

Part 1

The Standard Model and its supersymmetric extension

1.1 The Standard Model of particle physics

The formulation of a relativistic quantum field theory and of spontaneous symmetry breaking (SSB) by the Brout-Englert-Higgs mechanism, allowed to build a theory which is capable of explaining almost all observations of particle physics at colliders until today. This theory is known as the Standard Model (SM) of particle physics. Its last missing piece, the Higgs boson, was found at the LHC in the year 2012 [1, 2].

The Standard Model is a $SU(3)_C \times SU(2)_L \times U(1)_Y$ non-abelian gauge theory. “After” spontaneous symmetry breaking, its symmetries are reduced to $SU(3)_C \times U(1)_{EM}$. All particles that were found until today are contained in it¹. Furthermore, it is able to describe three of the four fundamental forces: the strong, weak and electromagnetic force.

Despite its great success, there are many open questions that cannot be addressed within the Standard Model. These “shortcomings” of the Standard Model will be discussed in Section 1.1.4. Before, however, a small introduction to the theory (Sections 1.1.1-1.1.3) of the Standard Model is given. It is not meant as a complete description. For a thorough and extensive introduction, the reader is referred to [3–5].

1.1.1 The particle content

First, it should be noted, that since the Standard Model is a quantum field theory, each type of field corresponds to a different particle type and vice versa.

The Standard Model of particle physics contains three different particle types, or three different types of fields. First, there are the so-called “matter particles”, which are all spin 1/2 particles in the SM. Second, the forces are described by spin 1 vector bosons. And finally, in order to give masses to all particles, the Standard Model embeds the Higgs boson, a scalar spin 0 particle.

Fermions in the Standard Model

The fermionic content can be further subdivided into leptons and quarks. In contrast to quarks, leptons are not strongly interacting, thus they only couple weakly and - in case they carry a non-zero charge - electromagnetically to other particles. Both, the quarks and

¹One can argue, that the right-handed neutrino, which is proven to exist, is not contained. But as at least the left-handed neutrino is embedded, we want to ignore that for a moment.

the leptons are ordered into three different families. Across these families, all quantum numbers are conserved. They only differ by their mass.

All left-handed particles of each family form a $SU(2)_L$ doublet, which causes the coupling via the weak force. The right-handed partners form $SU(2)$ singlets, thus, don't couple via the weak interaction. As quarks carry one further quantum number, the colour, they are additionally grouped into $SU(3)_C$ triplets.

Vector bosons in the Standard Model

As mentioned before, the vector bosons describe three of the four fundamental forces. There is one gauge boson corresponding to every generator of the above mentioned gauge groups. For $U(1)_Y$, it is the B -boson, for $SU(2)_L$, there are three gauge bosons $W^{1,2,3}$ and finally eight gauge bosons $G^{1\dots 8}$ for $SU(3)_C$, which are called gluons. As the B -field and the neutral W^3 -field can mix, a change in the basis is possible “after” SSB and leads to the well known photon and Z -boson.

The Higgs boson

The Higgs boson which was already predicted 50 years ago by Peter Higgs [6, 7] and was found by the LHC experiments CMS and ATLAS in 2012 [1, 2] plays a somehow extraordinary role. This particle is a consequence of spontaneous symmetry breaking after rotating three of the four degrees of freedom of the Higgs field to the longitudinal components of the W - and Z -bosons. It is the only known fundamental scalar particle.

An overview of all Standard Model particles and their transformation properties are shown in Table 1.1. For the $SU(3)_C$ and $SU(2)_L$ gauge groups, the corresponding representations are given for each of the particle types. For the $U(1)_Y$ gauge group, the corresponding quantum number, the so-called hypercharge, is depicted. If particles transform as singlets under $SU(2)_L$ or $SU(3)_C$, they don't couple via the corresponding force. The hypercharges Y are determined by $Q = Y + I_3$, where Q is the electric charge and I_3 is the third component of the weak isospin with $I^a = \sigma^a/2$, σ^a being the Pauli matrices.

1.1.2 The Lagrangian density

In particle physics, the dynamics of a particle system is described by the Lagrangian density. The Lagrangian density of the Standard Model is the most general set of Lagrangian terms, that are renormalisable and contain all up to date known particles as well as the

Table 1.1: All particles contained in the Standard Model and their transformation properties under $SU(3)_C \times SU(2)_L \times U(1)_Y$. For the gauge groups $SU(3)_C$ and $SU(2)_L$, the representations are listed whereas for $U(1)_Y$ the hypercharge is given.

	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$
Fermions:			
$(\nu_L, e_L)^T$	1	2	-1
e_R	1	1	-2
$(u_L, d_L)^T$	3	2	$+\frac{1}{3}$
u_R	3	1	$+\frac{4}{3}$
d_R	3	1	$-\frac{2}{3}$
Vector bosons:			
B_μ	1	1	0
W_μ^a	1	3	0
G_μ^a	8	1	0
Higgs boson: H	1	2	-1

above mentioned symmetries. The full SM Lagrangian density reads as follows:

$$\begin{aligned}
\mathcal{L} = & (D_\mu \Phi)^\dagger (D^\mu \Phi) - \mu^2 \Phi^\dagger \Phi - \frac{\lambda}{4} (\Phi^\dagger \Phi)^2 \\
& + \bar{L}_i^L i \not{D} L_i^L + \bar{e}_i^R i \not{D} e_i^R + \bar{Q}_{ib}^L i \not{D} Q_{ib}^L + \bar{u}_{ib}^R i \not{D} u_{ib}^R + \bar{d}_{ib}^R i \not{D} d_{ib}^R \\
& - \left(Y_{ij}^e \bar{L}_i^L \Phi e_j^R + Y_{ij}^u \bar{Q}_{ib}^L \Phi u_{jb}^R + Y_{ij}^d \bar{Q}_{ib}^L \Phi d_{jb}^R + h.c. \right) \\
& - \frac{1}{4} (B_{\mu\nu} B^{\mu\nu} + W_{\mu\nu}^a W^{a\mu\nu} + G_{\mu\nu}^a G^{a\mu\nu}),
\end{aligned} \tag{1.1}$$

with $\not{D} = \gamma_\mu D^\mu$ and the covariant derivative $D^\mu = \partial^\mu + ig' Y_W B^\mu - ig C_1 I^a W_a^\mu - ig_S C_2 T^a G_a^\mu$ including the three gauge couplings g , g' and g_S . I^a and T^a denote the generators of the $SU(2)_L$ and $SU(3)_C$, respectively. They are connected to the three Pauli matrices and the eight Gell-Mann matrices by $I^a = \frac{\sigma^a}{2}$ and $T^a = \frac{\lambda^a}{2}$. The sum of the hypercharge Y_W and the third component of the weak isospin yields the electrical charge $Q = Y_W + I_3$. Furthermore, it is $C_1 = 1$ for doublets and $C_1 = 0$ for singlets under $SU(2)_L$, $C_2 = 1$ for

triplets and $C_2 = 0$ for singlets under $SU(3)_C$.

The first line in Eq. (1.1) corresponds to the kinetic term of the Higgs field and its potential. Via this Higgs field, it is possible to give masses to the Z - and W^\pm -bosons as well as the fermions. This will be explained in detail in the following Section 1.1.3. The second line describes the kinetic terms of the leptons and quarks. The index i represents the three different families ($i = 1, 2, 3$). Since they are spin 1/2 particles, they can be described with the help of Dirac spinors. The left-handed leptons and quarks are described as $SU(2)_L$ doublets, $L_I^L = (\nu_{eL}, e_L)_i$, $Q_I^L = (u_L, d_L)_i$, the right-handed as singlets under $SU(2)_L$ e_i^R , u_i^R , d_i^R . Quarks carry a further quantum number, the colour, which is indicated by the index b with $b = 1, 2, 3$. Quarks transform as triplets under the $SU(3)_C$ gauge group. The third line contains the interaction terms between the fermions and the Higgs boson, called Yukawa interactions. After SSB, these terms lead to the fermion mass terms as can be seen later. The last line correspond to the kinetic terms of the gauge fields. These are connected to the field strength tensors by

$$\begin{aligned}
B^{\mu\nu} &\equiv \partial^\mu B^\nu - \partial^\nu B^\mu \\
W^{\mu\nu} &\equiv \partial^\mu W^\nu - \partial^\nu W^\mu - ig [W^\mu, W^\nu] \\
&= \left(\partial^\mu W_i^\nu - \partial^\nu W_i^\mu + g \epsilon_{ijk} W_j^\mu W_k^\nu \right) \frac{\sigma_i}{2} \equiv \frac{\sigma_i}{2} W_a^{\mu\nu} \\
G^{\mu\nu} &\equiv \partial^\mu G^\nu - \partial^\nu G^\mu - ig_S [G^\mu, G^\nu] \\
&= \left(\partial^\mu G_a^\nu - \partial^\nu G_a^\mu + g_S f_{abc} G_b^\mu G_c^\nu \right) \frac{\lambda_a}{2} \equiv \frac{\lambda_a}{2} G_a^{\mu\nu}.
\end{aligned} \tag{1.2}$$

The factors ϵ_{ijk} and f_{abc} are the structure constants of the corresponding Lie groups. The notation implies a summation over all indices that appear twice.

1.1.3 The Brout-Englert-Higgs mechanism

An essential ingredient of the Standard Model is the Brout-Englert-Higgs mechanism (BEH mechanism), earlier also called Higgs mechanism. It was developed by Peter Higgs, Robert Brout and François Englert in the 1960s [6–11]. Based on work from Sheldon Glashow [12], it was later applied by Steven Weinberg and Abdus Salam to a $SU(2) \times U(1)$ gauge theory [13, 14]. By this, a renormalisable theory of the weak and the electromagnetic interactions was born.

Mass terms of the gauge bosons

Due to the BEH mechanism, it is possible to give masses to the W^\pm - and Z -bosons. A scalar field Φ (Higgs field) is required, which has a non-zero vacuum expectation value. This is possible, if the mass parameter μ in front of the bilinear term in line one of Eq. (1.1)

is smaller than zero and $\lambda > 0$ at the same time.

The resulting potential of the Higgs field is then the famous “Mexican hat” potential. Expanding the Lagrangian density around the minimum of $\Phi = (0, v)$, the gauge symmetries of $SU(2)_L \times U(1)_Y$ are spontaneously broken and only the electrical charge conserving symmetry $U(1)_{EM}$ remains. After a unitary transformation, three of the four degrees of freedom of the Higgs field are absorbed by the gauge fields. Thus, “after” SSB, the part of the Lagrangian containing the scalar field is as follows

$$\mathcal{L}_{\text{Higgs}} = \frac{1}{2} (\partial_\mu h^0)^\dagger (\partial^\mu h^0) - \mu^2 (h^0)^2 + \frac{1}{2} v^2 g^2 W_\mu^- W^{+\mu} + \frac{1}{4} v^2 (g^2 + g'^2) Z_\mu Z^\mu + \text{interaction terms} \quad (1.3)$$

One kinetic and one mass term for one of the degrees of freedom of the Higgs fields remains, which is the Higgs boson (h^0). Furthermore, three of the four gauge bosons acquire a mass. The remaining gauge boson, the photon, remains massless because of the conserved $U(1)_{EM}$ gauge symmetry.

The mass eigenstates of the gauge bosons in Eq. (1.3) are obviously different to the interaction eigenstates in Eq. (1.1). The diagonalisation of the neutral mass matrices is described by the Weinberg angle θ_W

$$\begin{pmatrix} A_\mu \\ Z_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta_W & -\sin \theta_W \\ \sin \theta_W & \cos \theta_W \end{pmatrix} \begin{pmatrix} B_\mu \\ W_\mu^3 \end{pmatrix}. \quad (1.4)$$

For the charged gauge bosons, the relation between $W_{1,2}$ and W^\pm is the following

$$W_\mu^\pm = \frac{1}{\sqrt{2}} [W_\mu^1 \mp W_\mu^2]. \quad (1.5)$$

Consequently, the masses of the gauge bosons are the following (with $\sin \theta_W = \frac{g'}{\sqrt{g^2 + g'^2}}$)

$$\begin{aligned} M_H &= \sqrt{2} \mu \\ M_W &= \frac{g}{\sqrt{2}} v \\ M_Z &= \frac{1}{\sqrt{2}} v \sqrt{g^2 + g'^2} \\ M_\gamma &= 0. \end{aligned} \quad (1.6)$$

The first direct observation of the Z - and W^\pm -bosons was made in $p\bar{p}$ -collisions in the year 1983 at the Super Proton Synchrotron (SPS) at CERN [15, 16]. The experimental values of the masses are $m_Z = 91.1876 \pm 0.0021$ GeV and $m_{W^\pm} = 80.385 \pm 0.015$ GeV [17]. Finally, as mentioned several times before, the Higgs boson was found at the LHC in the

year 2012 [1,2]. The mass is measured to $m_{h^0} = 125.09 \pm 0.21(\text{stat.}) \pm 0.11(\text{sys.}) \text{ GeV}$ [18].

Mass terms of the fermions

Fermion mass terms cannot be easily inserted into the Lagrangian density in Eq. (1.1), since they would violate the imposed gauge symmetries. With the help of the BEH mechanism it is possible to generate fermion mass terms via the Yukawa interaction terms (line three of Eq. (1.1)). After spontaneous symmetry breaking, the Yukawa interactions lead to the following mass terms (colour indices are suppressed)

$$\mathcal{L}_{\text{Yukawa}} = - \left(Y_{ij}^e v \bar{e}_i^L e_j^R + Y_{ij}^u v \bar{u}_i^L u_j^R + Y_{ij}^d v \bar{d}_i^L d_j^R + h.c. \right) + \text{interaction terms} \quad (1.7)$$

The fermion masses are thus described by the following mass matrices

$$M_{ij}^e = Y_{ij}^e v \quad M_{ij}^u = Y_{ij}^u v \quad M_{ij}^d = Y_{ij}^d v \quad (1.8)$$

Since the Standard Model does not contain right-handed neutrinos, there are no gauge invariant Yukawa interactions, that could produce mass terms for neutrinos.

1.1.4 Limitations of the Standard Model

Despite the great success of the Standard Model, there remain observations and theoretical considerations that cannot be answered within the SM. In the following, the most important of such “limitations” shall be reviewed.

First of all, the Standard Model suffers from the so-called hierarchy problem. It is caused by the occurrence of quadratic divergencies in the calculation of the Higgs mass. The appearance of infinities is not uncommon in higher order calculations and happens for all particles. Still, for scalar particles the infinite term is quadratically divergent, which makes a huge difference compared to the logarithmic divergencies for fermion self-energies. When considering the Standard Model valid up to the Planck scale, an extraordinary fine-tuning would be needed to cancel a large bare mass with large counter terms

$$m_{h^0}^{\text{ren } 2} = m_{h^0}^{\text{bare } 2} + \Delta m_{h^0}^2 \quad (1.9)$$

to end up with a Higgs mass of about 125 GeV. Thus, this renormalisation procedure, even if mathematically possible, is regarded as highly unnatural. This raises the question why the Higgs mass is so small, despite the presence of such massive radiative corrections to the bare mass. A formulation of naturalness was given by t’Hooft in 1977 [19]. He stated,

that a small parameter can only be regarded natural, if the symmetries of the theory are enhanced by setting this parameter to zero. In the Standard Model, though, there is no enhancement of the symmetries of the Lagrangian by setting $\mu = 0$. Thus, the small mass of the Higgs boson compared to the Planck scale is considered as highly unnatural.

A further and probably the most striking shortcoming of the Standard Model is the missing fourth fundamental force, the gravitational force. Within the SM, it is not possible to add renormalisable terms, that can describe the gravitational force. Although, gravity is not important for particle physics at energies that are accessible at current particle colliders (it only becomes important at the Planck scale $\sim 10^{19}$ GeV), the fact that it cannot be embedded into the Standard Model leads to an understanding of the SM as an effective theory, only valid for low energies. Thus, it is obviously not an ultimate theory and something must be beyond.

Furthermore, in particle physics there is always the wish to describe nature with a theory as simple as possible. This usually implies the effort to embed the Standard Model into a higher symmetry group. To achieve a simplification by unifying the three fundamental forces is usually done within so-called Grand-Unified-Theories (GUTs). Calculating the running of the coupling constants in the Standard Model, the couplings seem to meet at a scale of $M_{\text{GUT}} \sim 10^{15}$ GeV. Unfortunately, they don't meet exactly. Therefore, a unification is not achievable in the Standard Model under the assumption that there are no new particles up to the GUT scale.

Finally, there is experimental evidence that cannot be explained within the Standard Model. Astrophysical observations suggest that there is a large amount of dark matter (DM) in the universe, that cannot be explained with the particle content of the Standard Model. Measurements of the velocity curves of galaxies, e.g. M33 [20] show discrepancies between the observed velocities and the predicted velocities by the visible matter. Furthermore, observations of the cosmic microwave background [?] as well as Supernova red shifts [?] and baryon acoustic oscillations [?] strongly suggests the existence of Dark Matter. The share of non-visible matter to the total amount of matter in the universe is estimated to be 84% [21]. Unfortunately, there is no suitable (only weakly interacting) candidate within the SM, that can make up the full DM contribution.

In the following Chapter 1.2, a theory is introduced, that can address most of the above mentioned problems. This theory is called supersymmetry.

1.2 Supersymmetry

As noted in the last chapter, the Higgs boson mass suffers from quadratic divergencies through radiative corrections. The reason for the quadratic divergencies is due to the fact, that the Lagrangian density does not contain further symmetries for $\mu \rightarrow 0$. This behaviour is typical for scalar particles. For fermions, on the other hand, there is a further symmetry for $m_f = 0$. The Lagrangian density becomes invariant under chiral transformations of the form $\Psi \rightarrow e^{i\vec{\alpha}\frac{\vec{\sigma}}{2}\gamma_5}\Psi$. Although the mass terms of the fermions break this symmetry, it protects the fermions against large radiative corrections.

Due to these considerations, it seems natural to transfer the mechanism of protecting fermion masses by a chiral symmetry to scalar masses as well. This can only be done by connecting fermions with bosons and vice versa. In the 1970s, exactly this linking between the different particle types was achieved. A work from Golfand and Likhtman in the year 1971 stated that an extension of the Poincaré algebra is possible via fermionic generators [22]. R. Haag, J. Lopuszanski and M. Sohnius finalised these considerations by showing that with the help of fermionic generators a connection between space-time symmetries and internal symmetries is possible [23]. The extensions of a symmetry group by fermionic generators is called supersymmetry (SUSY). These were the foundation of supersymmetric theories.

In the following, the most important aspects of supersymmetric theories are discussed. For a detailed introduction the reader is referred to [24–26].

In the subsequent sections, the description is restricted to the case of $\mathcal{N} = 1$ supersymmetry, i. e. there is only one supersymmetric generator and thus only one supersymmetric partner for every particle. A supersymmetric transformation transfers every bosonic state into a fermionic state and vice versa

$$\begin{aligned} Q |\text{boson}\rangle &= |\text{fermion}\rangle \\ Q |\text{fermion}\rangle &= |\text{boson}\rangle. \end{aligned} \tag{1.10}$$

The most important (anti-) commutation relations for SUSY algebra with fermionic gen-

erators Q are

$$\begin{aligned}\{Q_\alpha, Q_\beta\} &= \{Q_\alpha^\dagger, Q_\beta^\dagger\} = 0, \\ [Q_\alpha, P_\mu] &= [Q_\alpha^\dagger, P_\mu] = 0, \\ \{Q_\alpha, Q_\alpha^\dagger\} &= 2\sigma_{\alpha\dot{\alpha}}^\mu P_\mu.\end{aligned}\tag{1.11}$$

Here, P_μ denotes the four component generator of translations and $\sigma^\mu = (\mathbb{1}, \sigma_i)$ with the Pauli matrices σ_i . From the second relation in (1.11) follows

$$[Q_\alpha, P^2] = [Q_\alpha^\dagger, P^2] = 0.\tag{1.12}$$

Equation 1.12 implies, that particles that are transformed into each other with the generator Q need to have the same eigenvalues of P^2 , thus, also the same masses. This obviously imposes a problem, since no “scalar electron” was ever found with a mass of 0.51 MeV. Therefore, SUSY must be broken. There are many ideas how the breaking can actually happen. However, since up to now, only little is known about the breaking mechanism, usually further terms which break SUSY explicitly, are added by hand to the Lagrangian density. These terms can parametrise SUSY breaking without any knowledge about the breaking mechanism. One condition is however imposed on the supersymmetry breaking terms: they should not spoil the naturalness of the new theory, i.e. no new quadratic divergencies shall occur due to these terms. Therefore, they are called soft-breaking terms. How they actually look, will be explained in the Section 1.2.1.

Finally, it shall be discussed how a supersymmetric extension of the Standard Model can give possible answers to the shortcomings of the Standard Model, discussed in Section 1.1.4.

Radiative corrections by fermions always have a factor -1 compared to bosonic corrections. Thus, calculating radiative corrections of the Higgs boson mass in a supersymmetric theory leads in addition to the corrections by SM particles to further corrections by SUSY particles. If SUSY were exact, the quadratic divergencies Δm_h^2 would exactly cancel. However, as argued, SUSY must be broken. The cancellation of quadratic divergencies can therefore only be assured, if the breaking is not too drastic and only logarithmic divergencies remain.

Embedding gravity into a four dimensional quantum field theory proves difficult because of the non-renormalisability of the resulting theory. A possible answer, beyond quantum field theory, are string theories [27], where the existence of a fundamental length - that of the strings - regularises the ultraviolet behaviour and allows for a quantum description of objects in curved space. Yet, the only known procedure to incorporate fermions within a string Lagrangian density consists in adding supersymmetry as a condition. Supersym-

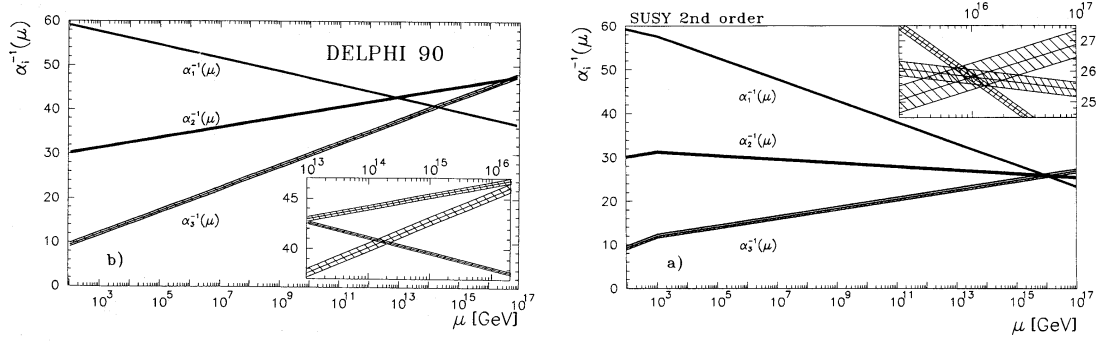


Figure 1.1: The running of the gauge couplings in the Standard Model (left) and in the minimal supersymmetric extension of the SM (right). Taken from [28].

metry thus appears as a fundamental ingredient for a description of quantum gravity.

The renormalisation group equations change under a supersymmetric extension of the Standard Model. By this, a unification of the gauge couplings at a GUT scale of about 10^{16} GeV is possible, as can be seen in Fig. 1.1. It can be nicely seen, that all three gauge couplings cross each other within the uncertainties.

Besides these arguments, SUSY can also provide an answer to the problem of non-visible matter in the universe. If the conservation of the so-called R-parity is required, the lightest supersymmetric particle (LSP) is stable. If this particle is only weakly interacting, it can serve as a good candidate to explain fully or partially the sources of the relic density. R-parity is a multiplicative quantum number with

$$\begin{aligned} P_R &= 1 && \text{SM particles} \\ P_R &= -1 && \text{SUSY particles.} \end{aligned} \tag{1.13}$$

If R-parity is conserved, only terms are allowed in the Lagrangian density, that contain an even number of supersymmetric particles. Therefore, no single SUSY particle can decay into only SM particles and thus, the LSP is stable. The following discussions are restricted to R-parity conserving supersymmetric models.

1.2.1 The MSSM

The supersymmetric extension of the Standard Model with a minimal particle content is called the Minimal Supersymmetric Standard Model (MSSM). In the following section, the particle content of the MSSM is introduced.

1.2.1.1 The particle content of the MSSM

In $\mathcal{N} = 1$ supersymmetry, every SM particle has exactly one supersymmetric partner particle, which leads to a doubling of the particle content in the MSSM with respect to the SM¹. Additionally, it is necessary to introduce a second Higgs doublet to ensure the holomorphicity of the superpotential in the presence of mass terms for the up-type particles. Furthermore, the MSSM only stays free from anomalies if there is a further Higgs doublet [29]. This leads to the fact, that in the MSSM, there are five Higgs bosons instead of only one as in the SM.

In supersymmetry, all particles and their partner particles are described by so-called supermultiplets. Since the generators of the gauge group commute with the generators of supersymmetry, all particles within one supermultiplet have same quantum numbers, besides the spin. In a renormalisable theory, there are two different types of supermultiplets: chiral multiplets, which contain a two-component Weyl spinor describing the fermionic degrees of freedom and a complex scalar field for the bosonic degrees of freedom; vector multiplets containing a vector field and a two-component Weyl spinor. The complete particle content of the MSSM is depicted in Tables 1.2 and 1.3. Since in supersymmetric theories only left-handed Weyl spinors appear in the Lagrangian density, the right-handed particles are described as charge conjugated spinors of the left-handed spinors.

Table 1.2: Chiral supermultiplets in the MSSM.

	spin 0	spin $\frac{1}{2}$	$SU(3)_C, SU(2)_L, U(1)_Y$
squarks/quarks	$(\tilde{u}_L, \tilde{d}_L)$	(u_L, d_L)	3, 2, $+\frac{1}{3}$
	$\tilde{\bar{u}}_L = \tilde{u}_R^\dagger$	$\bar{u}_L = (u_R)^c$	$\bar{3}, 1, -\frac{4}{3}$
	$\tilde{\bar{d}}_L = \tilde{d}_R^\dagger$	$\bar{d}_L = (d_R)^c$	$\bar{3}, 1, +\frac{2}{3}$
sleptons/leptons	$(\tilde{\nu}_{eL}, \tilde{e}_L)$	(ν_{eL}, e_L)	1, 2, -1
	$\tilde{\bar{e}}_L = \tilde{e}_R^\dagger$	$\bar{e}_L = (e_R)^c$	$\bar{1}, 1, +2$
Higgs/higgsinos	(H_u^+, H_u^0)	$(\tilde{H}_u^+, \tilde{H}_u^0)$	1, 2, $+1$
	(H_d^0, H_d^-)	$(\tilde{H}_d^0, \tilde{H}_d^-)$	1, 2, -1

¹The supersymmetric partner particles of the fermions are called sfermions, whereas the partner particles of the gauge (Higgs) bosons are referred to as gauginos (higgsinos).

1.2.1.2 The Lagrangian density of the MSSM

In the following, only the most important parts of the MSSM Lagrangian density will be described. For a complete description of the Lagrangian density, the reader is again referred to [26].

The superpotential

The superpotential of the MSSM contains the self interaction terms of the Higgs bosons and generates the interaction terms of the Higgs bosons with the fermions and their superpartners. As already noted, it is very common to assume R-parity conservation. Hence, no terms appear in the Lagrangian that would violate lepton or baryon number conservation and the lightest supersymmetric particle is stable. Thus, all possible terms are

$$W_{\text{MSSM}} = \mu H_u \cdot H_d - Y_u^{ij} H_u \cdot Q_L^i u_R^{cj} + Y_d^{ij} H_d \cdot Q_L^i d_R^{cj} + Y_e^{ij} H_d \cdot L_L^i e_R^{cj}, \quad (1.14)$$

with the dot product defined as in [25]

$$A \cdot B = \epsilon^{\alpha\beta} A_\alpha B_\beta = A_1 B_2 - A_2 B_1. \quad (1.15)$$

The soft-breaking Lagrangian density

Since supersymmetry is broken, explicit SUSY breaking terms are added to the Lagrangian density. In order not to introduce new sources of quadratic divergencies, only bilinear and

Table 1.3: Vector supermultiplets in the MSSM.

	spin $\frac{1}{2}$	spin 1	$SU(3)_C, SU(2)_L, U(1)_Y$
gluinos/gluons	\tilde{g}	g	8 , 1 , 0
winos/ W -bosons	$\tilde{W}^\pm, \tilde{W}^0$	W^\pm, W^0	1 , 3 , 0
bino/ B -boson	\tilde{B}	B	1 , 1 , 0

trilinear terms appear in the soft-breaking Lagrangian

$$\begin{aligned}
-\mathcal{L}_{soft}^{MSSM} = & m_{H_u}^2 H_u^\dagger \cdot H_u + m_{H_d}^2 H_d^\dagger \cdot H_d + (B\mu H_u \cdot H_d + h.c.) \\
& + m_{\tilde{Q}}^2 \tilde{Q}_{Li}^\dagger \cdot \tilde{Q}_{Lj} + m_{\tilde{u}}^2 \tilde{u}_{Ri}^{c\dagger} \cdot \tilde{u}_{Rj}^c + m_{\tilde{d}}^2 \tilde{d}_{Ri}^{c\dagger} \cdot \tilde{d}_{Rj}^c \\
& + m_{\tilde{L}}^2 \tilde{L}_{Li}^\dagger \cdot \tilde{L}_{Lj} + m_{\tilde{e}}^2 \tilde{e}_{Ri}^{c\dagger} \cdot \tilde{e}_{Rj}^c \\
& + \left(-(A_u Y_u)_{ij} H_u \cdot \tilde{Q}_{Li} \tilde{u}_{Rj}^c + (A_d Y_d)_{ij} H_d \cdot \tilde{Q}_{Li} \tilde{d}_{Rj}^c \right. \\
& \left. + (A_e Y_e)_{ij} H_d \cdot \tilde{L}_{Li} \tilde{e}_{Rj}^c + h.c. \right) \\
& + \left(M_1 \tilde{B} \tilde{B} + M_2 \tilde{W}_a \tilde{W}_a + M_3 \tilde{g}_i \tilde{g}_i + h.c. \right)
\end{aligned} \tag{1.16}$$

The first line contains mass terms for the Higgs bosons, the second and third line for the sfermions. In the fourth and fifth line the trilinear couplings between the Higgs bosons and the sfermions appear. Finally, the last line gives rise to mass terms for the gauginos (gluinos, winos, bino).

Because of the soft-breaking terms, the MSSM contains more than 100 free parameters. Constraining the MSSM is thus a difficult task and usually in experimental particle physics, constrained versions of the MSSM or assumptions at the GUT scale are used to report the impact of searches on SUSY. In the following a short introduction of the phenomenological MSSM is given. With its reduced parameter space, it allows to elaborate on long-lived particles in the MSSM in a much easier way.

1.2.1.3 The phenomenological MSSM

The phenomenological MSSM (pMSSM) imposes constraints that are reasonable in the sense that the pMSSM fulfils current observations and still keeps the phenomenological variety of the MSSM [30]. The following assumptions are imposed (in [30] more detailed information about these assumptions can be found):

- No new sources of CP violation,
- No flavour changing neutral currents,
- First and second generation universality.

These assumption reduce the number of SUSY parameters to only 19. The remaining free parameters are the following:

- $\tan \beta$ (the ratio of the vacuum expectation values of the two Higgs doublets)
- M_A (the mass of the pseudo-scalar Higgs boson)
- μ (the Higgs mass parameter)

- M_1, M_2, M_3 (bino, wino and gluino mass parameters, respectively)
- $m_{\tilde{q}}, m_{\tilde{l}}, m_{\tilde{u}}, m_{\tilde{d}}$ and $m_{\tilde{e}}$ (the first and second generation mass parameters)
- $m_{\tilde{Q}}, m_{\tilde{L}}, m_{\tilde{t}}, m_{\tilde{b}}$ and $m_{\tilde{\tau}}$ (the third generation mass parameters)
- A_t, A_b and A_{τ} (third generation trilinear couplings).

1.2.2 Supersymmetry breaking

As already noted, the mechanism of supersymmetry breaking is unknown. There exist, however, several ideas how to spontaneously break supersymmetry. All mechanisms have in common that they need to happen at high energies in a hidden sector. “Messenger” particles are introduced which mediate the breaking to the TeV scale. This, however, implies that supersymmetry breaking is a question of extraordinary high energies and one can parametrise the breaking by the soft breaking terms introduced in Section 1.2.1.2.

The most popular breaking mediation mechanisms are gravity-mediated supersymmetry breaking [31] and gauge-mediated supersymmetry breaking [32].

1.3 Long-lived particles in the MSSM

There are various mechanisms how particles can be long-lived, such as small couplings or (almost) conserved quantum numbers. For a comprehensive review, the reader is referred to [33].

In this thesis, the focus is set on particles that have a long lifetime due to a small decay phase space. A phase space suppression is possible when the mass splitting between the decaying particle and one of the decay products is very small. In Part ??, a search for highly ionising, short tracks is presented. This search is motivated by long-lived charginos, that are nearly mass-degenerate with the lightest supersymmetric particle, the neutralino. The underlying mechanism of this mass-degeneracy in the MSSM will be addressed in the next paragraphs.

In the MSSM, the lightest chargino ($\tilde{\chi}_1^\pm$) and the lightest neutralino ($\tilde{\chi}_1^0$) can be almost mass-degenerate, if the wino mass parameter (M_2) is smaller than the bino (M_1) and higgsino (μ) mass parameters. This can be seen from the chargino and neutralino mass matrices. The chargino mass matrix in the basis $\Psi_i^+ = (-i\tilde{W}^+, \tilde{h}_u^+)$ and $\Psi_i^- = (-i\tilde{W}^-, \tilde{h}_d^-)$

is given by

$$\mathcal{M}_{\Psi^\pm} = \begin{pmatrix} M_2 & gv_d \\ gv_u & \mu \end{pmatrix}. \quad (1.17)$$

The mass eigenstates can be deduced with the help of orthogonal matrices V and U , $\chi_i^+ = V_{ij}\Psi_j^+$ and $\chi_i^- = U_{ij}\Psi_j^-$.

The neutralino mass matrix in the basis $\Psi_i^0 = (-i\tilde{B}, -i\tilde{W}^0, \tilde{h}_u^0, \tilde{h}_d^0)$ is

$$\mathcal{M}_{\Psi^0} = \begin{pmatrix} M_1 & 0 & \frac{g'v_u}{\sqrt{2}} & -\frac{g'v_d}{\sqrt{2}} \\ 0 & M_2 & -\frac{gv_u}{\sqrt{2}} & \frac{gv_d}{\sqrt{2}} \\ \frac{g'v_u}{\sqrt{2}} & -\frac{gv_u}{\sqrt{2}} & 0 & -\mu \\ -\frac{g'v_d}{\sqrt{2}} & \frac{gv_d}{\sqrt{2}} & -\mu & 0 \end{pmatrix}. \quad (1.18)$$

The mass matrix can be diagonalised with an orthogonal matrix N leading to four different mass eigenstates of $\tilde{\chi}_i^0 = N_{ij}\Psi_j^0$.

It can be easily seen from the mass matrices (1.17) and (1.18), that in first order approximation - neglecting the off-diagonal elements which are of electroweak strength - the lightest chargino and the lightest neutralino are both wino-like for $M_2 < M_1, \mu$ with a mass of $m_\chi \simeq M_2$. Thus, the mass difference between $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_1^0$ is only determined by higher order corrections: radiative corrections as well as tree-level mixing with other states.

Furthermore, recent analyses of the pMSSM parameter space [34,35] show, that models with almost pure wino-like neutralinos as LSPs mostly come along with wino-like charginos being the next-to lightest supersymmetric particle (NLSP). In [34], a parameter scan in the pMSSM parameter space is performed, flat in the 19 different SUSY parameters. Afterwards, the generated 3 million pMSSM models are confronted with theoretical constraints as well as experimental observations. Theoretical constraints are e.g. requiring stable vacua and no colour- or charge breaking minima. Furthermore, the agreement with precision electroweak data, heavy flavour physics and collider results from LEP, Tevatron and LHC is required. The accordance with relic density data is only implemented as an upper bound. Phenomenological MSSM models that survive these constraints and have a wino-like neutralino as lightest supersymmetric particle, do frequently contain a metastable chargino. In a fraction of $\sim 25\%$ of these models, the metastable chargino decays inside the tracker, calorimeter or muon chamber. The mass splitting between chargino and neutralino in these scenarios is typically of the order of ~ 160 MeV [34].

Furthermore, a study has been performed within [36] which interpretes the results of various beyond Standard Model searches in terms of the fraction of excluded parameter points in the pMSSM. This study shows, that lifetimes between $1\text{ cm} \lesssim c\tau \lesssim 30\text{ cm}$ could not yet been accessed by any of the existing searches (cf. Fig. ?? in Section ??).

1.3.1 Previous searches and constraints from indirect searches

Several previous searches are sensitive on SUSY scenarios with almost mass-degenerate wino-like charginos and neutralinos. In the following an overview about these previous searches will be given.

Searches at LEP

Several searches at LEP were hunting for almost mass-degenerate neutralino-chargino scenarios [37–40]. These searches were looking for events with a high-energetic initial state radiated photon leading to missing energy in events with chargino-pair production and invisible decay products. The excluded parameter regions by these searches can be found in [41] and are depicted in Fig. 1.2. The searches were interpreted for M_1 and M_2 almost degenerate and with a large unified scalar mass m_0 leading to sneutrino masses larger than 500 GeV. Charginos are excluded up to a mass of 92.4 GeV [41].

Searches at ATLAS at 7 and 8 TeV

At the ATLAS experiment at the LHC, searches for events with a disappearing track signature were performed at $\sqrt{s} = 7\text{ TeV}$ [42] as well as at $\sqrt{s} = 8\text{ TeV}$ [43]. Furthermore, a search for metastable particles with high ionisation losses was performed with $\sqrt{s} = 8\text{ TeV}$ data [44]. These searches were interpreted within an anomaly-mediated supersymmetry breaking model [45] with $\tan\beta = 5$ and $\mu > 0$. The excluded parameter space by these searches is shown in Fig. 1.3. Models with charginos down to lifetimes of 0.06 ns could be excluded.

Searches at CMS at 7 and 8 TeV

There are several searches at the CMS experiment at the LHC that are sensitive to long-lived wino-like charginos. Among them is the search for long-lived charged particles [46], which searched for heavy particles with large energy deposits in the tracker at $\sqrt{s} = 7\text{ TeV}$ and $\sqrt{s} = 8\text{ TeV}$. Furthermore, there is the search for disappearing tracks [36] which analysed events with disappearing tracks in the tracker with respect to wino-like charginos almost mass-degenerate with the lightest neutralino. This search was performed at the CMS experiment at a centre-of mass energy of $\sqrt{s} = 8\text{ TeV}$. Since the latter search is more

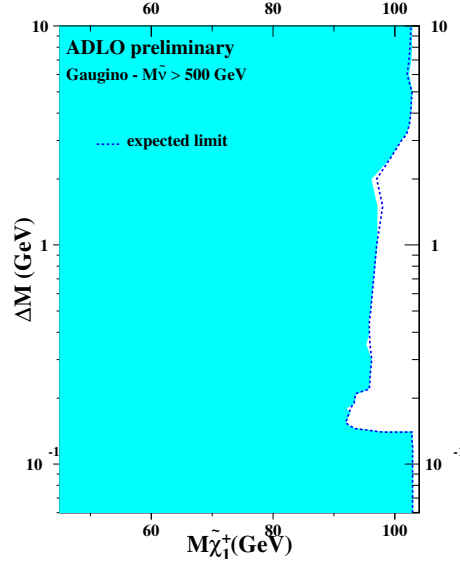


Figure 1.2: Observed and expected exclusion limits by LEP searches in the $m_{\tilde{\chi}_1^\pm} - \Delta m(\tilde{\chi}_1^\pm, \tilde{\chi}_1^0)$ plane for almost degenerate M_1 and M_2 and a large unified scalar mass m_0 . Taken from [41].

sensitive to shorter lifetime, only the exclusion limits derived by this search are shown in Fig. 1.4. The disappearing track search by CMS shows a very similar sensitivity as the searches done at the ATLAS experiment.

Indirect searches

Finally, also results from indirect dark matter searches constrain the parameter region of SUSY models with wino-like charginos and neutralinos. The most stringent limits are due to results by the Fermi Gamma-Ray Space Telescope (Fermi) [48] and the High Energy Spectroscopic System (H.E.S.S.) [49].

By the comparison of the observed gamma-ray signal to the theoretical prediction, Fermi sets upper limits on the dark matter annihilation cross-section considering six different decay channels [50].

H.E.S.S. sets upper limits on the DM annihilation cross section by the observation of the γ -ray line which is expected near the DM mass [51].

Recent interpretations of the Fermi and H.E.S.S. data [52–55] show that thermally produced wino-like neutralinos can only account for the full relic density for ~ 3.1 TeV [53], while DM masses between $1.6 - 3.0$ TeV are excluded by Fermi and H.E.S.S. observations. Lower masses are still allowed, however, the neutralino cannot make up the full relic

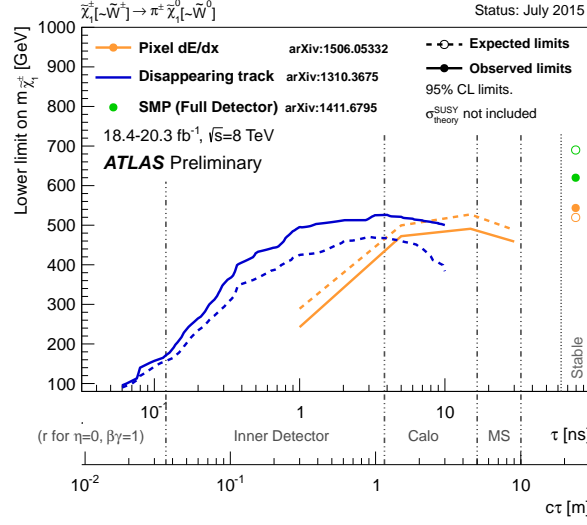


Figure 1.3: Excluded parameter space by ATLAS searches in the $m_{\tilde{\chi}_1^\pm} - \tau_{\tilde{\chi}_1^\pm}$ plane for an AMSB model with $\tan\beta = 5$ and $\mu > 0$. Only chargino pair production is taken into account. The area below the curves is excluded. Taken from [47].

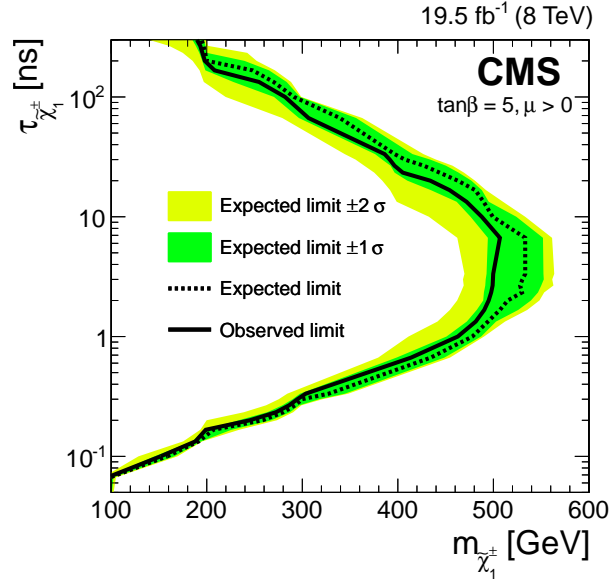


Figure 1.4: Excluded parameter space by the Disappearing track search of CMS in the $\tau_{\tilde{\chi}_1^\pm} - m_{\tilde{\chi}_1^\pm}$ plane for wino-like charginos. The region left to the curve is excluded. Taken from [36].

density.

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