

Automated and Early Detection of Disease Outbreaks

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DTU Compute

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Introduction

About me



- MSc Eng., Quantitative Biology and Disease Modelling @ DTU
- Wife and three kids @ Vedbæk
- Passionate about e-Sports, particularly Counter Strike



Introduction

Motivation





- Establishment of MiBa by SSI in 2010
- Great opportunity for data analysis
- No fully automated procedures in place at SSI



Algorithms for prospective disease outbreak detection



State-of-the-art algorithms

State-of-the-art algorithms for aberration detection is presented in Salmon, Schumacher, and Höhle 2016 and implemented in the R package **surveillance**. The R package includes the method introduced by Farrington et al. 1996 together with the subsequently improved method proposed by Noufaily et al. 2013.

Algorithms for prospective disease outbreak detection



Novel algorithm

The novel algorithm utilizes a generalized mixed effects model or a hierarchical mixed effects model as a modeling framework to model the count case observations y and assess the unobserved random effects u. These random effects are used directly to characterize an outbreak.



Formulation of hierarchical models

Poisson Normal

$$m{Y}|m{u} \sim \mathrm{Pois}\left(m{\lambda} \exp(m{u})
ight) \ m{u} \sim \mathrm{N}(m{0}, I\sigma^2)$$

Poisson Gamma

$$m{Y}|m{u} \sim ext{Pois}(m{\lambda}m{u}) \ m{u} \sim ext{G}(\mathbf{1}/\phi,\phi)$$



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$$Y \sim NB \left(1/\phi, 1/(\lambda \phi + 1) \right)$$



Step 1: Modeling framework

- Assume a hierarchical Poisson Normal or Poisson Gamma model to reference data using a log link
- Incorporate covariates by supplying a model formula on the form

$$\log(\lambda_{it}) = \boldsymbol{x}_{it}\boldsymbol{\beta} + \log(n_{it}), \quad i = 1, \dots, m, \quad t = 1, \dots, T$$
(1)

ullet Account for structural changes in the time series using a rolling window of width k



Step 2: Inference of random effects

- ullet Infer one-step ahead random effects \hat{u}_{it_1} for each group using the fitted model
- ullet Define outbreak detection threshold U_{t_0} as a quantile of the second stage model's random effects distribution
- Use either a Gaussian or Gamma distribution with respective plug-in estimates



Step 3: Parameter estimations and outbreak detection

- ullet Compare inferred random effects \hat{u}_{it_1} to a threshold U_{t_0}
- Raise and alarm if the inferred random effect exceeds the threshold, i.e. $\hat{u}_{it_1} > U_{t_0}$
- Omit outbreak related observations from future parameter estimation



Shiga toxin (verotoxin)-producing *Escherichia coli* (STEC)

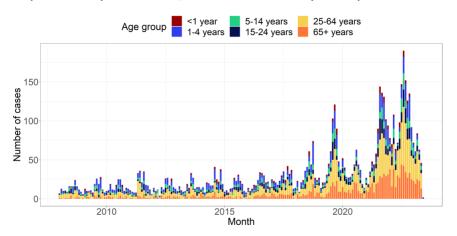


Figure: A stacked bar graph illustrating the number of monthly STEC cases observed in the period from 2008 to 2022 for the six age groups.

Constant model



$$\log(\lambda_{it}) = \beta(ageGroup_i) + \log(n_{it}) \tag{2}$$

- \bullet λ_{it} is the outbreak intensity at time t for age group i
- ullet $eta(ageGroup_i)$ is the fixed effect specific to age group i
- ullet $\log(n_{it})$ acts as an offset, accounting for the population size at time t for age group i

Trend model



$$\log(\lambda_{it}) = \beta(ageGroup_i) + \beta_{trend}t + \log(n_{it})$$
(3)

- In addition to constant model, includes a trend component
- \bullet β_{trend} quantifies the rate of change in the outbreak intensity over time

Seasonality model



$$\log(\lambda_{it}) = \beta(ageGroup_i) + \sin\left(\frac{2\pi \cdot \tau_t}{12}\right)\beta_{\sin} + \cos\left(2\frac{\pi \cdot \tau_t}{12}\right)\beta_{\cos} + \log(n_{it})$$
 (4)

- In addition to constant model, incorporates an annual seasonality pattern
- τ_t represents the time period t within a year (1-12)
- ullet eta_{\sin} and eta_{\cos} capture the effect of the seasonal pattern

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Combined trend and seasonality model

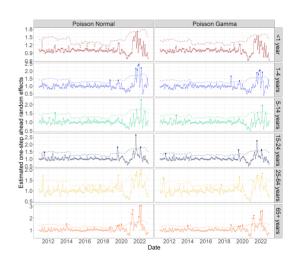
$$\log(\lambda_{it}) = \beta(ageGroup_i) + \beta_{trend}t + \sin\left(\frac{2\pi \cdot \tau_t}{12}\right)\beta_{\sin} + \cos\left(\frac{2\pi \cdot \tau_t}{12}\right)\beta_{\cos} + \log(n_{it}) \quad (5)$$

- Builds upon previous models, combining trend and seasonality components
- \bullet Includes both $\beta_{trend},~\beta_{\sin},$ and β_{\cos} parameters

Estimated one-step ahead random effects



- A rolling window of width k=36 months is employed
- The combined model minimizes the logarithmic score
- Upper bound U_{t_0} is based on the 90% quantile of the random effects distribution
- If the one-step ahead random effects u_{it_1} exceeds U_{t_0} an alarm is raised
- 30 alarms are generated using the Poisson
- A great number of alarms are generated in the

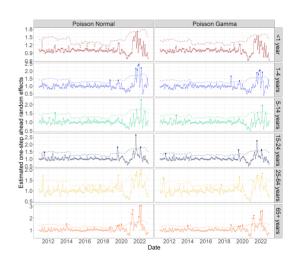


Case study

Estimated one-step ahead random effects

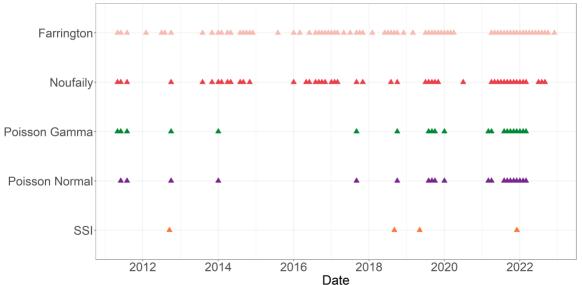


- A rolling window of width k = 36 months is
- The combined model minimizes the logarithmic
- Upper bound U_{t_0} is based on the 90% quantile of
- If the one-step ahead random effects u_{it_1} exceeds
- 30 alarms are generated using the Poisson Normal framework, while 31 alarms are generated using the Poisson Gamma framework.
- A great number of alarms are generated in the period from March 2021 to March 2022





Performance of statistical outbreak detection algorithms



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Baseline data

Simulated baseline data is generated according to a Negative Binomial distribution with mean μ and a variance parameter $\phi\mu$. The equation for the mean $\mu(t)$ is given as:

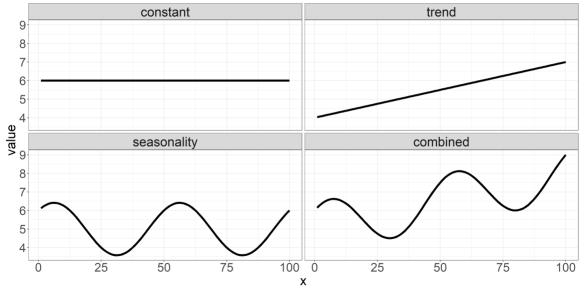
$$\mu(t) = \exp\left(\theta + \beta_{trend}t + \sum_{j=1}^{m} \left(\gamma_1 \cos\left(\frac{2\pi jt}{52}\right) + \gamma_2 \sin\left(\frac{2\pi jt}{52}\right)\right)\right)$$
 (6)

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Scenarios

Scenario	θ	φ	β	γ_1	γ_2	m	Trend
1	0.1	1.5	0.0000	0.00	0.00	0	0
2	0.1	1.5	0.0000	0.60	0.60	1	0
3	0.1	1.5	0.0025	0.00	0.00	0	1
4	0.1	1.5	0.0025	0.60	0.60	1	1
5	-2.0	2.0	0.0000	0.00	0.00	0	0
6	-2.0	2.0	0.0000	0.10	0.30	1	0
7	-2.0	2.0	0.0050	0.00	0.00	0	1
8	-2.0	2.0	0.0050	0.10	0.30	1	1
25	5.0	1.2	0.0000	0.00	0.00	0	0
26	5.0	1.2	0.0000	0.05	0.01	1	0
27	5.0	1.2	0.0001	0.00	0.00	0	1
28	5.0	1.2	0.0001	0.05	0.01	1	1

Scenarios illustration



Outbreaks



- Four outbreaks during baseline weeks (313-575), one outbreak during current weeks (576-624)
- Random constant value k is chosen
- ullet Outbreak size v is generated from a Poisson distribution with mean equal to k times the standard deviation from the baseline data
- ullet The v outbreak cases are distributed randomly in time according to a discretized log-normal distribution represented as $Z \sim \lfloor \mathrm{LN}(0, 0.5^2) \rfloor$

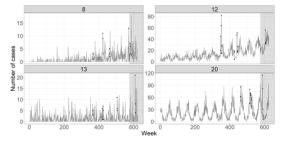
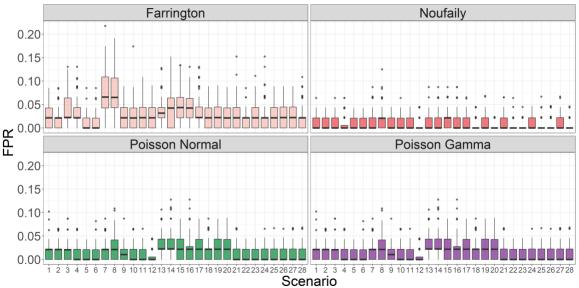


Figure: Plots of one randomly chosen realization for scenario 8, 12, 13, and 20.

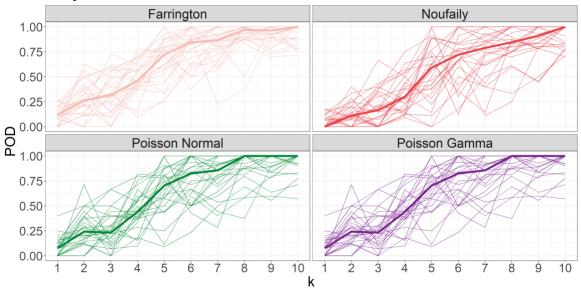
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False Positive Rates



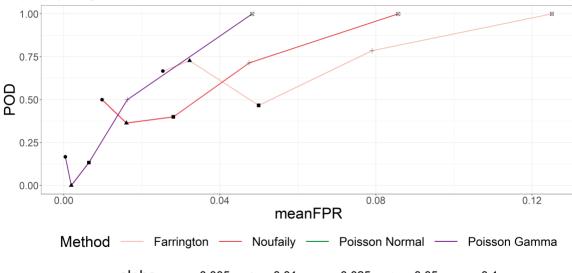
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Probability an outbreak is detected



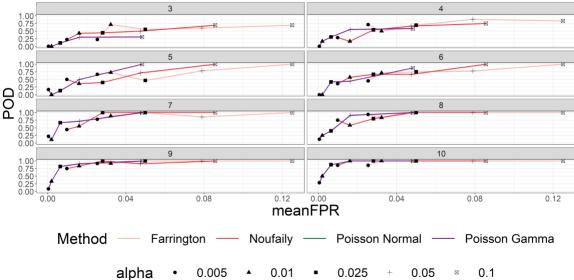






alpha 0.005 0.01 0.025 + 0.05 0.1

Profile of POD vs FPR for different outbreak sizes



Summary

Summary



- Easy incorporation of covariates
- Estimates are consistent across the two modeling frameworks
- Positively **identified outbreaks** coinciding with well-documented outbreaks
- Effectively control the number of "false alarms"
- Great potential in utilizing MiBa-based surveillance

References



- Farrington, C. P. et al. (1996). "A Statistical Algorithm for the Early Detection of Outbreaks of Infectious Disease". In: *Journal of the Royal Statistical Society. Series A (Statistics in Society)* 159.3, pp. 547–563. ISSN: 09641998, 1467985X. URL: http://www.jstor.org/stable/2983331 (visited on 01/27/2023).
- Noufaily, Angela et al. (2013). "An Improved Algorithm for Outbreak Detection in Multiple Surveillance Systems". en. In: *Online Journal of Public Health Informatics* 32.7, pp. 1206–1222.
- Salmon, Maëlle, Dirk Schumacher, and Michael Höhle (2016). "Monitoring Count Time Series in R: Aberration Detection in Public Health Surveillance". In: *Journal of Statistical Software* 70.10, pp. 1–35. DOI: 10.18637/jss.v070.i10. URL:

https://www.jstatsoft.org/index.php/jss/article/view/v070i10.

Probability function for *Y*

$$P[Y = y] = g_{Y}(y; \boldsymbol{\beta}, \phi)$$

$$= \frac{\lambda^{y}}{y!\Gamma(1/\phi)\phi^{1/\phi}} \frac{\phi^{y+1/\phi}\Gamma(y+1/\phi)}{(\lambda\phi+1)^{y+1/\phi}}$$

$$= \frac{\Gamma(y+1/\phi)}{\Gamma(1/\phi)y!} \frac{1}{(\lambda\phi+1)^{1/\phi}} \left(\frac{\lambda\phi}{\lambda\phi+1}\right)^{y}$$

$$= \left(\frac{y+1/\phi-1}{y}\right) \frac{1}{(\lambda\phi+1)^{1/\phi}} \left(\frac{\lambda\phi}{\lambda\phi+1}\right)^{y}, \quad \text{for } y = 0, 1, 2, \dots$$

$$(7)$$

where the following convention is used

The marginal distribution of Y is a negative binomial distribution, $Y \sim NB(1/\phi, 1/(\lambda \phi + 1))$

Proof

The probability function for the conditional distribution of Y for given u

$$f_{Y|u}(y; u, \beta) = \frac{(\lambda u)^y}{y!} \exp(-\lambda u)$$
(9)

and the probability density function for the distribution of u is

$$f_u(u;\phi) = \frac{1}{\phi\Gamma(1/\phi)} \left(\frac{u}{\phi}\right)^{1/\phi - 1} \exp(-u/\phi)$$
 (10)

Proof



Given (9) and (10), the probability function for the marginal distribution of Y is determined from

$$g_Y(y;\beta,\phi) = \int_{u=0}^{\infty} f_{Y|u}(y;u,\beta) f_u(u;\phi) du$$

$$= \int_{u=0}^{\infty} \frac{(\lambda u)^y}{y!} \exp(-\lambda u) \frac{1}{\phi \Gamma(1/\phi)} \left(\frac{u}{\phi}\right)^{1/\phi - 1} \exp(-u/\phi) du$$

$$= \frac{\lambda^y}{y! \Gamma(1/\phi) \phi^{1/\phi}} \int_{u=0}^{\infty} u^{y+1/\phi - 1} \exp\left(-u(\lambda \phi + 1)/\phi\right) du$$
(11)

Proof

In (11) it is noted that the integrand is the *kernel* in the probability density function for a Gamma distribution, $G\left(y+1/\phi,\phi/(\lambda\phi+1)\right)$. As the integral of the density shall equal one, we find by adjusting the norming constant that

$$\int_{u=0}^{\infty} u^{y+1/\phi-1} \exp\left(-u/(\phi/(\lambda\phi+1))\right) du = \frac{\phi^{y+1/\phi}\Gamma(y+1/\phi)}{(\lambda\phi+1)^{y+1/\phi}}$$
(12)

and then (7) follows