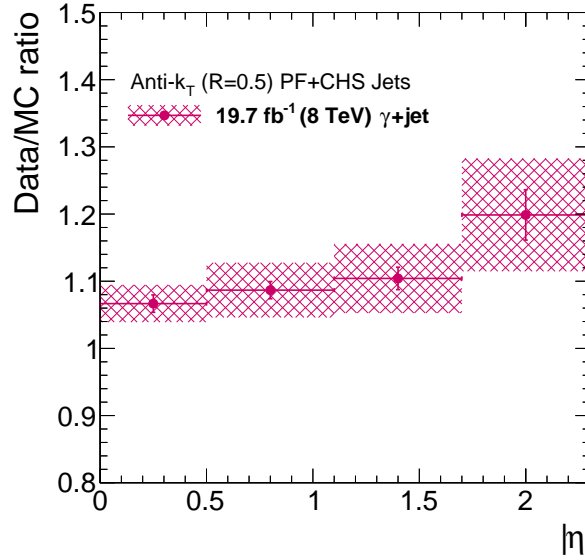


Figure 1.17: The measured data-to-simulation resolution ratio in  $\gamma + \text{jet}$  events using data recorded in the year 2012. The red band depicts the total uncertainty whereas the error bars show the statistical uncertainty only.

### 1.6.1 Comparison to 2011 measurement

A comparison of the data-to-simulation resolution scale factors  $\rho_{\text{res}}$  between this analysis and the results of 2011 which were determined from a dijet data sample [9] can be found in Fig. 1.18. It can be seen, that throughout the whole  $\eta^{\text{jet}}$ -range the data-to-simulation resolution ratios  $\rho_{\text{res}}$  are systematically larger for the result in 2011. Comparing the precision of both measurements, the  $\gamma + \text{jet}$  analysis is for all  $\eta$ -bins more precise than

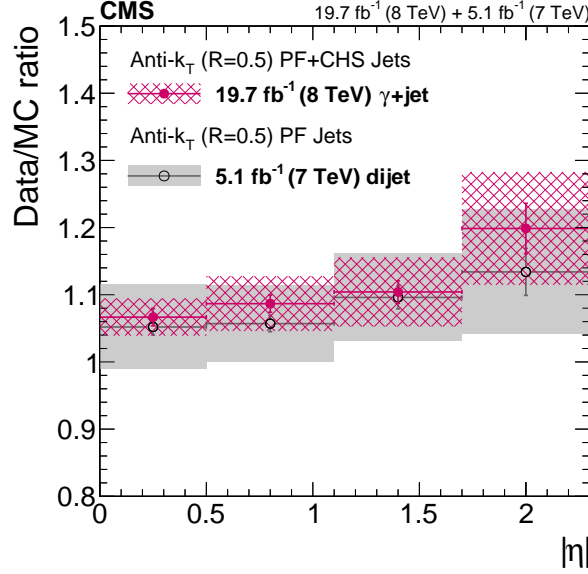


Figure 1.18: Data-to-simulation jet  $p_T$  resolution ratio determined from  $\gamma$ +jet events from 2012 compared to dijet results from 2011. The grey and magenta bands correspond to the full uncertainties, whereas the error bars depict the statistical uncertainties only.

the analysis done with dijet events. This is due to the smaller systematic uncertainties of this analysis which compensates for the better statistical precision of the QCD-multijet sample due to the large cross section.

### 1.6.2 Comparison to 2012 dijet measurement

A jet  $p_T$  resolution measurement using dijet events was also carried out in 2012 [8, 18]. A comparison of the here presented measurement using  $\gamma$  + jet events to the measurement with dijet events can be found in Fig. 1.19. Both measurements are compatible within their uncertainties. It can be seen that the statistical precision is much better for the measurement with QCD-multijet events because of the larger cross section. The systematic uncertainties are of comparable size for small pseudorapidity bins and are larger for high  $|\eta^{\text{jet}}|$  in the here presented measurement. This is due to the uncertainty on the simulation of the out-of-cone showering. This uncertainty plays a smaller role in the dijet measurement (between 0.4% and 1.5%) as the effect by out-of-cone showering partly cancels out in case of two balanced jets.

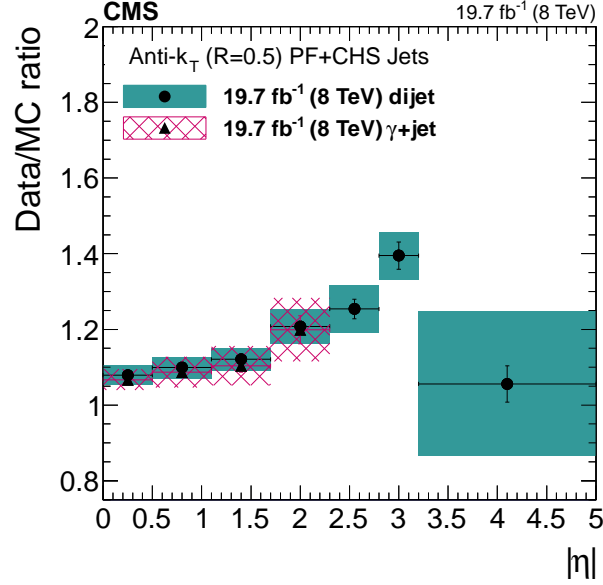


Figure 1.19: Data-to-simulation jet  $p_T$  resolution ratio determined from  $\gamma$ +jet events from 2012 compared to dijet results from 2012. The blue and magenta bands correspond to the full uncertainties, whereas the error bars depict the statistical uncertainties only.

## 1.7 Discussion and conclusion

The difference of the jet transverse-momentum resolution between data and simulation is an important input for many analyses at CMS, including searches for physics beyond the Standard Model using QCD-multijet events, e. g. [3–5].

In this analysis, the first measurement of the data-to-simulation scale factors  $\rho_{\text{res}}$  using  $\gamma$ +jet events with  $19.7 \text{ fb}^{-1}$   $pp$ -collision data at  $\sqrt{s} = 8 \text{ TeV}$  collected in 2012 at the CMS detector is presented. The analysis relies on the methodology developed in [6, 7]. During the study, it was found that the jet transverse-momentum response depends on the topology of additional jet activity in the events, leading to a double peak structure. This was not accounted for in previous analyses [6, 7]. Therefore, a new method has been developed within this thesis to consistently deal with the distortion of the response distribution due to additional jets from initial and final state radiation (see Section 1.4).

The resolution in data is found to be systematically larger than in simulation by around



7% to 20% throughout the investigated  $\eta^{\text{jet}}$  plane. A possible  $p_{\text{T}}^{\text{jet}}$  dependence of the resolution scale factors  $\rho_{\text{res}}$  is not visible. Thus, the ratio is parametrised with a constant for each  $\eta^{\text{jet}}$ -bin. The accuracy of the measurement is dominated by systematic uncertainties, leading to a total uncertainty of 3% to 8%. The results of this analysis compare well to similar studies, including a dijet study at 8 TeV [8,18]. Both measurements are compatible within their statistical and systematic uncertainties.

For a future measurement, a reduction of the uncertainties is desirable. The main source of uncertainty is the systematic uncertainty on the simulation of out-of-cone showering. Within this analysis, this uncertainty was estimated by varying the jet clustering radius from  $R=0.5$  to  $R=0.7$ . This approach might overestimate the uncertainty, since the difference in  $\rho_{\text{res}}$  associated with different jet clustering radii may include other effects than out-of-cone showering. Thus, a more detailed investigation of the quality of out-of-cone showering simulation could yield a reduced uncertainty of the  $\rho_{\text{res}}$  measurement using  $\gamma + \text{jet}$  events.

Furthermore, an increase in the statistical precision is desirable to allow for the determination of resolution scale factors in the high pseudorapidity regions which have not been accessible so far.



## A Measurement of the jet transverse-momentum resolution

### A.1 Pileup reweighting

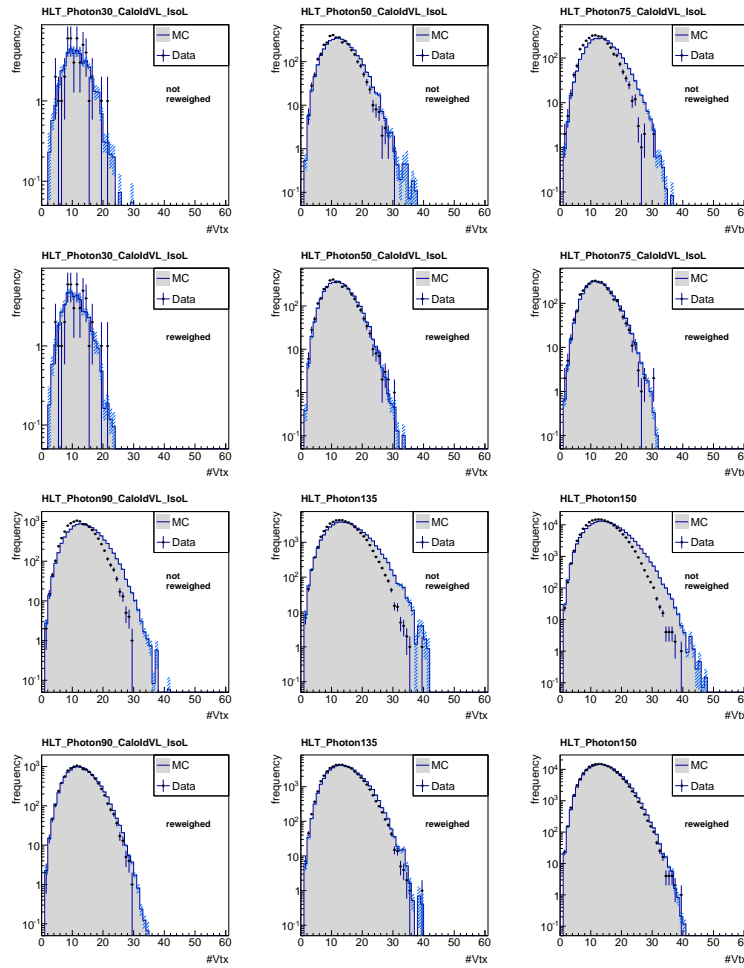


Figure 1.20: The number of primary vertices in data and simulation before (1st row) and after (2nd row) pileup reweighting for  $36 \text{ GeV} < p_T^\gamma < 60 \text{ GeV}$  (left),  $60 \text{ GeV} < p_T^\gamma < 88 \text{ GeV}$  (middle), and  $88 \text{ GeV} < p_T^\gamma < 105 \text{ GeV}$  (right) and the number of primary vertices in data and simulation before (3rd row) and after (4th row) pileup reweighting for  $105 \text{ GeV} < p_T^\gamma < 149 \text{ GeV}$  (left),  $149 \text{ GeV} < p_T^\gamma < 165 \text{ GeV}$  (middle), and  $165 \text{ GeV} < p_T^\gamma$  (right).

## 550 A.2 Summary of all selection requirements

Table 1.7: Summary of all selection criteria for the measurement of the jet transverse-momentum resolution with  $\gamma + \text{jet}$  events.

One jet with	$p_T > 10 \text{ GeV}$ Neutral hadron fraction $< 0.90$ Neutral electromagnetic fraction $< 0.90$ Number of constituents $> 1$ Charged hadron fraction $> 0$ Charged hadron multiplicity $> 0$
One photon with	$p_T > 36 \text{ GeV}$ $ \eta  < 1.3$ $\frac{H}{E} < 0.05$ $\sigma_{in\eta} < 0.013$ ECAL isolation $< 4.2 \text{ GeV} + 0.0060 \cdot p_T^\gamma$ HCAL isolation $< 2.2 \text{ GeV} + 0.0025 \cdot p_T^\gamma$ Track Isolation $< 2.0 \text{ GeV} + 0.0010 \cdot p_T^\gamma$ Pixel seed veto
Event-based selection	$p_T^{2^{\text{nd}} \text{ jet}} > 10 \text{ GeV}$ $\frac{p_T^{2^{\text{nd}} \text{ jet}}}{p_T^\gamma} < 0.20$ $\Delta\Phi(1^{\text{st}} \text{ jet}, \gamma) > 2.95$

## 551 A.3 Generator-level jet flavour definition

552 The algorithmic flavour definition uses the following discrimination:

- 553 • Try to find the parton that most likely determines the properties of the jet and assign  
554 that flavour as true flavour

- Here, the “final state” partons (after showering, radiation) are analysed (also within  $\Delta R < 0.3$  of reconstructed jet cone)
- Jets from radiation are matched with full efficiency
- If there is a b/c within the jet cone: label as b/c
- Otherwise: assign flavour of the hardest parton

## A.4 Extrapolation plots

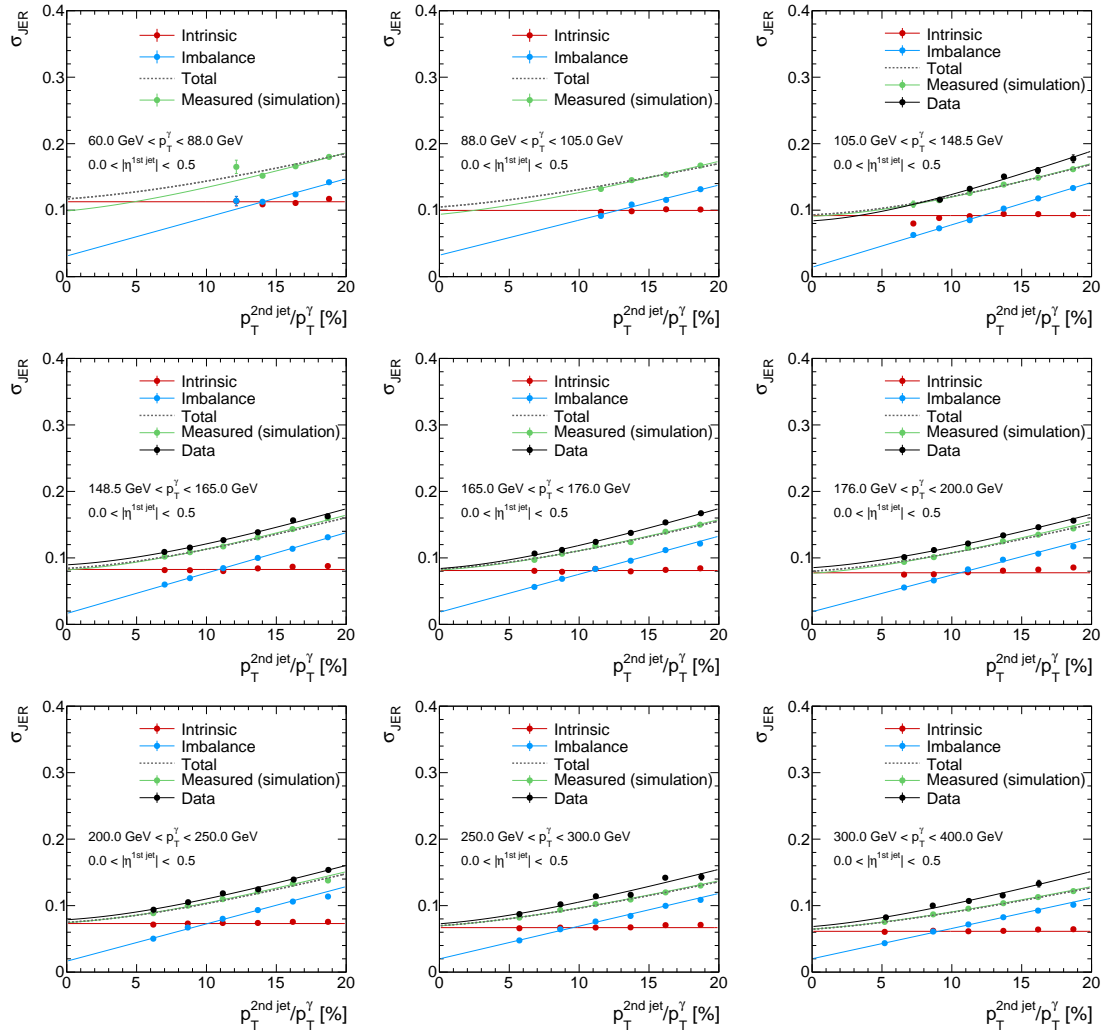


Figure 1.21:  $\sigma_{\text{JER}}(\alpha)$  of the intrinsic, imbalance and measured resolution in simulation and the resolution measured in data for all  $|\eta^{1\text{st jet}}|$  and  $p_T^\gamma$  bins.

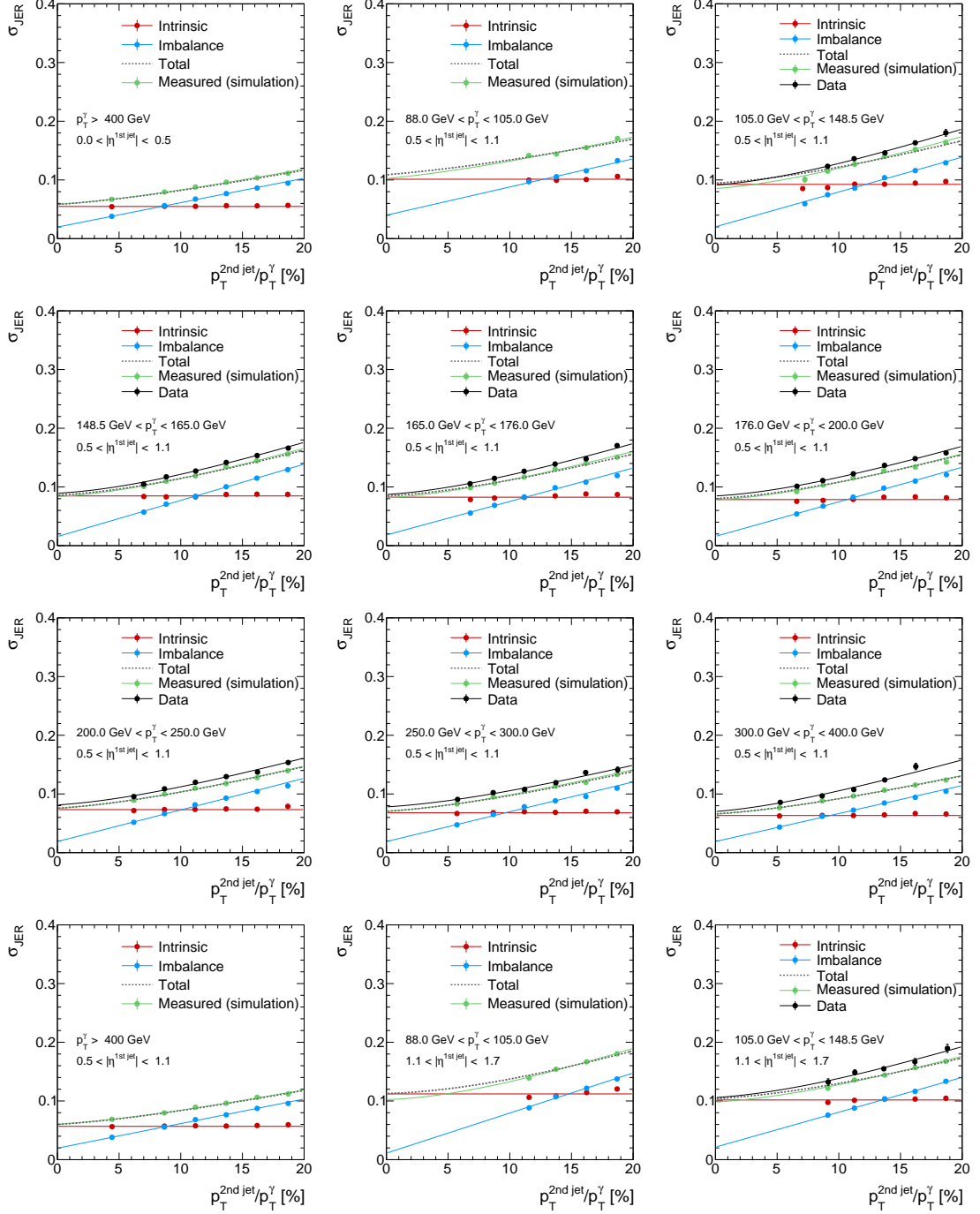


Figure 1.22: Continued from Fig. 1.21:  $\sigma_{\text{JER}}(\alpha)$  of the intrinsic, imbalance and measured resolution in simulation and the resolution measured in data for all  $|\eta^{1\text{st jet}}|$  and  $p_T^\gamma$  bins.

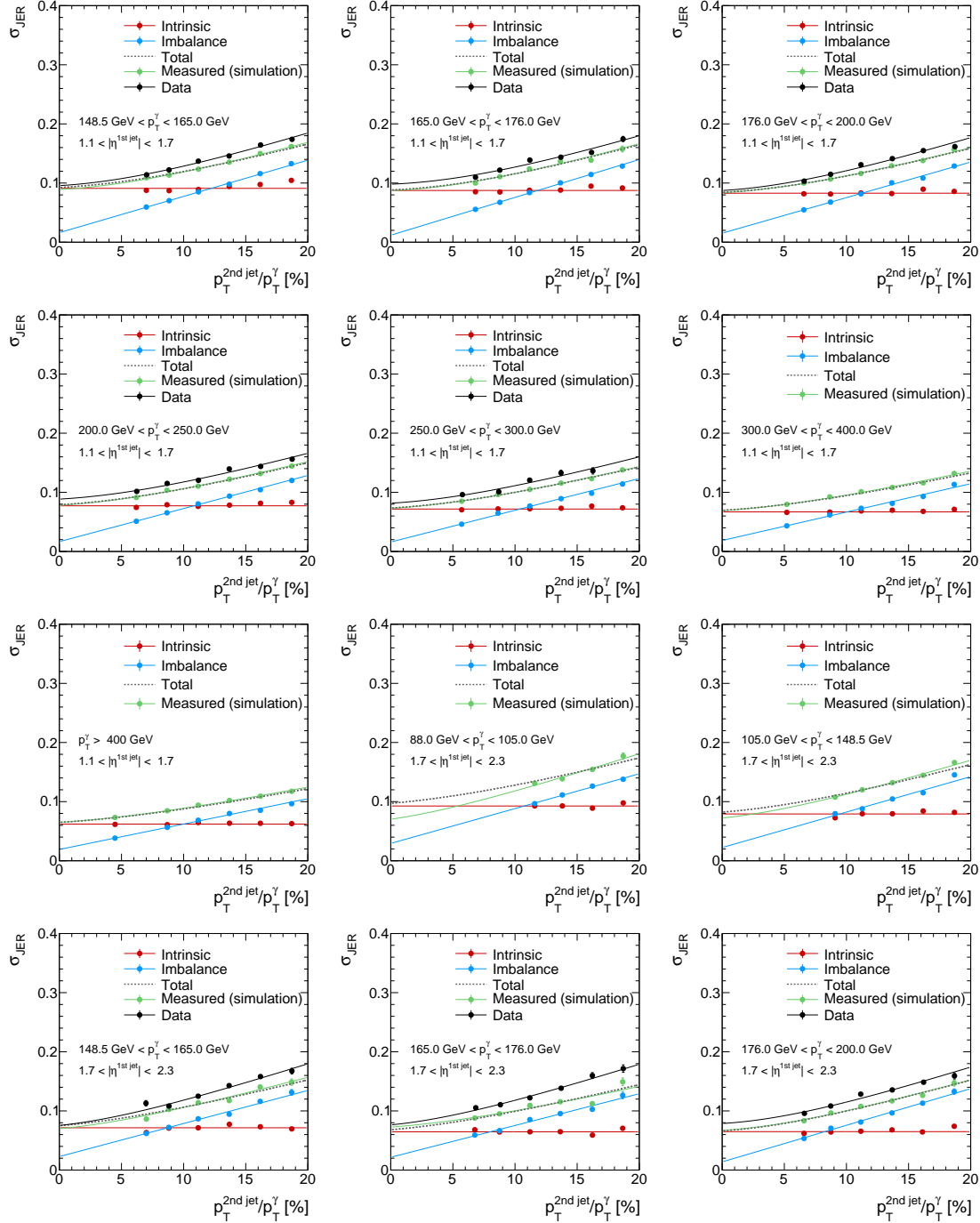


Figure 1.23: Continued from Fig. 1.22:  $\sigma_{\text{JER}}(\alpha)$  of the intrinsic, imbalance and measured resolution in simulation and the resolution measured in data for all  $|\eta^{1\text{st jet}}|$  and  $p_T^\gamma$  bins.

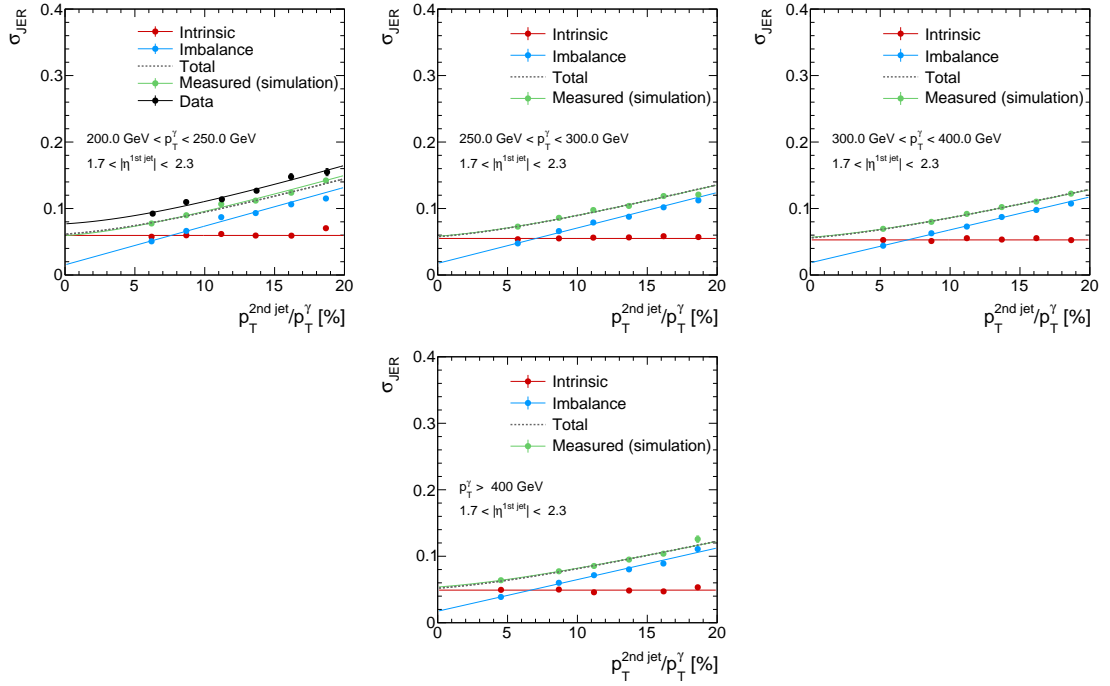


Figure 1.24: Continued from Fig. 1.23:  $\sigma_{\text{JER}}(\alpha)$  of the intrinsic, imbalance and measured resolution in simulation and the resolution measured in data for all  $|\eta^{1\text{st jet}}|$  and  $p_T^\gamma$  bins.



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