Using Normalized Difference Vegetation Index to assess N status and predict grain yield in rice.

These are the packages needed for the analysis

```
## -- Attaching packages ------ tidyverse 1.2.1 --
## v tibble 2.0.1
                     v purrr
                             0.3.0
## v tidyr
          0.8.2
                     v dplyr
                              0.7.8
## v readr 1.3.1
                   v stringr 1.4.0
## v tibble 2.0.1
                    v forcats 0.3.0
## -- Conflicts ----- tidyverse conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                   masks stats::lag()
## For news about 'ggpmisc', please, see https://www.r4photobiology.info/
## For on-line documentation see https://docs.r4photobiology.info/ggpmisc/
##
## Attaching package: 'gridExtra'
## The following object is masked from 'package:dplyr':
##
##
      combine
##
## Attaching package: 'nlme'
## The following object is masked from 'package:dplyr':
##
##
      collapse
## Loading required package: carData
## Attaching package: 'car'
## The following object is masked from 'package:dplyr':
##
##
      recode
## The following object is masked from 'package:purrr':
##
##
      some
##
##
    This is piecewiseSEM version 2.0.2
##
##
    If you have used the package before, it is strongly recommended you read Section 3 of the vignette
##
    Questions or bugs can be addressed to <jlefcheck@bigelow.org>
## Loading required package: sp
## Attaching package: 'raster'
```

```
## The following object is masked from 'package:nlme':
##
## getData
## The following object is masked from 'package:dplyr':
##
## select
## The following object is masked from 'package:tidyr':
##
## extract
```

R Markdown

This is an R Markdown document. Markdown is a simple formatting syntax for authoring HTML, PDF, and MS Word documents. For more details on using R Markdown see http://rmarkdown.rstudio.com.

When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document. You can embed an R code chunk like this:

```
Sys.time()
## [1] "2019-03-21 13:45:11 PDT"
```

GREENSEEKER CONVERSION

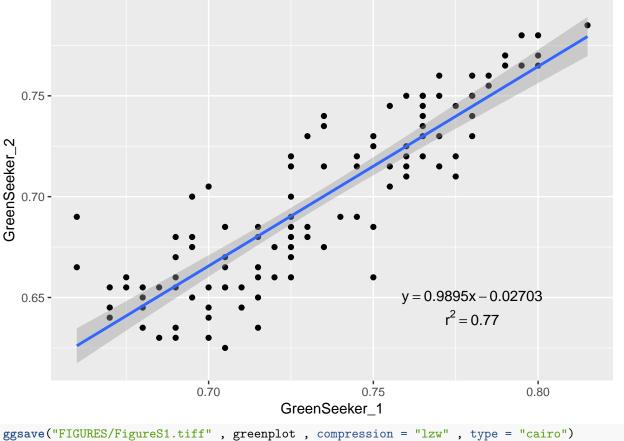
Getting the linear regression conversion from GreenSeeker 1 to GreenSeeker 2

From the paper – "two GreenSeekers were used to measure NDVI in this study (GreenSeeker 1 in 2015 and GreenSeeker 2 from 2016 to 2018). Consistent differences between the two devices were detected by plotting side by side NDVI measurements (n=105). Differences were normalized by adjusting NDVI values based on the resulting fitted linear regression equation (Fig. S1)."

Figure S1

```
GS_data <- read_csv(file = "DATA/greenseeker_comparison.csv")
## Parsed with column specification:
## cols(
##
     Greenseeker1_NDVI1 = col_double(),
     Greenseeker1_NDVI2 = col_double(),
##
     Greenseeker2 NDVI1 = col double(),
##
     Greenseeker2_NDVI2 = col_double()
##
## )
str(GS_data)
## Classes 'spec_tbl_df', 'tbl_df', 'tbl' and 'data.frame': 105 obs. of 4 variables:
   $ Greenseeker1_NDVI1: num 0.69 0.71 0.72 0.75 0.78 0.77 0.69 0.7 0.7 0.68 ...
   $ Greenseeker1_NDVI2: num 0.71 0.72 0.73 0.78 0.78 0.79 0.72 0.71 0.7 0.68 ...
  $ Greenseeker2_NDVI1: num 0.64 0.69 0.69 0.72 0.75 0.74 0.68 0.68 0.65 0.64 ...
  $ Greenseeker2 NDVI2: num 0.65 0.68 0.69 0.72 0.75 0.72 0.65 0.66 0.66 0.65 ...
## - attr(*, "spec")=
```

```
##
     .. cols(
##
          Greenseeker1_NDVI1 = col_double(),
##
          Greenseeker1 NDVI2 = col double(),
         Greenseeker2_NDVI1 = col_double(),
##
##
          Greenseeker2_NDVI2 = col_double()
##
     ..)
GS_data <- GS_data %>%
 rowwise() %>%
  mutate(GreenSeeker_1 = mean(c(Greenseeker1_NDVI1 , Greenseeker1_NDVI2)),
         GreenSeeker_2 = mean(c(Greenseeker2_NDVI1 , Greenseeker2_NDVI2))) #takes the mean of GreenSeek
greenmod1 <- lm(GreenSeeker_2 ~ GreenSeeker_1 , data = GS_data) #creates a linear regression of GreenSe
summary(greenmod1) #the resulting equation is GreenSeeker_2 = -0.02703 + 0.98950 * GreenSeeker_1
##
## Call:
## lm(formula = GreenSeeker_2 ~ GreenSeeker_1, data = GS_data)
##
## Residuals:
##
         Min
                    1Q
                          Median
                                        3Q
                                                 Max
## -0.055099 -0.015309 0.000426 0.014429 0.063957
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -0.02703
                             0.03936 -0.687
                                                0.494
## GreenSeeker 1 0.98950
                             0.05368 18.434
                                               <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.0209 on 103 degrees of freedom
## Multiple R-squared: 0.7674, Adjusted R-squared: 0.7651
## F-statistic: 339.8 on 1 and 103 DF, p-value: < 2.2e-16
label_eqn <- paste("y == 0.9895 * x - 0.02703")
label_r2 \leftarrow paste("r^2 == 0.77")
greenplot <- ggplot(data = GS_data, aes(x = GreenSeeker_1 , y = GreenSeeker_2 )) +</pre>
  geom_point(mapping = aes(GreenSeeker_1, GreenSeeker_2) , data = GS_data) +
  geom_smooth( data = GS_data , aes(x = GreenSeeker_1 , y = GreenSeeker_2 ) , method = lm, formula = y
  annotate("text" , x = 0.78 , y = 0.65 , label = label_eqn , parse = TRUE) +
  annotate("text" , x = 0.78 , y = 0.64 , label = label_r2 , parse = TRUE ) \#generates\ a\ plot\ of\ the\ da
greenplot
```



Saving 6.5×4.5 in image

DATA

The following chunk processes the PI NDVI data into a single data frame with only the relevant columns. The N trial data is processed seperately from the Farm Survey data and then merged into a single data frame.

N Trial NDVI Data

```
ntrial_data <- read_csv(file = "DATA/N_trial_data.csv")</pre>
## Warning: Missing column names filled in: 'X16' [16], 'X17' [17],
## 'X18' [18], 'X19' [19], 'X20' [20], 'X21' [21], 'X22' [22], 'X23' [23],
## 'X24' [24]
## Parsed with column specification:
## cols(
##
     .default = col_double(),
##
     site_year = col_character(),
    NDVI_1 = col_character(),
##
    NDVI 2 = col character(),
##
    NDVI_3 = col_character(),
##
    NDVI_4 = col_character(),
##
```

```
##
     X16 = col_logical(),
##
    X17 = col_logical(),
##
    X18 = col_logical(),
##
    X19 = col_logical(),
##
    X20 = col_logical(),
##
    X21 = col logical(),
    X22 = col_logical(),
     X23 = col_logical(),
##
##
    X24 = col_logical()
## )
## See spec(...) for full column specifications.
ntrial_data <- ntrial_data[c(1:231), c(1:15)] #removes the empty rows and columns from the data frame
ntrial_data$block <- factor(ntrial_data$block)</pre>
ntrial_data$plot <- factor(ntrial_data$plot)</pre>
ntrial_data$plot_id <- factor(ntrial_data$plot_id)</pre>
ntrial_data$N_level <- factor(ntrial_data$N_level)</pre>
ntrial_data$exp_plot_number <- factor(ntrial_data$exp_plot_number)</pre>
ntrial_data$site_year <- factor(ntrial_data$site_year , levels = c("Arbuckle-15" , "RES-15" , "RES-16"
ntrial_data$NDVI_1 <- as.numeric(as.character(ntrial_data$NDVI_1))</pre>
## Warning: NAs introduced by coercion
ntrial_data$NDVI_2 <- as.numeric(as.character(ntrial_data$NDVI_2))</pre>
## Warning: NAs introduced by coercion
ntrial data$NDVI 3 <- as.numeric(as.character(ntrial data$NDVI 3))</pre>
## Warning: NAs introduced by coercion
ntrial_data$NDVI_4 <- as.numeric(as.character(ntrial_data$NDVI_4)) #gets the data right
## Warning: NAs introduced by coercion
str(ntrial_data)
## Classes 'tbl_df', 'tbl' and 'data.frame':
                                                 231 obs. of 15 variables:
                        : Factor w/ 10 levels "Arbuckle-15",...: 1 1 1 1 1 1 1 1 1 1 ...
## $ site_year
                        : Factor w/ 28 levels "101", "102", "103", ...: 1 2 3 4 5 8 9 10 11 12 ...
## $ exp_plot_number
## $ block
                        : Factor w/ 40 levels "1", "2", "3", "4", ...: 1 1 1 1 1 2 2 2 2 2 ....
                        : Factor w/ 7 levels "1", "2", "3", "4", ...: 1 2 3 4 5 1 2 3 4 5 ...
## $ plot
## $ plot_id
                        : Factor w/ 231 levels "1","2","3","4",..: 1 2 3 4 5 6 7 8 9 10 ...
## $ N level
                        : Factor w/ 12 levels "0","45","75",...: 6 11 1 3 8 1 8 6 11 3 ...
## $ biomass_plus_bag_g: num 414 472 281 386 455 304 402 322 418 336 ...
## $ paper_bag_g
                       : num 45 45 45 45 45 45 45 45 45 ...
## $ num of paper bags : num 1 1 1 1 1 1 1 1 1 1 ...
## $ sample_weight_mg : num 4.84 5.12 4.78 5.15 4.93 ...
## $ sample_N_ug
                        : num 117.1 153.4 64.9 92.9 116 ...
                        : num 0.77 \ 0.82 \ 0.56 \ 0.72 \ 0.79 \ 0.7 \ 0.81 \ 0.82 \ 0.82 \ 0.73 \ \dots
## $ NDVI_1
## $ NDVI_2
                        : num NA NA NA NA NA NA NA NA NA ...
## $ NDVI_3
                        : num NA NA NA NA NA NA NA NA NA ...
## $ NDVI_4
                        : num NA NA NA NA NA NA NA NA NA ...
ntrial_data <- ntrial_data %>%
  mutate( biomass_dry_wt = biomass_plus_bag_g - (paper_bag_g * num_of_paper_bags) ,
          aboveground_biomass = (biomass_dry_wt / 0.50) / 1000 , #ring size 0.5 m~2
```

```
n_content = sample_N_ug / sample_weight_mg ,
          N_Uptake = aboveground_biomass * n_content) #processes the data
ntrial_data <- ntrial_data %>%
  rowwise() %>%
  mutate(NDVI = mean(c( NDVI_1 , NDVI_2 , NDVI_3 , NDVI_4) , na.rm = T)) #takes average of four NDVI re
ntrial data <- ntrial data %>%
  mutate(NDVI = case_when(site_year == "Arbuckle-15" ~ -0.02703 + 0.98950*NDVI,
                           site_year == "RES-15" \sim -0.02703 + 0.98950*NDVI,
                           site_year == "RES-16" ~ NDVI,
                           site_year == "Davis-16" ~ NDVI,
                           site_year == "Nicolaus-17" ~ NDVI,
                           site_year == "Williams-17" ~ NDVI,
                           site_year == "Nicolaus-18" ~ NDVI,
                           site_year == "Arbuckle-18" ~ NDVI,
                           site_year == "Marysville-18" ~ NDVI,
                           site_year == "Biggs-18" ~ NDVI)) #normailizes the data for the two greenseeke
ntrial_data <- dplyr::select(ntrial_data ,</pre>
                      site_year,
                    exp_plot_number,
                    block,
                    plot,
                    N level,
                    aboveground_biomass,
                    n_content,
                    N_Uptake,
                    NDVI) #selects the relevant columns
ntrial_data$site_year <- factor(ntrial_data$site_year , levels = c("Arbuckle-15" , "RES-15" , "Davis-16")</pre>
```

Farm Survey NDVI Data

```
farmsurvey_data <- read_csv(file = "DATA/farm_survey_data.csv")</pre>
## Warning: Missing column names filled in: 'X16' [16], 'X17' [17],
## 'X18' [18], 'X19' [19], 'X20' [20], 'X21' [21]
## Parsed with column specification:
## cols(
##
     .default = col_double(),
     site_year = col_character(),
##
##
    exp_plot_number = col_character(),
##
    plot = col_character(),
    NDVI_2 = col_character(),
    NDVI_3 = col_character(),
##
##
    NDVI_4 = col_character(),
##
    X16 = col logical(),
    X17 = col_logical(),
##
##
    X18 = col_logical(),
##
    X19 = col_logical(),
##
    X20 = col_logical(),
```

```
X21 = col_logical()
## )
## See spec(...) for full column specifications.
farmsurvey_data <- farmsurvey_data[c(1:58), c(1:15)] #removes the extra rows and columns from the data
farmsurvey_data$block <- factor(farmsurvey_data$block)</pre>
farmsurvey_data$plot <- factor(farmsurvey_data$plot)</pre>
farmsurvey_data$plot_id <- factor(farmsurvey_data$plot_id)</pre>
farmsurvey_data$N_level <- factor(farmsurvey_data$N_level)</pre>
farmsurvey_data$exp_plot_number <- factor(farmsurvey_data$exp_plot_number)</pre>
farmsurvey_data$site_year <- factor(farmsurvey_data$site_year)</pre>
farmsurvey_data$NDVI_1 <- as.numeric(as.character(farmsurvey_data$NDVI_1))</pre>
farmsurvey_data$NDVI_2 <- as.numeric(as.character(farmsurvey_data$NDVI_2))</pre>
## Warning: NAs introduced by coercion
farmsurvey data$NDVI 3 <- as.numeric(as.character(farmsurvey data$NDVI 3))</pre>
## Warning: NAs introduced by coercion
farmsurvey_data$NDVI_4 <- as.numeric(as.character(farmsurvey_data$NDVI_4)) #gets the data right
## Warning: NAs introduced by coercion
str(farmsurvey_data)
## Classes 'tbl_df', 'tbl' and 'data.frame':
                                                58 obs. of 15 variables:
                       : Factor w/ 1 level "Farm Survey-15": 1 1 1 1 1 1 1 1 1 1 ...
## $ site_year
## $ exp_plot_number : Factor w/ 29 levels "001","002","003",..: 1 1 2 2 3 3 4 4 5 5 ...
## $ block
               : Factor w/ 1 level "25": 1 1 1 1 1 1 1 1 1 ...
                       : Factor w/ 2 levels "a", "b": 1 2 1 2 1 2 1 2 1 2 ...
## $ plot
## $ plot_id
                       : Factor w/ 58 levels "1","2","3","4",..: 1 2 3 4 5 6 7 8 9 10 ...
## $ N_level
                      : Factor w/ 1 level "175": 1 1 1 1 1 1 1 1 1 ...
## $ biomass_plus_bag_g: num 275 318 379 374 334 349 350 359 328 346 ...
## $ paper_bag_g
                     : num 45 45 45 45 45 45 45 45 45 ...
## $ num_of_paper_bags : num 1 1 1 1 1 1 1 1 1 1 ...
## $ sample_weight_mg : num 4.9 5.19 4.69 4.95 4.67 ...
## $ sample_N_ug
                       : num 136 140 120 119 149 ...
## $ NDVI_1
                       : num 0.82 0.76 0.84 0.84 0.85 0.86 0.84 0.84 0.85 0.85 ...
                       : num NA NA NA NA NA NA NA NA NA ...
## $ NDVI 2
## $ NDVI_3
                       : num NA NA NA NA NA NA NA NA NA ...
## $ NDVI 4
                        : num NA NA NA NA NA NA NA NA NA ...
farmsurvey_data <- farmsurvey_data %>%
  filter(plot == "a" | plot == "b") %>%
  group_by(exp_plot_number) %>%
  summarize(biomass_plus_bag_g = mean(biomass_plus_bag_g) , sample_weight_mg = mean(sample_weight_mg) ,
farmsurvey_data <- farmsurvey_data %>%
  mutate(site_year = factor("Farm Survey-15") , block = factor("41") , plot = factor("ab") , plot_id = :
farmsurvey_data <- dplyr::select(farmsurvey_data,</pre>
                                 site_year ,
                                 exp_plot_number ,
                                 block ,
                                 plot ,
```

```
N_{level} ,
                                  biomass_plus_bag_g ,
                                  paper_bag_g ,
                                 num_of_paper_bags ,
                                  sample_weight_mg ,
                                  sample_N_ug ,
                                 NDVI_1 ,
                                 NDVI_2 ,
                                 NDVI_3 ,
                                  NDVI_4) #makes df identical to n_trial_data
farmsurvey_data <- farmsurvey_data %>%
  mutate( biomass_dry_wt = biomass_plus_bag_g - (paper_bag_g * num_of_paper_bags) ,
          aboveground_biomass = (biomass_dry_wt / 0.50) / 1000 , #ring size 0.50 m~2
          n_content = sample_N_ug / sample_weight_mg ,
          N_Uptake = aboveground_biomass * n_content) #processes the data
farmsurvey_data <- farmsurvey_data %>%
 rowwise() %>%
 mutate(NDVI = mean(c( NDVI_1 , NDVI_2 , NDVI_3 , NDVI_4) , na.rm = T)) #mean NDVI
farmsurvey_data <-farmsurvey_data[1:28 , ] #removes outlier</pre>
farmsurvey_data <- farmsurvey_data %>%
  mutate(NDVI = -0.02703 + 0.98950*NDVI) #adjusts NDVI readings using eqn from above
farmsurvey_data <- dplyr::select(farmsurvey_data ,</pre>
                      site_year,
                    exp_plot_number,
                    block,
                    plot,
                    N_level,
                    aboveground_biomass,
                    n_content,
                    N_Uptake,
                    NDVI) #selects relevant columns
```

NDVI Data

```
ndvi_data <- bind_rows(list(ntrial_data, farmsurvey_data)) #binds both df

## Warning in bind_rows_(x, .id): Unequal factor levels: coercing to character

## Warning in bind_rows_(x, .id): binding character and factor vector,

## warning in bind_rows_(x, .id): binding character and factor vector,

## coercing into character vector

## Warning in bind_rows_(x, .id): Unequal factor levels: coercing to character

## Warning in bind_rows_(x, .id): binding character and factor vector,

## coercing into character vector</pre>
```

```
## Warning in bind_rows_(x, .id): binding character and factor vector,
## coercing into character vector
## Warning in bind_rows_(x, .id): Unequal factor levels: coercing to character
## Warning in bind_rows_(x, .id): binding character and factor vector,
## coercing into character vector
## Warning in bind_rows_(x, .id): binding character and factor vector,
## coercing into character vector
## Warning in bind_rows_(x, .id): Unequal factor levels: coercing to character
## Warning in bind_rows_(x, .id): binding character and factor vector,
## coercing into character vector
## Warning in bind_rows_(x, .id): binding character and factor vector,
## coercing into character vector
## Warning in bind_rows_(x, .id): Unequal factor levels: coercing to character
## Warning in bind_rows_(x, .id): binding character and factor vector,
## coercing into character vector
## Warning in bind_rows_(x, .id): binding character and factor vector,
## coercing into character vector
ndvi_data <- tibble::rowid_to_column(ndvi_data, "plot_id")</pre>
ndvi_data <- dplyr::select (ndvi_data,</pre>
                            site_year,
                            exp_plot_number,
                            block,
                            plot,
                            plot_id,
                            N_level,
                            aboveground_biomass,
                            n_content,
                            N_Uptake,
                            NDVI)
ndvi_data$block <- factor(ndvi_data$block) #changes block to a factor
ndvi_data$plot <- factor(ndvi_data$plot) #changes plot to a factor</pre>
ndvi_data$plot_id <- factor(ndvi_data$plot_id)</pre>
ndvi_data$N_level <- factor(ndvi_data$N_level)</pre>
ndvi_data$exp_plot_number <- factor(ndvi_data$exp_plot_number)</pre>
ndvi_data$site_year <- factor(ndvi_data$site_year , levels = c("Arbuckle-15" , "Farm Survey-15" , "RES-
```

Table 3

```
summary(subset(ndvi_data, site_year == "Arbuckle-15")) #this subsets the ndvi data just by Arbuckle-15
##
            site_year exp_plot_number
                                          block
                                                      plot
                                                                plot_id
## Arbuckle-15 :20
                      101
                             : 1
                                             :5
                                      1
                                                 1
                                                        :4
                                                                    : 1
                                                             1
## Farm Survey-15: 0
                       102
                             : 1
                                      2
                                             :5
                                                 2
                                                        :4
                                                             2
                                                                    : 1
## RES-15
                                             :5
                : 0
                      103
                             : 1
                                      3
                                                 3
                                                        :4
                                                             3
                                                                    : 1
```

```
## Davis-16
                 : 0
                        104
                               : 1
                                        4
                                               :5
                                                           :4
                               : 1
                                                           :4
                                                                       : 1
##
   RES-16
                  : 0
                        105
                                        10
                                               :0
                                                    5
                                                                5
##
   Nicolaus-17
                  : 0
                        201
                               : 1
                                        11
                                               :0
                                                           :0
                                                                6
                  : 0
                        (Other):14
##
    (Other)
                                        (Other):0
                                                    (Other):0
                                                                (Other):14
##
      N level aboveground biomass
                                      n content
                                                       N Uptake
##
   0
           :4
               Min.
                       :0.3400
                                    Min. :13.58
                                                    Min. : 4.885
   125
           :4
               1st Qu.:0.5600
                                    1st Qu.:17.98
                                                    1st Qu.:10.546
                                    Median :21.38
   175
               Median :0.6610
                                                    Median :13.280
##
           :4
##
   225
           :4
               Mean
                      :0.6334
                                    Mean :21.44
                                                    Mean :14.144
##
   75
           :4
              3rd Qu.:0.7335
                                    3rd Qu.:24.41
                                                    3rd Qu.:18.209
   120
         :0
              Max. :0.8540
                                    Max. :30.52
                                                    Max. :25.577
    (Other):0
##
        NDVI
##
##
         :0.4875
   Min.
##
   1st Qu.:0.6854
##
   Median :0.7398
##
   Mean
         :0.7057
   3rd Qu.:0.7670
##
##
  Max. :0.7844
##
summary(subset(ndvi_data, site_year == "RES-15"))
##
             site_year
                        exp_plot_number
                                            block
                                                         plot
                                                                   plot_id
  RES-15
                 :20
                        101
                              : 1
                                        5
                                               :5
                                                           :4
                                                                21
                                                                       : 1
                                                    1
   Arbuckle-15
                 : 0
                        102
                               : 1
                                                    2
##
                                        6
                                               :5
                                                           :4
                                                                22
                                                                       : 1
                                                           :4
##
  Farm Survey-15: 0
                        103
                               : 1
                                        7
                                               :5
                                                    3
                                                                23
                                                                       : 1
## Davis-16
                 : 0
                        104
                               : 1
                                        8
                                               :5
                                                    4
                                                           :4
                                                                24
                                                                       : 1
##
  RES-16
                  : 0
                        105
                               : 1
                                                                       : 1
                                        1
                                               :0
                                                    5
                                                           :4
                                                                25
##
   Nicolaus-17
                 : 0
                        201
                               : 1
                                        10
                                               :0
                                                           :0
                                                                26
                 : 0
##
    (Other)
                        (Other):14
                                                                (Other):14
                                        (Other):0
                                                    (Other):0
##
      N_level aboveground_biomass
                                      n_{content}
                                                       N_Uptake
                                    Min. :11.86
##
               Min. :0.3520
                                                    Min. : 4.174
   0
           :4
##
   125
           :4
               1st Qu.:0.4615
                                    1st Qu.:17.90
                                                    1st Qu.: 8.592
           :4
              Median :0.5120
                                    Median :23.55
                                                    Median :12.658
##
   175
   225
           :4 Mean :0.5084
                                    Mean :23.84
                                                    Mean :12.647
##
   75
           :4 3rd Qu.:0.5770
                                    3rd Qu.:30.78
                                                    3rd Qu.:18.156
##
   120
          :0
              Max.
                       :0.6540
                                    Max.
                                          :37.30
                                                           :23.051
                                                    Max.
##
    (Other):0
##
        NDVI
   Min.
          :0.5271
##
   1st Qu.:0.6928
##
##
  Median :0.7745
         :0.7339
##
  Mean
   3rd Qu.:0.7943
##
##
   Max. :0.8042
##
summary(subset(ndvi_data, site_year == "Farm Survey-15"))
##
             site_year exp_plot_number
                                            block
                                                          plot
## Farm Survey-15:28
                        001
                               : 1
                                        41
                                               :28
                                                            :28
                                                     ab
## Arbuckle-15
                : 0
                        002
                               : 1
                                        1
                                               : 0
                                                     1
                                                            : 0
## RES-15
                        003
                 : 0
                               : 1
                                        10
                                               : 0
                                                     2
                                                            : 0
## Davis-16
                 : 0
                        004
                               : 1
                                                     3
                                                            : 0
                                        11
                                               : 0
```

```
## RES-16
                 : 0
                      005
                             : 1
                                     12
                                            : 0 4
##
   Nicolaus-17
                : 0
                      006
                             : 1
                                      13
                                            : 0 5
                                                         : 0
                                      (Other): 0
##
    (Other)
                 : 0
                       (Other):22
                                                 (Other): 0
                            aboveground_biomass n_content
##
      plot_id
                 N_level
##
   232 : 1
                175
                      :28
                            Min. :0.1260
                                             Min. :10.91
##
   233
         : 1
                0
                       : 0
                            1st Qu.:0.4577
                                                1st Qu.:16.84
   234
        : 1
                120
                       : 0
                            Median: 0.5120
                                               Median :21.81
   235
                      : 0
                                               Mean :21.93
##
         : 1
                125
                            Mean :0.5090
                                             3rd Qu.:26.49
##
   236
          : 1
                150
                      : 0
                            3rd Qu.:0.6085
##
   237
                180
                     : 0
                            Max. :0.7260
                                              Max. :33.62
         : 1
   (Other):22 (Other): 0
      N Uptake
                        NDVI
##
##
  Min. : 1.375
                   Min. :0.1758
                   1st Qu.:0.5357
##
   1st Qu.: 8.189
  Median :11.280
                   Median :0.7200
## Mean :11.488
                    Mean :0.6458
##
   3rd Qu.:15.058
                    3rd Qu.:0.7819
## Max. :19.636
                    Max. :0.8190
summary(subset(ndvi_data, site_year == "Davis-16"))
                                                                plot_id
            site_year exp_plot_number
                                          block
                                                      plot
## Davis-16
                :20
                      101
                             : 1
                                             :5
                                                             61
                                                                   : 1
                                      13
                                                  1
                                                        :4
## Arbuckle-15 : 0
                      102
                             : 1
                                      14
                                             :5
                                                  2
                                                         :4
                                                             62
                                                                    : 1
## Farm Survey-15: 0
                       103
                             : 1
                                      15
                                             :5
                                                             63
                                                                    : 1
                                                  3
                                                        :4
## RES-15
                : 0
                      104
                             : 1
                                      16
                                             :5
                                                  4
                                                        :4
                                                             64
                                                                    : 1
## RES-16
                 : 0
                      105
                             : 1
                                      1
                                             :0
                                                  5
                                                        :4
                                                             65
                                                                    : 1
##
  Nicolaus-17
               : 0
                       201
                             : 1
                                      10
                                            :0
                                                        :0
                                                             66
                                                                    : 1
                                                  6
                : 0
                                      (Other):0
##
   (Other)
                       (Other):14
                                                  (Other):0
                                                             (Other):14
##
      N_level aboveground_biomass n_content
                                                    N_Uptake
          :4 Min. :0.1332
                                                  Min. : 2.030
##
   0
                                  Min. :14.61
##
          :4 1st Qu.:0.2258
                                  1st Qu.:17.42
                                                  1st Qu.: 4.016
  125
          :4 Median :0.2792
##
   175
                                  Median :20.62
                                                  Median: 5.919
         :4 Mean :0.2609
:4 3rd Qu.:0.3001
:0 Max. :0.3714
   225
        :4 Mean
                                  Mean :21.52
                                                  Mean : 5.888
##
##
   75
                                  3rd Qu.:25.21
                                                  3rd Qu.: 7.968
   120
                                  Max. :31.73
##
        :0
                                                  Max. :11.467
##
   (Other):0
##
        NDVI
##
         :0.5567
  Min.
  1st Qu.:0.6458
##
  Median :0.6667
  Mean :0.6665
##
   3rd Qu.:0.6917
##
## Max. :0.7233
##
summary(subset(ndvi_data, site_year == "RES-16"))
                                                                plot_id
            site_year exp_plot_number
                                          block
                                                      plot
                             : 1
                                                                    : 1
## RES-16
                 :20
                      101
                                      10
                                             :5
                                                  1
                                                        :4
                                                             41
## Arbuckle-15
                : 0
                       102
                              : 1
                                      11
                                             :5
                                                  2
                                                        :4
                                                             42
                                                                    : 1
## Farm Survey-15: 0
                       103
                                      12
                                             :5
                                                             43
                                                                    : 1
                             : 1
                                                  3
                                                        :4
                                             :5
## RES-15
                : 0
                       104
                             : 1
                                                  4
                                                        :4
                                                             44
                                                                    : 1
## Davis-16
                 : 0
                                                                    : 1
                       105
                             : 1
                                      1
                                             :0
                                                 5
                                                        :4
                                                             45
```

```
Nicolaus-17 : 0 201 : 1
                                   13 :0
                                                 6 :0
                                                             46 : 1
##
   (Other)
                : 0
                      (Other):14
                                     (Other):0
                                                  (Other):0
                                                             (Other):14
##
      N level aboveground biomass
                                  n content
                                                    N Uptake
               Min. :0.1466
                                  Min. :18.48
                                                 Min. : 3.086
##
   0
          :4
##
   125
          :4
               1st Qu.:0.3016
                                  1st Qu.:22.26
                                                 1st Qu.: 6.294
##
   175
          :4
              Median :0.3578
                                  Median :28.51
                                                 Median :11.187
   225
          :4
             Mean :0.3428
                                  Mean :28.58
                                                 Mean :10.324
##
   75
          :4 3rd Qu.:0.4108
                                  3rd Qu.:33.50
                                                 3rd Qu.:13.442
##
   120
         :0
             Max. :0.4960
                                  Max. :38.83
                                                 Max. :19.260
##
   (Other):0
##
        NDVI
   Min. :0.3567
##
   1st Qu.:0.6167
##
  Median :0.6850
## Mean :0.6382
## 3rd Qu.:0.7233
## Max. :0.7467
##
summary(subset(ndvi_data, site_year == "Nicolaus-17"))
##
            site_year exp_plot_number
                                          block
                                                      plot
                                                                plot_id
## Nicolaus-17
                :28
                      101
                             : 1
                                      22
                                             :8
                                                 1
                                                        :4
                                                             109
## Arbuckle-15
                : 0
                       102
                             : 1
                                      23
                                             :7
                                                 2
                                                             110
                                                        :4
## Farm Survey-15: 0
                       103
                             : 1
                                      24
                                             :7
                                                 3
                                                        :4
                                                             111
                                                                    : 1
## RES-15
                : 0
                       104
                                      21
                             : 1
                                             :6
                                                 4
                                                        :4
                                                             112
                                                                    : 1
## Davis-16
                 : 0
                       105
                             : 1
                                      1
                                             :0
                                                 5
                                                        :4
                                                             113
                                                                    : 1
  RES-16
##
                : 0
                       106
                             : 1
                                      10
                                            :0
                                                        :4
                                                             114
##
   (Other)
                : 0
                      (Other):22
                                     (Other):0
                                                  (Other):4
                                                             (Other):22
##
      N level aboveground biomass
                                  n content
                                                    N Uptake
          :4
                                                 Min. : 6.171
##
              Min. :0.3970
                                  Min. :15.54
   0
              1st Qu.:0.4785
                                  1st Qu.:21.14
##
  125
          :4
                                                 1st Qu.:10.062
  175
          :4 Median :0.5412
                                  Median :25.22
                                                 Median :13.893
##
##
   225
        :4 Mean :0.5559
                                  Mean :25.73
                                                 Mean :14.766
##
   275
        :4 3rd Qu.:0.6301
                                  3rd Qu.:31.24
                                                 3rd Qu.:19.986
##
   45
         :4 Max. :0.7426
                                  Max. :36.12
                                                 Max. :24.021
   (Other):4
##
##
        NDVI
##
        :0.4933
  Min.
  1st Qu.:0.6417
## Median :0.6850
## Mean :0.6842
## 3rd Qu.:0.7733
## Max. :0.8000
##
summary(subset(ndvi data, site year == "Williams-17"))
                                                                plot_id
##
            site_year exp_plot_number
                                          block
                                                      plot
## Williams-17 :28
                      101
                             : 1
                                      17
                                             :7
                                                 1
                                                        :4
                                                             81
                                                                    : 1
## Arbuckle-15 : 0
                             : 1
                                                 2
                                                                    : 1
                       102
                                      18
                                             :7
                                                        :4
                                                             82
## Farm Survey-15: 0
                       103
                             : 1
                                      19
                                             :7
                                                 3
                                                        :4
                                                             83
                                                                    : 1
## RES-15
                                      20
                : 0
                       104
                             : 1
                                             :7
                                                 4
                                                        :4
                                                             84
                                                                    : 1
## Davis-16
                                                             85
                 : 0
                       105
                             : 1
                                      1
                                             :0
                                                 5
                                                        :4
                                                                    : 1
## RES-16
                 : 0
                       106
                             : 1
                                             :0
                                                        :4
                                                             86
                                      10
                                                 6
                                                                    : 1
```

```
(Other):22
##
    (Other)
                  : 0 (Other):22
                                        (Other):0
                                                     (Other):4
                                      n_content
##
       N level
               aboveground_biomass
                                                       N_Uptake
                                    Min. :12.34
##
   0
           :4
                Min.
                       :0.2740
                                                    Min. : 3.381
                                    1st Qu.:16.59
                                                    1st Qu.: 9.050
##
   125
           :4
                1st Qu.:0.5010
##
   175
           :4
               Median :0.5512
                                    Median :22.70
                                                    Median :11.876
##
   225
           :4
               Mean
                       :0.5471
                                    Mean
                                          :22.06
                                                    Mean
                                                          :12.459
   275
           :4
               3rd Qu.:0.6156
                                    3rd Qu.:27.58
                                                    3rd Qu.:16.687
   45
                       :0.7270
                                    Max. :30.61
                                                    Max. :19.430
##
           :4
               Max.
##
    (Other):4
##
        NDVI
##
   Min.
           :0.3567
   1st Qu.:0.6733
##
   Median : 0.7650
##
   Mean
         :0.7058
##
   3rd Qu.:0.7967
## Max.
         :0.8233
##
summary(subset(ndvi_data, site_year == "Arbuckle-18"))
                                                                    plot_id
             site_year exp_plot_number
                                            block
                                                         plot
                               : 1
##
   Arbuckle-18
                 :24
                        101
                                        29
                                               :6
                                                    1
                                                            :4
                                                                 161
                                                                        : 1
                 : 0
##
   Arbuckle-15
                        102
                               : 1
                                        30
                                               :6
                                                    2
                                                            :4
                                                                 162
                                                                        : 1
## Farm Survey-15: 0
                        103
                               : 1
                                        31
                                               :6
                                                    3
                                                            :4
                                                                 163
  RES-15
                 : 0
                        104
                               : 1
                                        32
                                               :6
                                                    4
                                                            :4
                                                                 164
                                                                        : 1
##
  Davis-16
                  : 0
                        105
                                                                 165
                               : 1
                                        1
                                               :0
                                                    5
                                                            :4
                                                                        : 1
                  : 0
##
   RES-16
                        106
                               : 1
                                        10
                                               :0
                                                    6
                                                            :4
                                                                 166
                                                                        : 1
##
    (Other)
                  : 0
                        (Other):18
                                        (Other):0
                                                     (Other):0
                                                                 (Other):18
##
       N_level aboveground_biomass
                                    n content
                                                       N_Uptake
##
   0
           :4
               Min.
                       :0.0730
                                    Min. :12.12
                                                    Min. : 0.9657
   120
           :4
                1st Qu.:0.3015
                                    1st Qu.:18.10
                                                    1st Qu.: 5.0762
##
##
   150
           :4
              Median :0.3402
                                    Median :21.45
                                                    Median: 7.5737
   180
              Mean
                      :0.3397
                                    Mean :21.43
                                                    Mean : 7.6532
##
           :4
##
   210
           :4
              3rd Qu.:0.4258
                                    3rd Qu.:25.88
                                                    3rd Qu.:10.4248
          :4
                                    Max. :30.22
##
   90
               Max. :0.8006
                                                    Max. :16.0598
##
    (Other):0
         NDVI
##
          :0.1467
##
   Min.
##
   1st Qu.:0.6062
   Median :0.6800
  Mean :0.6070
##
##
   3rd Qu.:0.7244
##
  Max. :0.7525
##
summary(subset(ndvi_data, site_year == "Biggs-18"))
             site_year exp_plot_number
                                                                    plot_id
##
                                                         plot
                                            block
##
                                                            :4
                                                                        : 1
  Biggs-18
                 :23
                        102
                               : 1
                                        37
                                               :6
                                                                 209
                                                    1
  Arbuckle-15 : 0
                                        39
                        103
                               : 1
                                               :6
                                                    2
                                                            :4
                                                                 210
                                                                        : 1
## Farm Survey-15: 0
                        104
                               : 1
                                        40
                                               :6
                                                    3
                                                            :4
                                                                 211
                                                                        : 1
## RES-15
                  : 0
                        105
                               : 1
                                        38
                                               :5
                                                    4
                                                            :4
                                                                 212
                                                                        : 1
## Davis-16
                  : 0
                        106
                                                :0
                                                    5
                                                            :4
                                                                 213
                                                                        : 1
                               : 1
                                        1
                  : 0
## RES-16
                        201
                               : 1
                                        10
                                               :0
                                                    6
                                                            :3
                                                                 214
                                                                        : 1
## (Other)
                  : 0
                        (Other):17
                                        (Other):0
                                                                 (Other):17
                                                     (Other):0
```

```
##
       N level
               aboveground biomass
                                       n content
                                                          N Uptake
                                                      Min. : 2.037
##
    0
           :4
                Min.
                        :0.1962
                                     Min.
                                            :10.38
                1st Qu.:0.4857
                                      1st Qu.:17.76
##
    120
           :4
                                                      1st Qu.:10.175
    150
                Median :0.5422
                                     Median :23.39
                                                      Median :12.570
##
           :4
##
    180
           :4
                Mean
                        :0.5019
                                     Mean
                                            :21.48
                                                      Mean
                                                             :11.359
##
    210
           :4
                3rd Qu.:0.5859
                                     3rd Qu.:25.58
                                                      3rd Qu.:14.422
    90
           :3
                Max.
                        :0.6812
                                     Max.
                                             :32.94
                                                      Max.
                                                             :19.341
    (Other):0
##
##
         NDVI
##
           :0.3625
   Min.
   1st Qu.:0.7037
   Median :0.7475
##
   Mean
           :0.6931
##
##
   3rd Qu.:0.7712
## Max.
           :0.7925
##
summary(subset(ndvi_data, site_year == "Marysville-18"))
##
             site_year exp_plot_number
                                              block
                                                            plot
                                                                      plot_id
   Marysville-18:24
                         101
                                : 1
                                          33
                                                 :6
                                                              :4
                                                                   185
                                                                          : 1
                                                      1
## Arbuckle-15 : 0
                         102
                                : 1
                                          34
                                                 :6
                                                      2
                                                              :4
                                                                   186
                                                                           : 1
##
   Farm Survey-15: 0
                         103
                                : 1
                                          35
                                                 :6
                                                      3
                                                              :4
                                                                   187
                                                                           : 1
##
   RES-15
                  : 0
                         104
                                          36
                                                 :6
                                                      4
                                                              :4
                                                                   188
                                : 1
   Davis-16
                  : 0
                         105
                                : 1
                                          1
                                                 :0
                                                      5
                                                              :4
                                                                   189
                                                                           : 1
    RES-16
                  : 0
                         106
                                : 1
                                                                   190
##
                                          10
                                                 :0
                                                      6
                                                              :4
                                                                           : 1
##
    (Other)
                  : 0
                         (Other):18
                                          (Other):0
                                                       (Other):0
                                                                   (Other):18
##
       N level aboveground biomass
                                       n content
                                                          N Uptake
##
   0
           :4
                Min.
                        :0.2384
                                     Min.
                                            :16.05
                                                      Min. : 3.826
                                      1st Qu.:29.29
##
    120
           :4
                1st Qu.:0.4505
                                                      1st Qu.:13.828
    150
           :4
                Median :0.4864
                                     Median :32.14
                                                      Median :15.784
##
   180
                                     Mean :29.88
##
           :4
                Mean :0.4604
                                                      Mean :14.202
                3rd Qu.:0.5079
##
    210
                                     3rd Qu.:33.75
                                                      3rd Qu.:16.954
           :4
##
    90
           :4
                Max.
                        :0.5472
                                     Max.
                                             :36.99
                                                      Max.
                                                             :20.240
    (Other):0
##
##
         NDVI
##
           :0.4500
    Min.
    1st Qu.:0.6669
##
##
   Median : 0.6950
   Mean
          :0.6619
    3rd Qu.:0.7206
##
           :0.7500
##
   Max.
##
summary(subset(ndvi_data, site_year == "Nicolaus-18"))
##
                         exp_plot_number
                                                                      plot_id
             site_year
                                                            plot
                                              block
   Nicolaus-18
                  :24
                         101
                                : 1
##
                                          25
                                                 :6
                                                      1
                                                              :4
                                                                   137
                  : 0
   Arbuckle-15
                         102
                                          26
                                                      2
                                                              :4
                                : 1
                                                 :6
                                                                   138
                                                                           : 1
   Farm Survey-15: 0
                         103
                                : 1
                                          27
                                                 :6
                                                      3
                                                              :4
                                                                   139
                                                                           : 1
   RES-15
##
                  : 0
                         104
                                : 1
                                          28
                                                 :6
                                                      4
                                                              :4
                                                                   140
                                                                           : 1
##
   Davis-16
                   : 0
                         105
                                : 1
                                          1
                                                 :0
                                                      5
                                                              :4
                                                                   141
                                                                           : 1
##
   RES-16
                   : 0
                         106
                                          10
                                                 :0
                                                              :4
                                                                   142
                                                                           : 1
                                 : 1
##
   (Other)
                  : 0
                         (Other):18
                                          (Other):0
                                                       (Other):0
                                                                   (Other):18
##
       N_level aboveground_biomass
                                       n_{content
                                                          N_Uptake
```

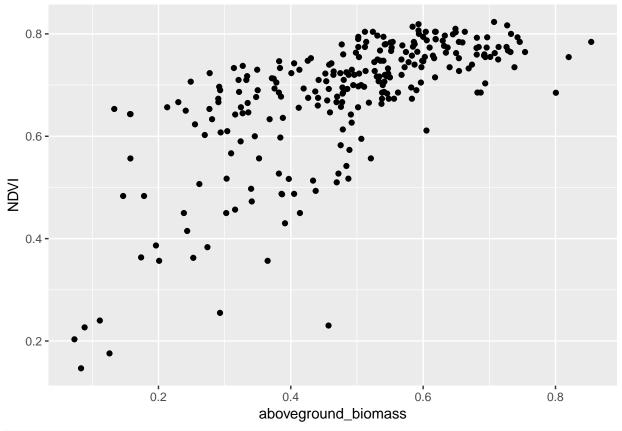
```
##
            :4
                 Min.
                         :0.3242
                                      Min.
                                              :13.07
                                                        Min.
                                                                : 4.603
            :4
##
    120
                 1st Qu.:0.5630
                                       1st Qu.:20.85
                                                        1st Qu.:11.428
##
    150
            :4
                 Median : 0.6332
                                      Median :23.96
                                                        Median :15.108
    180
                                              :23.32
##
            :4
                 Mean
                         :0.6069
                                      Mean
                                                                :14.603
                                                        Mean
##
    210
            :4
                 3rd Qu.:0.6835
                                       3rd Qu.:27.21
                                                        3rd Qu.:18.685
##
    90
            :4
                         :0.7282
                                      Max.
                                              :30.69
                                                                :22.352
                 Max.
                                                        Max.
##
    (Other):0
         NDVI
##
##
    Min.
            :0.5825
##
    1st Qu.:0.7125
    Median :0.7375
##
    Mean
            :0.7170
    3rd Qu.:0.7575
##
##
    Max.
            :0.7725
##
```

summary(ndvi_data)

```
##
                           exp_plot_number
                                                 block
                                                                 plot
              site_year
##
    Farm Survey-15: 28
                           102
                                   : 10
                                            41
                                                    : 28
                                                                    :40
                                                            1
    Nicolaus-17
                                                            2
##
                   : 28
                           103
                                   : 10
                                            22
                                                       8
                                                                    :40
    Williams-17
                   : 28
                                                       7
##
                           104
                                   : 10
                                            17
                                                            3
                                                                    :40
                   : 24
##
    Arbuckle-18
                           105
                                   : 10
                                            18
                                                       7
                                                            4
                                                                    :40
##
    Marysville-18: 24
                           201
                                   : 10
                                            19
                                                       7
                                                            5
                                                                    :40
    Nicolaus-18
                                            20
##
                   : 24
                           202
                                   : 10
                                                       7
                                                            ab
                                                                   :28
    (Other)
                   :103
                           (Other):199
##
                                            (Other):195
                                                            (Other):31
                                                         n_content
##
       plot_id
                      N level
                                  aboveground_biomass
##
    1
                   175
                           :52
                                 Min.
                                         :0.0730
                                                       Min.
                                                               :10.38
##
    2
                   0
                           :40
                                 1st Qu.:0.3820
                                                       1st Qu.:18.55
               1
##
    3
               1
                   125
                           :24
                                 Median :0.5018
                                                       Median :23.54
##
    4
               1
                   225
                           :24
                                 Mean
                                         :0.4840
                                                       Mean
                                                               :23.73
    5
                                                       3rd Qu.:28.51
##
                   75
                           :24
                                  3rd Qu.:0.5930
##
    6
                   120
                                         :0.8540
                                                       Max.
                                                               :38.83
             1
                           :16
                                 Max.
##
    (Other):253
                   (Other):79
                             NDVI
##
       N_Uptake
           : 0.9657
                               :0.1467
    Min.
                       Min.
    1st Qu.: 7.4993
                       1st Qu.:0.6533
##
    Median :11.6888
                       Median :0.7133
##
##
    Mean
           :11.8929
                       Mean
                               :0.6776
    3rd Qu.:16.0854
                       3rd Qu.:0.7612
##
    Max.
            :25.5772
                       Max.
                               :0.8233
##
```

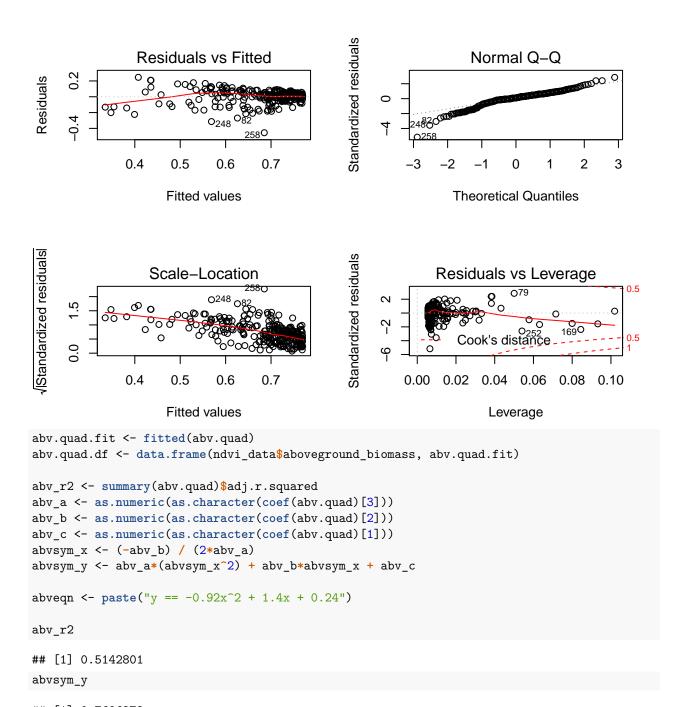
MODELS

Aboveground Biomass



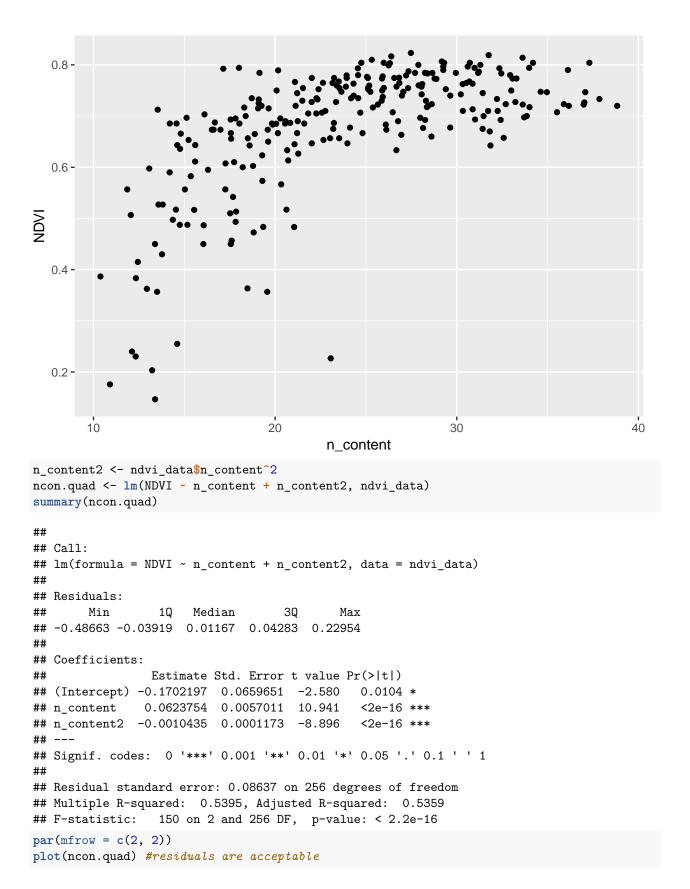
```
aboveground_biomass2 <- ndvi_data$aboveground_biomass^2
abv.quad <- lm(NDVI ~ aboveground_biomass + aboveground_biomass2 , ndvi_data)
summary(abv.quad)
```

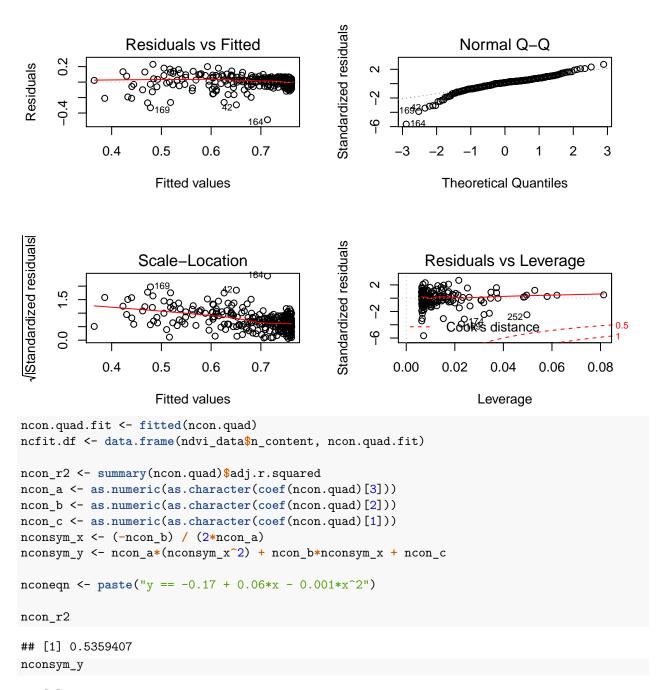
```
##
## Call:
## lm(formula = NDVI ~ aboveground_biomass + aboveground_biomass2,
##
       data = ndvi_data)
##
## Residuals:
                 1Q
                      Median
                                    3Q
##
  -0.45491 -0.03436  0.00818  0.05326  0.24556
##
## Coefficients:
##
                       Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        0.23756
                                   0.03769
                                              6.303 1.27e-09 ***
## aboveground_biomass
                        1.40068
                                    0.16878
                                              8.299 6.08e-15 ***
## aboveground_biomass2 -0.92184
                                    0.18122 -5.087 7.04e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.08836 on 256 degrees of freedom
## Multiple R-squared: 0.518, Adjusted R-squared: 0.5143
## F-statistic: 137.6 on 2 and 256 DF, p-value: < 2.2e-16
par(mfrow = c(2, 2))
plot(abv.quad) #residuals are acceptable
```



[1] 0.7696272

N Concentration

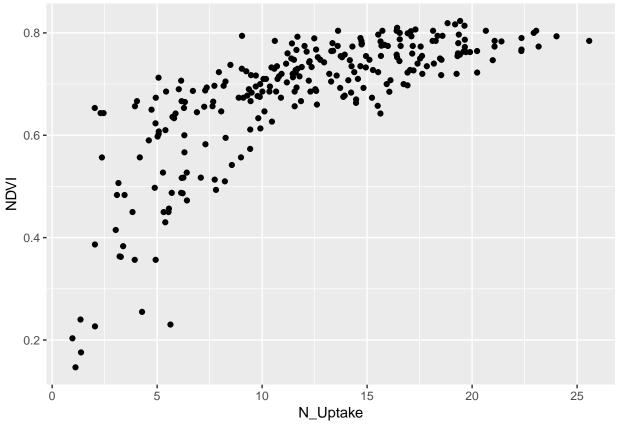




[1] 0.7618864

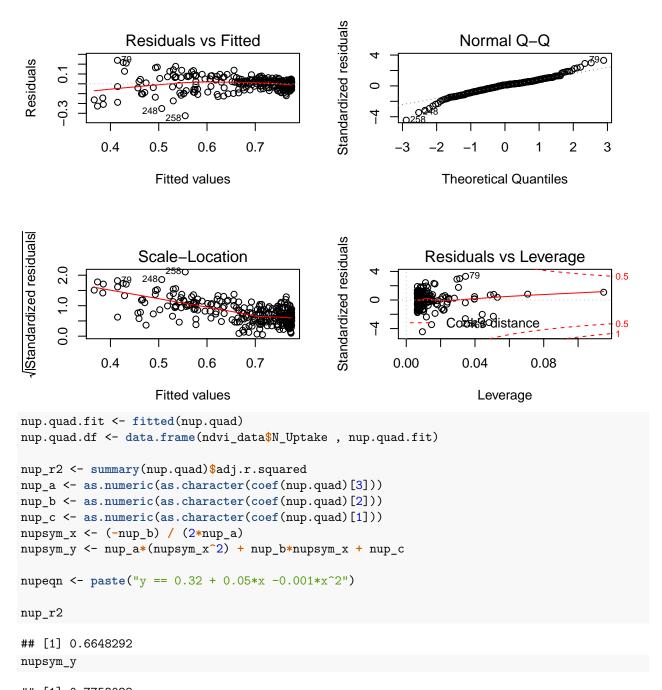
N Uptake

```
ggplot(data = ndvi_data , aes(x = N_Uptake , y = NDVI)) +
geom_point(mapping = aes(N_Uptake , NDVI), data = ndvi_data) #visualizes the data
```



```
N_Uptake2 <- ndvi_data$N_Uptake^2
nup.quad <- lm(NDVI ~ N_Uptake + N_Uptake2 , ndvi_data)
summary(nup.quad)</pre>
```

```
##
## Call:
## lm(formula = NDVI ~ N_Uptake + N_Uptake2, data = ndvi_data)
##
## Residuals:
##
        Min
                  1Q
                      Median
                                    ЗQ
                                             Max
## -0.32464 -0.03989 0.00853 0.03927 0.23885
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.3202576 0.0194828 16.438
                                                <2e-16 ***
## N_Uptake
               0.0491128 0.0034762 14.128
                                                <2e-16 ***
               -0.0013252 0.0001403 -9.444
## N_Uptake2
                                                <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
\ensuremath{\mbox{\#\#}} Residual standard error: 0.0734 on 256 degrees of freedom
## Multiple R-squared: 0.6674, Adjusted R-squared: 0.6648
## F-statistic: 256.9 on 2 and 256 DF, p-value: < 2.2e-16
par(mfrow = c(2, 2))
plot(nup.quad) #residuals are acceptable
```



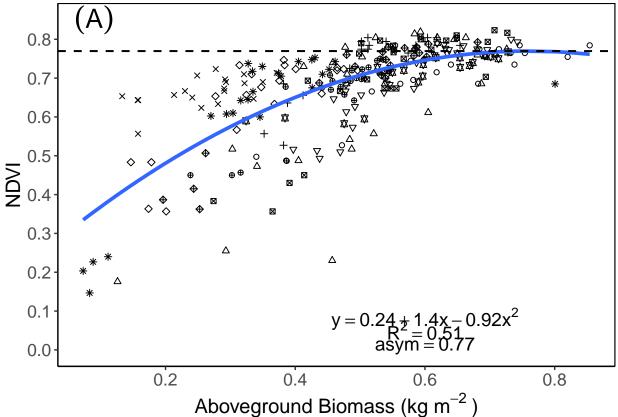
[1] 0.7753028

PLOTS

Aboveground Biomass Plot

```
a <- ggplot( data = ndvi_data , aes ( x = aboveground_biomass , y = NDVI)) +
  geom_point(mapping = aes(aboveground_biomass , NDVI, shape = factor(site_year)) , data = ndvi_data )
  theme_classic() +
  labs( x = "Aboveground Biomass (kg m"^-2~")" , y = "NDVI" , shape = "Site Year" ) +</pre>
```

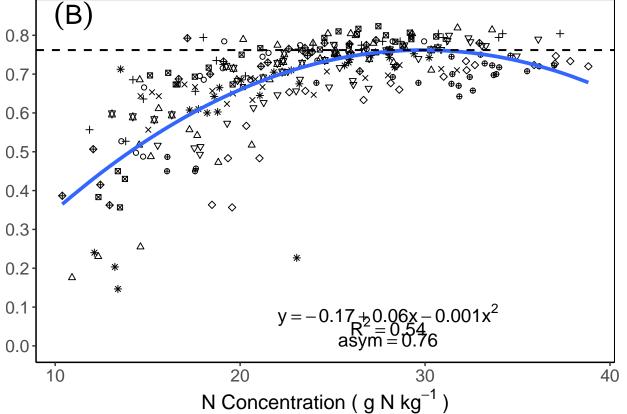
```
theme(legend.position = "none") +
theme(axis.title = element_text(size = 15)) +
theme(axis.text = element_text(size = 13)) +
theme(legend.text = element_text(size = 11)) +
theme(legend.title = element_text(size = 11)) +
scale_shape_manual(values = seq(0:10)) +
coord_cartesian(ylim=c(0,0.85)) +
scale_y\_continuous(breaks = c(0, 0.10, 0.20, 0.30, 0.40, 0.50, 0.60, 0.70, 0.80)) +
scale_x_continuous(breaks = c(0, .2, .4, .6, .8, 1, 1.2, 1.4)) +
theme(panel.background = element_rect(fill = "white", color = "grey0")) +
geom_line(data = abv.quad.df, aes( x = ndvi_data$aboveground_biomass , y = abv.quad.fit), size = 1.3
geom_hline( yintercept = abvsym_y , size = 0.7 , color = "black" , lty = 2) +
annotate("text" , x = .09, y = 0.85, label = "(A)", color="black", size = 7, parse = TRUE) +
annotate("text", x = .60, y = 0.08, label = "y == 0.24 + 1.4*x - 0.92*x^2", size = 5, parse = TRUE
annotate("text" , x = .60 , y = 0.05 , label = "R^2 == 0.51" , size = 5, parse = TRUE) +
annotate("text", x = .60, y = 0.01, label = "asym == 0.77", size = 5, parse = TRUE)
```



N Concentration Plot

```
b <- ggplot( data = ndvi_data , aes ( x = n_content , y = NDVI)) +
geom_point(mapping = aes(n_content , NDVI , shape = site_year) , data = ndvi_data ) +
theme_classic() +</pre>
```

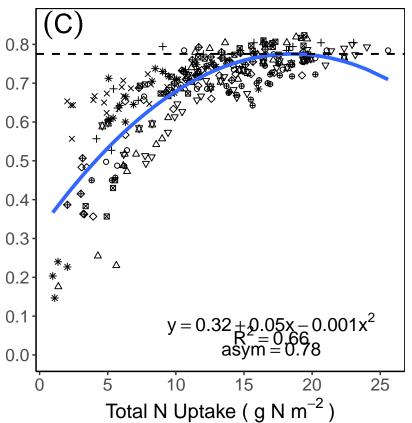
```
labs( x = "N Concentration ( g N kg"^-1~")", y = NULL, shape = "Site Year" ) +
  theme(legend.position = "none") +
  theme(axis.title = element_text(size = 15)) +
  theme(axis.text = element_text(size = 13)) +
  theme(legend.text = element_text(size = 11)) +
  theme(legend.title = element_text(size = 11)) +
  scale_shape_manual(values = seq(0:10)) +
  coord cartesian(ylim=c(0,0.85)) +
  scale_y = continuous(breaks = c(0, 0.10, 0.20, 0.30, 0.40, 0.50, 0.60, 0.70, 0.80)) +
  scale_x_continuous(breaks = c(0, 10, 20, 30, 40, 50)) +
  theme(panel.background = element_rect(fill = "white", color = "grey0")) +
  geom_line(data = ncfit.df, aes( x = ndvi_data$n_content , y = ncon.quad.fit), size = 1.3 , color = "#
 geom_hline( yintercept = nconsym_y , size = 0.7 , color = "black" , lty = 2) +
annotate("text", x = 11, y = 0.85, label = "(B)", color="black", size = 7, parse = TRUE) +
  annotate("text", x = 28, y = 0.08, label = nconeqn, size = 5, parse = TRUE) +
  annotate("text", x = 28, y = 0.05, label = "R^2 == 0.54", size = 5, parse = TRUE) +
  annotate("text", x = 28, y = 0.01, label = "asym == 0.76", size = 5, parse = TRUE)
b
```



N Uptake Plot

```
c <- ggplot( data = ndvi_data , aes ( x = N_Uptake , y = NDVI)) +
geom_point(mapping = aes(N_Uptake , NDVI, shape = site_year) , data = ndvi_data ) +
theme_classic() +</pre>
```

```
labs(x = "Total N Uptake (g N m"^-2~")", y = NULL, shape = "Site Year") +
  theme(axis.title = element_text(size = 15)) +
  theme(axis.text = element_text(size = 13)) +
  theme(legend.text = element_text(size = 15)) +
  theme(legend.title = element_text(size = 15)) +
  scale_shape_manual(values = seq(0:10)) +
  coord_cartesian(ylim=c(0,0.85)) +
  scale_y\_continuous(breaks = c(0, 0.10, 0.20, 0.30, 0.40, 0.50, 0.60, 0.70, 0.80)) +
  scale_x_continuous(breaks = c(0, 5, 10, 15, 20, 25, 30)) +
  theme(panel.background = element_rect(fill = "white", color = "grey0")) +
  geom_line(data = nup.quad.df , aes( x = ndvi_data$N_Uptake , y = nup.quad.fit), size = 1.3 , color =
  geom_hline( yintercept = nupsym_y , size = 0.7 , color = "black" , lty = 2) +
  annotate("text", x = 1.75, y = 0.85, label = "(C)", color="black", size = 7, parse = TRUE) +
  annotate("text" , x = 17 , y = 0.08 , label = nupeqn , size = 5 , parse = TRUE) +
  annotate("text" , x = 17 , y = 0.05 , label = "R^2 == 0.66" , size = 5 , parse = TRUE) +
  annotate("text", x = 17, y = 0.01, label = "asym == 0.78", size = 5, parse = TRUE)
С
```



Site Year

- Arbuckle–15
- △ Farm Survey–15
- + RES-15
- × Davis-16
- ♦ RES-16
- ¬ Nicolaus–17
- Williams–17
- * Arbuckle–18
- Biggs-18
- Marysville–18

```
g_legend <- function(c){
  tmp <- ggplot_gtable(ggplot_build(c))
  leg <- which(sapply(tmp$grobs, function(x) x$name) == "guide-box")
  legend <- tmp$grobs[[leg]]
  return(legend)}
legend <- g_legend(c) #extract the legend from plot c</pre>
```

```
theme(legend.position = "none")
c
```

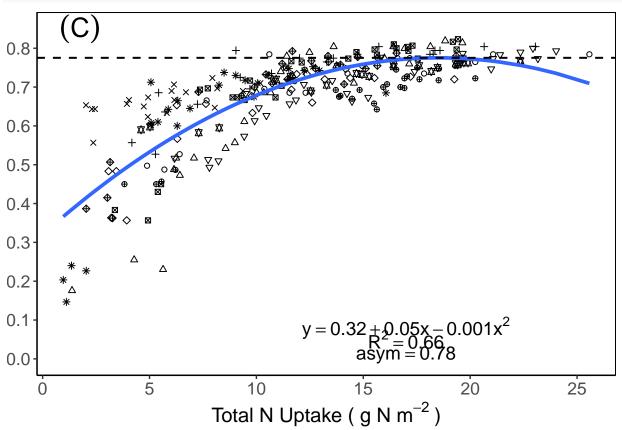
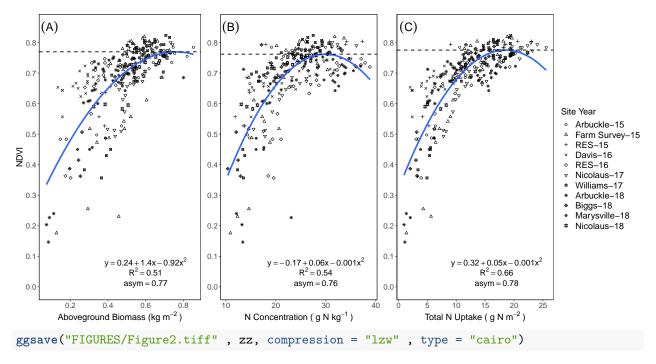


Figure 2



Saving 15 x 7.5 in image

YIELD DATA

Dataframe

the code below processes the yield data into a single dataframe with the relevant columns. The N Uptake and NDVI data is extracted from the NDVI dataframe. Overall, the steps are pretty obvious. I guess the only thing would be worthy of noting is that "A's" clean grain weight data had already subtracted the paper bag weight, while my data included this value. Thus, tare 2 only subtracts the paper bag weight from my data.

```
yield_data <- read_csv(file = "DATA/yield_data.csv" )</pre>
## Parsed with column specification:
##
     site_year = col_character(),
##
     exp_plot_number = col_double(),
##
     block = col_double(),
     plot = col_double(),
##
     plot_id = col_double(),
##
     N_level = col_double(),
##
##
     tare1 = col_double(),
##
     fw1_plus_tare1 = col_double(),
##
     fw2_plus_tare1 = col_double(),
##
     ss_fw_plus_tare1 = col_double(),
##
     clean_grain_odw_plus_tare2 = col_double(),
##
     tare2 = col_double(),
##
     yc_clean_grain_odw_plus_tare_3 = col_double(),
##
     tare_3 = col_double()
```

```
## )
yield_data$exp_plot_number <- factor(yield_data$exp_plot_number)</pre>
yield_data$block <- factor(yield_data$block)</pre>
yield_data$plot <- factor(yield_data$plot)</pre>
yield_data$plot_id <- factor(yield_data$plot_id)</pre>
yield_data$N_level <- factor(yield_data$N_level)</pre>
yield_data\site_year <- factor(yield_data\site_year , levels = c("Arbuckle-15" , "RES-15" , "RES-16" ,
str(yield data)
## Classes 'spec_tbl_df', 'tbl_df', 'tbl' and 'data.frame': 231 obs. of 14 variables:
## $ site_year
                                 : Factor w/ 10 levels "Arbuckle-15",..: 1 1 1 1 1 1 1 1 1 1 ...
## $ exp_plot_number
                                 : Factor w/ 28 levels "101", "102", "103", ...: 1 2 3 4 5 8 9 10 11 12
## $ block
                                 : Factor w/ 40 levels "1", "2", "3", "4", ...: 1 1 1 1 1 2 2 2 2 2 ...
## $ plot
                                 : Factor w/ 7 levels "1", "2", "3", "4", ...: 1 2 3 4 5 1 2 3 4 5 ...
                                 : Factor w/ 231 levels "1","2","3","4",..: 1 2 3 4 5 6 7 8 9 10 ...
## $ plot_id
                                 : Factor w/ 12 levels "0","45","75",..: 6 11 1 3 8 1 8 6 11 3 ...
## $ N level
## $ tare1
                                 : num 1224 1224 1224 1224 1224 ...
                                 : num 5352 5418 4086 5512 5714 ...
## $ fw1_plus_tare1
## $ fw2_plus_tare1
                                 : num 1224 1224 1224 1224 1224 ...
                                 : num 1880 2170 1792 2180 2192 ...
## $ ss_fw_plus_tare1
## $ clean_grain_odw_plus_tare2
                                 : num 178 243 132 266 255 ...
## $ tare2
                                 : num 0000000000...
## $ tare_3
                                  ## - attr(*, "spec")=
##
    .. cols(
##
         site year = col character(),
##
       exp_plot_number = col_double(),
##
       block = col_double(),
    . .
##
    .. plot = col_double(),
##
    .. plot_id = col_double(),
##
       N_level = col_double(),
##
       tare1 = col_double(),
    . .
##
    .. fw1_plus_tare1 = col_double(),
##
    .. fw2_plus_tare1 = col_double(),
##
       ss_fw_plus_tare1 = col_double(),
##
    .. clean_grain_odw_plus_tare2 = col_double(),
##
    .. tare2 = col_double(),
    .. yc_clean_grain_odw_plus_tare_3 = col_double(),
##
         tare_3 = col_double()
yield_data$fw1_minus_tare1 <- yield_data$fw1_plus_tare1 - yield_data$tare1
yield_data$fw2_minus_tare1 <- yield_data$fw2_plus_tare1 - yield_data$tare1
yield_data$fw_net <- yield_data$fw1_minus_tare1 + yield_data$fw2_minus_tare1
yield_data$ss_fw_net <- yield_data$ss_fw_plus_tare1 - yield_data$tare1
yield_data$ratio <- yield_data$ss_fw_net / yield_data$fw_net</pre>
yield_data$clean_grain_1 <- yield_data$clean_grain_odw_plus_tare2 - yield_data$tare2</pre>
```

```
yield_data$clean_grain_2 <- yield_data$yc_clean_grain_odw_plus_tare_3 - yield_data$tare_3
yield_data$clean_grain_2 <- yield_data$clean_grain_2 * yield_data$ratio #this essntially subsamples the</pre>
yield_data$clean_grain_m2 <- (yield_data$clean_grain_1 + yield_data$clean_grain_2) / yield_data$ratio
yield_data$grain_yield <- yield_data$clean_grain_m2 * 10</pre>
yield_data$grain_yield <- yield_data$grain_yield*(98.1/86) #this corrects the grain yield values to 14%
head(yield_data)
## # A tibble: 6 x 23
     site_year exp_plot_number block plot plot_id N_level tare1
                               <fct> <fct> <fct>
                                                    <fct>
               <fct>
                                                             <dbl>
## 1 Arbuckle~ 101
                               1
                                      1
                                            1
                                                    125
                                                             1224
## 2 Arbuckle~ 102
                               1
                                      2
                                            2
                                                    225
                                                             1224
## 3 Arbuckle~ 103
                                      3
                                            3
                                                             1224
                               1
                                                    75
## 4 Arbuckle~ 104
                                            4
                                                             1224
                               1
## 5 Arbuckle~ 105
                                            5
                                                             1224
                                                    175
## 6 Arbuckle~ 201
                               2
                                      1
                                            6
                                                    0
                                                             1224
## # ... with 16 more variables: fw1_plus_tare1 <dbl>, fw2_plus_tare1 <dbl>,
       ss_fw_plus_tare1 <dbl>, clean_grain_odw_plus_tare2 <dbl>, tare2 <dbl>,
       yc_clean_grain_odw_plus_tare_3 <dbl>, tare_3 <dbl>,
## #
       fw1_minus_tare1 <dbl>, fw2_minus_tare1 <dbl>, fw_net <dbl>,
       ss_fw_net <dbl>, ratio <dbl>, clean_grain_1 <dbl>,
       clean_grain_2 <dbl>, clean_grain_m2 <dbl>, grain_yield <dbl>
tail(yield data)
## # A tibble: 6 x 23
     site_year exp_plot_number block plot plot_id N_level tare1
                               <fct> <fct> <fct>
##
                                                    <fct>
                                                            <dbl>
     <fct>
               <fct>
                                                             1098
## 1 Biggs-18 401
                               40
                                      1
                                            226
                                                    90
## 2 Biggs-18
               402
                                      2
                                            227
                                                    210
                                                             1098
                               40
## 3 Biggs-18 403
                               40
                                      3
                                            228
                                                    0
                                                             1098
                                            229
                                                             1098
## 4 Biggs-18
               404
                               40
                                      4
                                                    180
## 5 Biggs-18
               405
                               40
                                      5
                                            230
                                                    150
                                                             1098
                                                    120
## 6 Biggs-18
               406
                               40
                                      6
                                            231
                                                             1098
## # ... with 16 more variables: fw1_plus_tare1 <dbl>, fw2_plus_tare1 <dbl>,
## # ss fw plus tare1 <dbl>, clean grain odw plus tare2 <dbl>, tare2 <dbl>,
       yc_clean_grain_odw_plus_tare_3 <dbl>, tare_3 <dbl>,
       fw1_minus_tare1 <dbl>, fw2_minus_tare1 <dbl>, fw_net <dbl>,
       ss_fw_net <dbl>, ratio <dbl>, clean_grain_1 <dbl>,
       clean_grain_2 <dbl>, clean_grain_m2 <dbl>, grain_yield <dbl>
str(yield_data)
## Classes 'spec_tbl_df', 'tbl_df', 'tbl' and 'data.frame': 231 obs. of 23 variables:
## $ site_year
                                     : Factor w/ 10 levels "Arbuckle-15",..: 1 1 1 1 1 1 1 1 1 1 ...
## $ exp plot number
                                     : Factor w/ 28 levels "101", "102", "103", ...: 1 2 3 4 5 8 9 10 11 12
                                     : Factor w/ 40 levels "1","2","3","4",..: 1 1 1 1 1 2 2 2 2 2 ...
## $ block
## $ plot
                                     : Factor w/ 7 levels "1", "2", "3", "4", ...: 1 2 3 4 5 1 2 3 4 5 ...
                                     : Factor w/ 231 levels "1","2","3","4",..: 1 2 3 4 5 6 7 8 9 10 ...
## $ plot_id
```

: Factor w/ 12 levels "0","45","75",...: 6 11 1 3 8 1 8 6 11 3 ...

\$ N_level

```
## $ tare1
                               : num 1224 1224 1224 1224 1224 ...
## $ fw1_plus_tare1
                               : num 5352 5418 4086 5512 5714 ...
## $ fw2 plus tare1
                               : num 1224 1224 1224 1224 1224 ...
                               : num 1880 2170 1792 2180 2192 ...
## $ ss_fw_plus_tare1
## $ clean_grain_odw_plus_tare2 : num 178 243 132 266 255 ...
## $ tare2
                               : num 0000000000...
## $ tare_3
                               : num 4128 4194 2862 4288 4490 ...
## $ fw1_minus_tare1
## $ fw2_minus_tare1
                               : num 0000000000...
## $ fw_net
                               : num 4128 4194 2862 4288 4490 ...
                               : num 656 946 568 956 968 ...
## $ ss_fw_net
                               : num 0.159 0.226 0.198 0.223 0.216 ...
## $ ratio
                              : num 178 243 132 266 255 ...
## $ clean_grain_1
## $ clean_grain_2
                               : num 0000000000...
## $ clean_grain_m2
                               : num 1121 1076 665 1193 1183 ...
## $ grain_yield
                               : num 12791 12274 7587 13605 13492 ...
## - attr(*, "spec")=
##
    .. cols(
##
        site year = col character(),
##
    .. exp_plot_number = col_double(),
##
    .. block = col_double(),
##
    .. plot = col_double(),
    .. plot_id = col_double(),
##
##
    .. N_level = col_double(),
    .. tare1 = col_double(),
##
       fw1_plus_tare1 = col_double(),
    .. fw2_plus_tare1 = col_double(),
##
##
    .. ss_fw_plus_tare1 = col_double(),
##
    .. clean_grain_odw_plus_tare2 = col_double(),
##
       tare2 = col_double(),
##
    .. yc_clean_grain_odw_plus_tare_3 = col_double(),
##
    .. tare_3 = col_double()
##
    ..)
nup <- data.frame(ndvi_data$site_year , ndvi_data$N_Uptake , ndvi_data$NDVI) #calls the N Uptake values
str(nup)
## 'data.frame':
                 259 obs. of 3 variables:
## $ ndvi_data.site_year: Factor w/ 11 levels "Arbuckle-15",..: 1 1 1 1 1 1 1 1 1 1 ...
## $ ndvi_data.N_Uptake : num 17.84 25.58 6.41 12.3 19.3 ...
## $ ndvi data.NDVI
                     : num 0.735 0.784 0.527 0.685 0.755 ...
nup <- nup[!(nup$ndvi_data.site_year == "Farm Survey-15"),] #deletes Farm Survey since it doesnt have y
str(nup)
## 'data.frame':
                 231 obs. of 3 variables:
## $ ndvi data.site year: Factor w/ 11 levels "Arbuckle-15",..: 1 1 1 1 1 1 1 1 1 1 ...
## $ ndvi_data.N_Uptake : num 17.84 25.58 6.41 12.3 19.3 ...
## $ ndvi data.NDVI : num 0.735 0.784 0.527 0.685 0.755 ...
head(nup)
    ndvi data.site year ndvi data.N Uptake ndvi data.NDVI
## 1
           Arbuckle-15
                            17.843952
                                            0.734885
```

0.784360

25.577198

2

Arbuckle-15

```
## 3
             Arbuckle-15
                                   6.410093
                                                   0.527090
## 4
             Arbuckle-15
                                  12.299746
                                                   0.685410
                                  19.304427
## 5
             Arbuckle-15
                                                   0.754675
## 6
             Arbuckle-15
                                   7.670085
                                                   0.665620
tail(nup)
##
       ndvi_data.site_year ndvi_data.N_Uptake ndvi_data.NDVI
## 226
                  Biggs-18
                                    14.104389
                                                    0.7075000
## 227
                  Biggs-18
                                    11.681729
                                                    0.7925000
## 228
                  Biggs-18
                                     3.156508
                                                    0.5066667
## 229
                  Biggs-18
                                    15.657989
                                                    0.7550000
## 230
                  Biggs-18
                                    10.581186
                                                    0.7300000
## 231
                  Biggs-18
                                                    0.700000
                                     9.905855
summary(nup)
##
       ndvi_data.site_year ndvi_data.N_Uptake ndvi_data.NDVI
## Nicolaus-17 :28
                           Min.
                                  : 0.9657
                                               Min.
                                                      :0.1467
## Williams-17 :28
                           1st Qu.: 7.4993
                                               1st Qu.:0.6567
## Arbuckle-18 :24
                           Median :11.8504
                                               Median :0.7133
                                  :11.9420
## Marysville-18:24
                           Mean
                                               Mean
                                                     :0.6814
## Nicolaus-18
                :24
                           3rd Qu.:16.2583
                                               3rd Qu.:0.7575
                 :23
                                  :25.5772
## Biggs-18
                           Max.
                                               Max.
                                                     :0.8233
## (Other)
                 :80
yield <- yield_data$grain_yield #calls the grain yield values from yield data
yield_data <- data.frame( nup, yield) #creates a dataframe with these three columns, that are needed fo
head(yield_data)
     ndvi_data.site_year ndvi_data.N_Uptake ndvi_data.NDVI
                                                                yield
                                                   0.734885 12791.283
## 1
             Arbuckle-15
                                  17.843952
## 2
             Arbuckle-15
                                  25.577198
                                                   0.784360 12273.760
                                                   0.527090 7586.925
## 3
             Arbuckle-15
                                   6.410093
## 4
             Arbuckle-15
                                  12.299746
                                                   0.685410 13604.600
## 5
             Arbuckle-15
                                  19.304427
                                                   0.754675 13492.167
## 6
             Arbuckle-15
                                   7.670085
                                                   0.665620 11388.668
tail(yield_data)
       ndvi_data.site_year ndvi_data.N_Uptake ndvi_data.NDVI
##
## 226
                  Biggs-18
                                    14.104389
                                                    0.7075000 12740.258
## 227
                  Biggs-18
                                    11.681729
                                                    0.7925000 12069.239
## 228
                  Biggs-18
                                     3.156508
                                                    0.5066667 7655.621
## 229
                  Biggs-18
                                    15.657989
                                                    0.7550000 12411.614
## 230
                                                    0.7300000 12775.161
                  Biggs-18
                                    10.581186
## 231
                  Biggs-18
                                     9.905855
                                                    0.7000000 12628.612
colnames(yield_data) <- c( "site_year" , "n_uptake" , "ndvi" , "yield" )</pre>
head(yield_data)
       site_year n_uptake
                               ndvi
                                         yield
## 1 Arbuckle-15 17.843952 0.734885 12791.283
## 2 Arbuckle-15 25.577198 0.784360 12273.760
## 3 Arbuckle-15 6.410093 0.527090 7586.925
## 4 Arbuckle-15 12.299746 0.685410 13604.600
```

```
## 5 Arbuckle-15 19.304427 0.754675 13492.167
## 6 Arbuckle-15 7.670085 0.665620 11388.668
str(yield_data)
## 'data.frame':
                   231 obs. of 4 variables:
## $ site_year: Factor w/ 11 levels "Arbuckle-15",..: 1 1 1 1 1 1 1 1 1 1 ...
## $ n_uptake : num 17.84 25.58 6.41 12.3 19.3 ...
             : num 0.735 0.784 0.527 0.685 0.755 ...
              : num 12791 12274 7587 13605 13492 ...
## $ yield
yield_data$site_year <- factor(yield_data$site_year , levels = c("Arbuckle-15" , "RES-15" , "Davis-16"
Table 4
summary(subset(yield data, site year == "Arbuckle-15")) #this subsets the yield data just by Arbuckle-1
##
         site_year
                      n_uptake
                                         ndvi
                                                        yield
## Arbuckle-15:20
                   Min. : 4.885
                                   Min.
                                           :0.4875
                                                     Min. : 6469
## RES-15
             : 0
                                    1st Qu.:0.6854
                                                     1st Qu.:11337
                    1st Qu.:10.546
## Davis-16
             : 0
                    Median :13.280
                                    Median :0.7398
                                                     Median :13176
## RES-16
              : 0
                    Mean
                         :14.144
                                    Mean :0.7057
                                                     Mean
                                                           :12072
## Nicolaus-17: 0
                    3rd Qu.:18.209
                                    3rd Qu.:0.7670
                                                     3rd Qu.:13824
## Williams-17: 0
                    Max. :25.577
                                    Max. :0.7844
                                                     Max.
                                                           :14529
## (Other)
             : 0
summary(subset(yield_data, site_year == "RES-15"))
                                                         yield
##
         site_year
                       n_uptake
                                         ndvi
## RES-15
              :20
                    Min. : 4.174
                                    Min.
                                           :0.5271
                                                     Min. : 5235
## Arbuckle-15: 0
                    1st Qu.: 8.592
                                    1st Qu.:0.6928
                                                     1st Qu.:11317
                                                     Median :12621
## Davis-16
             : 0
                    Median :12.658
                                    Median :0.7745
                          :12.647
## RES-16
              : 0
                   Mean
                                    Mean
                                          :0.7339
                                                     Mean
                                                           :11753
## Nicolaus-17: 0
                                    3rd Qu.:0.7943
                                                     3rd Qu.:12942
                    3rd Qu.:18.156
## Williams-17: 0
                    Max. :23.051
                                    Max.
                                           :0.8042
                                                     Max.
                                                           :14140
## (Other) : 0
summary(subset(yield_data, site_year == "Davis-16"))
##
                      n_uptake
                                         ndvi
         site_year
                                                        yield
## Davis-16 :20
                   Min. : 2.030
                                    Min. :0.5567
                                                     Min. : 6664
                    1st Qu.: 4.016
## Arbuckle-15: 0
                                    1st Qu.:0.6458
                                                     1st Qu.: 8497
## RES-15
              : 0
                    Median : 5.919
                                    Median :0.6667
                                                     Median :10457
## RES-16
              : 0
                    Mean : 5.888
                                    Mean :0.6665
                                                     Mean :10599
## Nicolaus-17: 0
                    3rd Qu.: 7.968
                                    3rd Qu.:0.6917
                                                     3rd Qu.:12557
## Williams-17: 0
                    Max. :11.467
                                    Max.
                                           :0.7233
                                                     Max. :13969
## (Other)
summary(subset(yield_data, site_year == "RES-16"))
         site_year
                       n_uptake
                                         ndvi
                                                         yield
## RES-16
              :20
                    Min. : 3.086
                                           :0.3567
                                                     Min. : 6653
                                    Min.
## Arbuckle-15: 0
                    1st Qu.: 6.294
                                    1st Qu.:0.6167
                                                     1st Qu.:10623
## RES-15
             : 0
                    Median :11.187
                                    Median :0.6850
                                                     Median :11700
## Davis-16
             : 0
                    Mean :10.324
                                    Mean :0.6382
                                                     Mean :11246
## Nicolaus-17: 0
                    3rd Qu.:13.442
                                    3rd Qu.:0.7233
                                                     3rd Qu.:12358
```

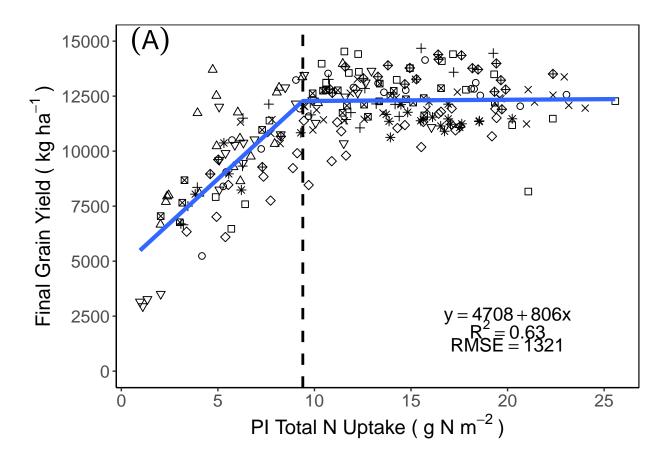
```
## Williams-17: 0 Max. :19.260 Max. :0.7467 Max. :14675
## (Other)
summary(subset(yield_data, site_year == "Nicolaus-17"))
                                                      yield
         site_year
                      n_uptake
                                       ndvi
## Nicolaus-17:28
                   Min. : 6.171
                                  Min. :0.4933
                                                  Min. :10345
## Arbuckle-15: 0
                   1st Qu.:10.062 1st Qu.:0.6417
                                                  1st Qu.:11432
## RES-15
            : 0
                   Median :13.893 Median :0.6850
                                                  Median :12042
## Davis-16 : 0
                   Mean :14.766 Mean :0.6842
                                                  Mean :12005
## RES-16 : 0
                   3rd Qu.:19.986
                                 3rd Qu.:0.7733
                                                  3rd Qu.:12460
## Williams-17: 0
                   Max. :24.021
                                  Max. :0.8000
                                                  Max. :13375
## (Other) : 0
summary(subset(yield_data, site_year == "Williams-17"))
##
         site_year
                     n_uptake
                                       ndvi
                                                      yield
## Williams-17:28
                  Min. : 3.381 Min. :0.3567
                                                  Min. : 6096
## Arbuckle-15: 0
                   1st Qu.: 9.050 1st Qu.:0.6733
                                                  1st Qu.: 9132
## RES-15
             : 0
                   Median :11.876 Median :0.7650
                                                  Median :10924
             : 0
## Davis-16
                   Mean :12.459
                                  Mean :0.7058
                                                  Mean :10159
            : 0
## RES-16
                   3rd Qu.:16.687
                                   3rd Qu.:0.7967
                                                   3rd Qu.:11341
## Nicolaus-17: 0
                   Max. :19.430
                                  Max. :0.8233
                                                  Max.
                                                        :12829
## (Other)
            : 0
summary(subset(yield_data, site_year == "Arbuckle-18"))
                                                       yield
##
         site_year
                      n_uptake
                                        ndvi
                   Min. : 0.9657
## Arbuckle-18:24
                                    Min.
                                          :0.1467
                                                   Min. : 2948
## Arbuckle-15: 0
                   1st Qu.: 5.0762
                                    1st Qu.:0.6062
                                                   1st Qu.: 9566
## RES-15
            : 0
                   Median : 7.5737
                                    Median :0.6800
                                                   Median :10646
## Davis-16 : 0
                   Mean
                        : 7.6532
                                   Mean
                                         :0.6070
                                                   Mean : 9980
## RES-16
            : 0
                   3rd Qu.:10.4248
                                    3rd Qu.:0.7244
                                                   3rd Qu.:12354
## Nicolaus-17: 0
                   Max. :16.0598
                                   Max.
                                          :0.7525
                                                   Max.
                                                         :13648
## (Other)
            : 0
summary(subset(yield_data, site_year == "Biggs-18"))
##
         site_year
                      n uptake
                                       ndvi
                                                      yield
## Biggs-18 :23
                   Min. : 2.037
                                  Min. :0.3625
                                                  Min. : 6767
## Arbuckle-15: 0
                                                   1st Qu.:11593
                   1st Qu.:10.175
                                  1st Qu.:0.7037
## RES-15
            : 0
                   Median :12.570 Median :0.7475
                                                  Median :12207
## Davis-16 : 0
                                  Mean :0.6931
                   Mean :11.359
                                                  Mean :11468
## RES-16
           : 0
                   3rd Qu.:14.422 3rd Qu.:0.7712
                                                  3rd Qu.:12684
## Nicolaus-17: 0
                                 Max. :0.7925
                   Max. :19.341
                                                  Max. :13069
  (Other)
summary(subset(yield_data, site_year == "Marysville-18"))
           site_year
                       n_uptake
                                         ndvi
                                                        yield
                                    Min. :0.4500
## Marysville-18:24
                     Min. : 3.826
                                                    Min. : 8046
## Arbuckle-15 : 0
                     1st Qu.:13.828
                                    1st Qu.:0.6669
                                                    1st Qu.:10887
## RES-15
               : 0
                    Median :15.784
                                    Median :0.6950
                                                    Median :11352
                                                    Mean :11000
## Davis-16
               : 0
                    Mean :14.202
                                    Mean :0.6619
## RES-16
               : 0
                     3rd Qu.:16.954
                                    3rd Qu.:0.7206
                                                    3rd Qu.:11490
## Nicolaus-17 : 0
                    Max. :20.240
                                    Max. :0.7500
                                                    Max. :12246
## (Other)
               : 0
```

```
summary(subset(yield_data, site_year == "Nicolaus-18"))
                       n_uptake
##
         site_year
                                         ndvi
                                                         yield
##
  Nicolaus-18:24
                    Min. : 4.603
                                    Min.
                                           :0.5825
                                                     Min. : 8961
## Arbuckle-15: 0
                    1st Qu.:11.428
                                    1st Qu.:0.7125
                                                     1st Qu.:12688
## RES-15
             : 0
                    Median :15.108 Median :0.7375
                                                     Median :13289
## Davis-16
              : 0
                    Mean
                          :14.603 Mean :0.7170
                                                     Mean
                                                            :12793
## RES-16
             : 0
                    3rd Qu.:18.685
                                    3rd Qu.:0.7575
                                                     3rd Qu.:13794
## Nicolaus-17: 0
                    Max. :22.352 Max.
                                           :0.7725
                                                            :14391
                                                     Max.
## (Other)
summary(yield_data)
                                                            yield
##
           site_year
                         n_uptake
                                            ndvi
## Nicolaus-17 :28
                     Min. : 0.9657
                                              :0.1467
                                                        Min.
                                                               : 2948
                                       Min.
## Williams-17 :28
                      1st Qu.: 7.4993
                                                        1st Qu.:10442
                                       1st Qu.:0.6567
                                      Median :0.7133
## Arbuckle-18 :24
                     Median :11.8504
                                                        Median :11741
## Marysville-18:24
                      Mean :11.9420
                                       Mean :0.6814
                                                        Mean :11291
## Nicolaus-18 :24
                      3rd Qu.:16.2583
                                       3rd Qu.:0.7575
                                                        3rd Qu.:12773
## Biggs-18
                :23
                      Max.
                             :25.5772
                                      Max. :0.8233
                                                        Max.
                                                              :14675
## (Other)
                :80
yield_avgs <- yield_data %>%
 group_by(site_year) %>%
 summarise(avg_yield = mean(yield)) #average yield for all sites
yield_avgs
## # A tibble: 10 x 2
##
     site_year avg_yield
##
     <fct>
                       <dbl>
                      12072.
## 1 Arbuckle-15
## 2 RES-15
                      11753.
## 3 Davis-16
                      10599.
## 4 RES-16
                      11246.
## 5 Nicolaus-17
                      12005.
## 6 Williams-17
                      10159.
## 7 Arbuckle-18
                       9980.
## 8 Biggs-18
                      11468.
## 9 Marysville-18
                      11000.
## 10 Nicolaus-18
                      12793.
cv(yield_avgs$avg_yield)
## [1] 7.901049
Model (Yield ~ N Uptake)
set.seed(10)
lin.mod <- lm(yield ~ n_uptake, data = yield_data)</pre>
segmented.mod <- segmented(lin.mod , seg.Z = ~n_uptake, psi = 9)</pre>
summary(segmented.mod)
```

```
## ***Regression Model with Segmented Relationship(s)***
##
## Call:
## segmented.lm(obj = lin.mod, seg.Z = ~n_uptake, psi = 9)
## Estimated Break-Point(s):
     Est. St.Err
## 9.397 0.451
##
## Meaningful coefficients of the linear terms:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 4707.63
                           422.66
                                     11.14 <2e-16 ***
## n_uptake
                 805.77
                             69.91
                                     11.53
                                             <2e-16 ***
## U1.n_uptake -800.46
                             75.65 -10.58
                                                  NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1332 on 227 degrees of freedom
## Multiple R-Squared: 0.6397, Adjusted R-squared: 0.6349
## Convergence attained in 5 iterations with relative change 1.091534e-05
my.fitted <- fitted(segmented.mod)</pre>
my.model <- data.frame(yield_data$n_uptake , my.fitted)</pre>
mse.seg.mod<- mean(residuals(segmented.mod)^2)</pre>
rmse.seg.mod <- sqrt(mse.seg.mod)</pre>
rmse.seg.mod
## [1] 1320.506
confint.segmented(segmented.mod)
## $n_uptake
       Est. CI(95%).1 CI(95%).u
## 9.39736 8.50782
                        10.2869
pscore.test(lin.mod, seg.Z = ~n_uptake, k = 10)
## Score test for one change in the slope
## data: formula = yield ~ n_uptake ,
                                         method = lm
## model = gaussian , link = identity
## segmented variable = n_uptake
## observed value = -9.1617, n.points = 10, p-value < 2.2e-16
## alternative hypothesis: two.sided
breakpoint <- segmented.mod$psi[2]</pre>
prediction <- nup_a*(breakpoint^2) + nup_b*breakpoint + nup_c</pre>
prediction
## [1] 0.664761
```

Plot (Yield ~ N Uptake)

```
aaa <- ggplot(data = yield_data , aes(x = n_uptake , y = yield )) +</pre>
  geom_point(mapping = aes(n_uptake , yield , shape = site_year) , data = yield_data, size = 2) +
  theme_classic() +
  labs( x = "PI Total N Uptake ( g N m"^-2~")" , y = "Final Grain Yield ( kg ha"^-1~")", shape = "Site-"
  theme(axis.title = element text(size = 15)) +
  theme(axis.text = element_text(size = 13)) +
  theme(legend.text = element_text(size = 11)) +
  theme(legend.title = element_text(size = 13)) +
  scale_shape_manual(values = seq(0,10)) +
  theme(legend.position = "none") +
  theme(panel.background = element_rect(fill = "white", color = "grey0")) +
  scale_x_continuous(breaks = c(0, 5, 10, 15, 20, 25, 30)) +
  scale_y_continuous(breaks = c(0, 2500, 5000, 7500, 10000, 12500, 15000)) +
  expand_limits(y = 0) +
  geom_line(data = my.model, aes(x = yield_data$n_uptake , y = my.fitted), size = 1.5 , color = "#3366F
  geom_vline( xintercept = segmented.mod$psi[2] , color = "black" , lty = 2 , size = 1)
label_aaa_1 <- paste("(A)")</pre>
label_aaa_2 \leftarrow paste(" y == 4708 + 806 * x")
label_aaa_3 <- paste("R^2 == 0.63")</pre>
label_aaa_4 <- paste("RMSE == 1321")</pre>
aaa <- aaa + annotate("text", x = 1.5, y = 15000, label = label_aaa_1, color="black", size = 7, parse =
aaa <- aaa + annotate("text", x = 20, y = 2500, label = label_aaa_2, color="black", size = 5, parse = T.
aaa <- aaa + annotate("text", x = 20, y = 1900, label = label_aaa_3, color="black", size = 5, parse = T
aaa <- aaa + annotate("text", x = 20, y = 1200, label = label_aaa_4, color="black", size = 5, parse = T
aaa
```



$Model (Yield \sim NDVI)$

```
fm1yield.lm <- lm(yield ~ ndvi, data = yield_data)</pre>
summary(fm1yield.lm)
##
## Call:
## lm(formula = yield ~ ndvi, data = yield_data)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
##
  -4605.3 -866.4
                      48.3 1013.5
                                   3180.8
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                1513.5
                             551.1
                                     2.746
                                             0.0065 **
                14349.3
                                             <2e-16 ***
## ndvi
                             797.0 18.005
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1422 on 229 degrees of freedom
## Multiple R-squared: 0.586, Adjusted R-squared: 0.5842
## F-statistic: 324.2 on 1 and 229 DF, p-value: < 2.2e-16
#tests of normality, linear regression assumptions follow
par(mfrow=c(2,2))
```

plot(fm1yield.lm) Standardized residuals Normal Q-Q Residuals vs Fitted 4000 MODO O Residuals α 0 -4000 **ο** က် 4000 8000 12000 2 0 3 -3 Fitted values Theoretical Quantiles (Standardized residuals Standardized residuals Scale-Location Residuals vs Leverage 1.0 0 Cook's distance 1810^C 0.0 4000 8000 12000 0.02 0.00 0.04 0.06 0.08 Fitted values Leverage acf(fm1yield.lm\$residuals) cor.test(yield_data\$ndvi, fm1yield.lm\$residuals) ## ## Pearson's product-moment correlation ## ## data: yield_data\$ndvi and fm1yield.lm\$residuals ## t = 2.0689e-15, df = 229, p-value = 1 ## alternative hypothesis: true correlation is not equal to 0 ## 95 percent confidence interval: -0.1290777 0.1290777 ## sample estimates: ## 1.367174e-16 mean(fm1yield.lm\$residuals) ## [1] 1.095343e-13 x<- resid(fm1yield.lm) shapiro.test(x) ## Shapiro-Wilk normality test ## ## ## data: x ## W = 0.98648, p-value = 0.02762

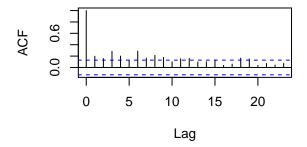
```
mse.yield.mod<- mean(residuals(fm1yield.lm)^2)
mse.yield.mod

## [1] 2003482
rmse.yield.mod <- sqrt(mse.yield.mod)
rmse.yield.mod

## [1] 1415.444
var(yield_data$ndvi)

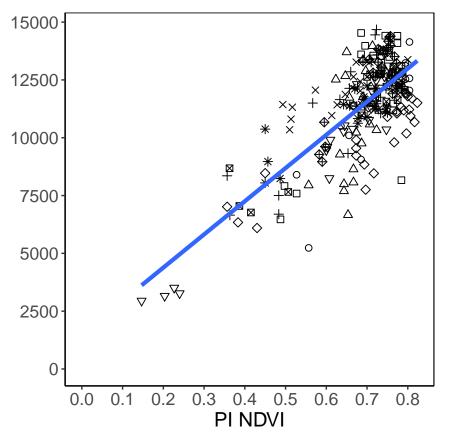
## [1] 0.01383443
predicted_fm1yield <- fitted(fm1yield.lm)
fitted_fm1yield <- data.frame(yield_data$ndvi , predicted_fm1yield)</pre>
```

Series fm1yield.lm\$residuals



Plot Yield $\sim NDVI$

```
bbb <- ggplot(data = yield_data , aes(x = ndvi , y = yield )) +</pre>
  geom_point(mapping = aes(ndvi , yield , shape = site_year) , data = yield_data, size = 2) +
  theme_classic() +
  labs( x = "PI NDVI" , y = NULL, shape = "Site-Year") +
 theme(axis.title = element_text(size = 15)) +
  theme(axis.text = element_text(size = 13)) +
  theme(legend.text = element_text(size = 15)) +
  theme(legend.title = element_text(size = 15)) +
  scale_shape_manual(values = seq(0,10)) +
  theme(plot.title = element_text(size = 15, hjust = .5)) +
  theme(panel.background = element_rect(fill = "white", color = "grey0")) +
  scale_x = c(0, 0.10, .20, .30, .40, .50, .60, .70, .80, .90, 1.0)) +
  scale_y_continuous(breaks = c(0, 2500, 5000, 7500, 10000, 12500, 15000)) +
  expand_limits(x = 0, y = 0) +
  geom_line(data = fitted_fm1yield, aes(x = yield_data$ndvi , y = predicted_fm1yield) , size = 1.5 , co
bbb
```

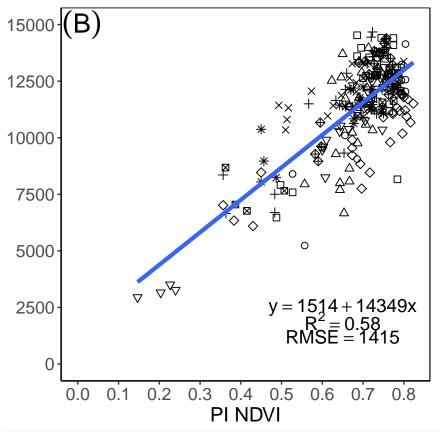


Site-Year

- □ Arbuckle-15
- RES-15
- △ Davis-16
- + RES-16
- × Nicolaus-17
- ♦ Williams–17
- Biggs−18
- * Marysville-18
- ♦ Nicolaus-18

```
label_bbb_1 <- paste("(B)")
label_bbb_2 <- paste(" y == 1514 + 14349 * x")
label_bbb_3 <- paste("R^2 == 0.58")
label_bbb_4 <- paste("RMSE == 1415")

bbb <- bbb + annotate("text", x = .01, y = 15000, label = label_bbb_1, color="black", size = 7, parse = bbb <- bbb + annotate("text", x = .65, y = 2500, label = label_bbb_2, color="black", size = 5, parse = bbb <- bbb + annotate("text", x = .65, y = 1900, label = label_bbb_3, color="black", size = 5, parse = bbb <- bbb + annotate("text", x = .65, y = 1200, label = label_bbb_4, color="black", size = 5, parse = bbb <- bbb + annotate("text", x = .65, y = 1200, label = label_bbb_4, color="black", size = 5, parse = bbb <- bbb + annotate("text", x = .65, y = 1200, label = label_bbb_4, color="black", size = 5, parse = bbb</pre>
```



Site-Year

- □ Arbuckle-15
- RES-15
- △ Davis–16
- + RES-16
- × Nicolaus-17
- ♦ Williams–17
- Biggs−18
- * Marysville-18
- ♦ Nicolaus-18

```
g_legend <- function(bbb){
  tmp <- ggplot_gtable(ggplot_build(bbb))
  leg <- which(sapply(tmp$grobs, function(x) x$name) == "guide-box")
  legend <- tmp$grobs[[leg]]
  return(legend)}
legend3 <- g_legend(bbb) #extracts the legend from plot c

bbb <- bbb +
  theme(legend.position = "none")</pre>
```

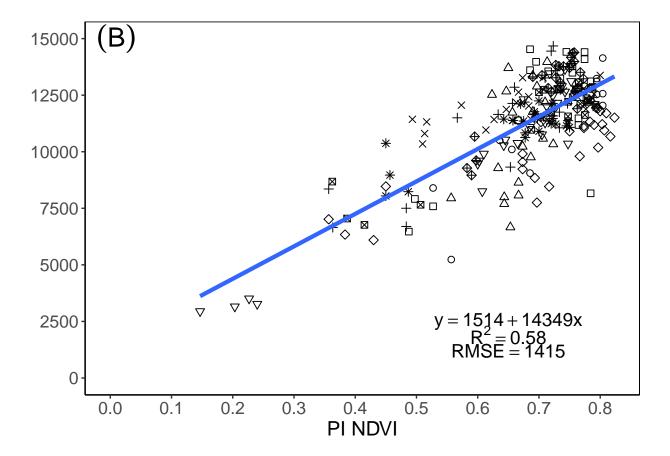
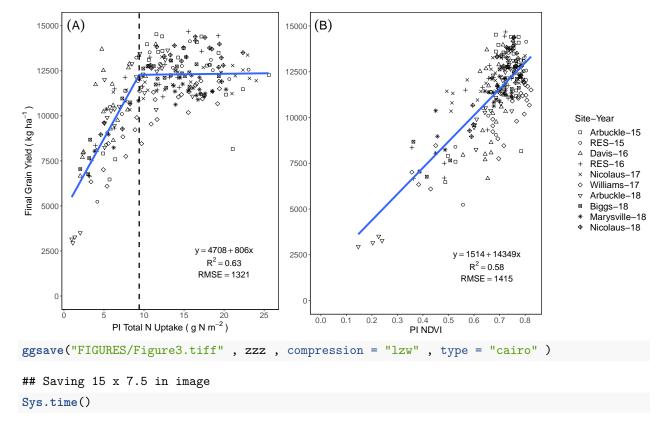


Figure 3



[1] "2019-03-21 13:45:23 PDT"