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184.754 Seminar on Algorithms

**Paper: Coloring the Vertices of 9-pt and 27-pt
Stencils with Intervals**

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Introduction

Interval Vertex Coloring (IVC)

- Vertex Color Problem

- Interval Vertex Coloring Problem

- Simple Paragraphs

Special Case Analysis

- Definitions

Heuristics

Application and Experiments

Footnotes

References

Block

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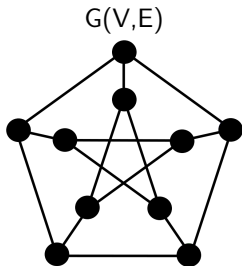
Example

This is an example block.

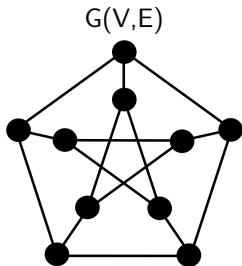
Attention

This is an alert block.

- Given $G(V,E)$



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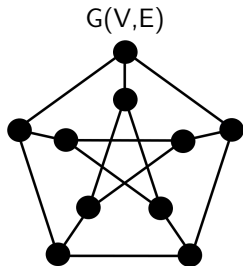


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Formal Definition of VCP given $G(V,E)$

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$\forall v \in V : \forall w \text{ in } \Gamma(v) : f(v) \neq f(w).$

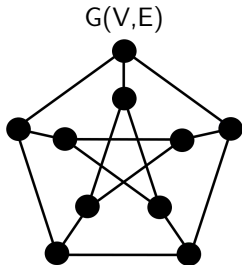


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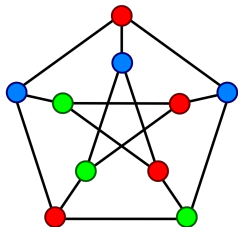
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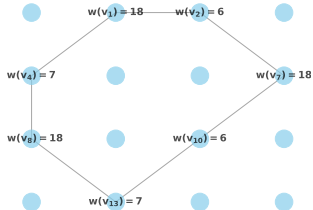


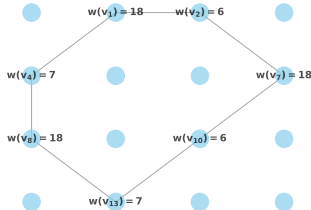
Colored $G(V,E)$



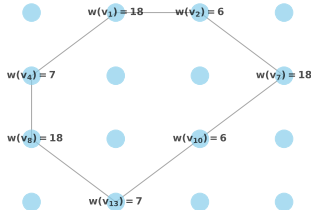
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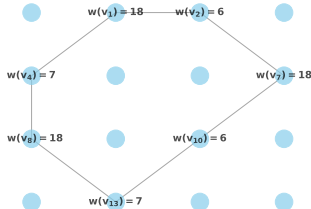


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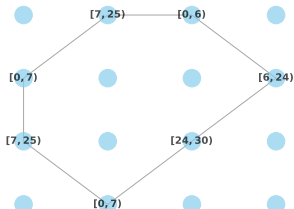
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- Vertex v is colored with open interval: $[\text{start}(v), \text{start}(v) + w(v))$
- Neighboring Vertices must have disjoint color intervals: $\forall (a, b) \in E : [\text{start}(a), \text{start}(a) + w(a)) \cap [\text{start}(b), \text{start}(b) + w(b)) = \emptyset$.

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Interval Colored $G(V,E)$
with $\text{maxcolor} = 25$

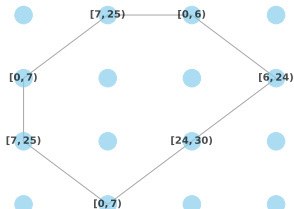


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Optimization Problem Instance:

Find a coloring start : $V \mapsto \mathbb{Z}^+$ that minimizes maxcolor.

- A maxcolor that is indeed minimal, is denoted with maxcolor^* .

Title first category

Title second category

Lets see if the citation works in this part [1]. The second paper I use should appear in the bibliography now [2] and the third one as well [3].

You can cite **Tan11**. Urls look like this: <http://www.google.com/>.

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hi there

hi there!

You can also place footnotes, e.g., here ¹ and here ².

¹This is a footnote.

²This is a longer footnote going over two lines. So I've added some more blah blah. Lorem ipsum whatever.



D. Durrman and E. Saule, "Coloring the vertices of 9-pt and 27-pt stencils with intervals," in *2022 IEEE International Parallel and Distributed Processing Symposium (IPDPS)*, 2022, pp. 963–973. DOI: 10.1109/IPDPS53621.2022.00098.



A. Hohl, E. Delmelle, W. Tang, and I. Casas, "Accelerating the discovery of space-time patterns of infectious diseases using parallel computing," *Spatial and Spatio-temporal Epidemiology*, vol. 19, pp. 10–20, 2016, ISSN: 1877-5845. DOI: <https://doi.org/10.1016/j.sste.2016.05.002>. [Online]. Available: <https://www.sciencedirect.com/science/article/pii/S187758451530040X>.



E. Saule, D. Panchananam, A. Hohl, W. Tang, and E. M. Delmelle, "Parallel space-time kernel density estimation," *2017 46th International Conference on Parallel Processing (ICPP)*, pp. 483–492, 2017. [Online]. Available: <https://api.semanticscholar.org/CorpusID:6645797>.