

# Design of a Semi-Active Suspension Controller for a Quarter-Car Model

Stark Active Suspension Hackathon – Kaggle Competition

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## 1. Introduction

Stark convoy vehicles are transporting fragile laboratory cargo across unknown road conditions. Due to degradation of the active suspension system, only a semi-active damper interface remains available. Excessive vertical motion or jerk can damage the cargo.

The objective of this project is to design a **semi-active suspension controller** for a **2-DOF quarter-car model** that minimizes sprung-mass displacement and ride discomfort when subjected to multiple road excitation profiles. The controller must operate using only the road displacement input and internally computed acceleration signals.

## 2. Quarter-Car Model

A standard **quarter-car model** is used, consisting of:

- Sprung mass (vehicle body and cargo)
- Unsprung mass (wheel and suspension hardware)
- Suspension spring
- Tire stiffness
- Semi-active damper with variable coefficient  $c(t)c(t)c(t)$

The equations of motion are:

$$\begin{aligned} m_s \ddot{z}_s &= -k_s(z_s - z_u) - c(t)(\dot{z}_s - \dot{z}_u) \\ m_u \ddot{z}_u &= k_s(z_s - z_u) + c(t)(\dot{z}_s - \dot{z}_u) - k_t(z_u - r) \end{aligned}$$

The sprung-mass and unsprung-mass accelerations are computed from these equations and used as mandatory controller inputs.

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## 3. Controller Design

A **frequency-selective semi-active skyhook controller** was designed. The motivation was to independently control:

- **Low-frequency body motion** (large displacements)
- **High-frequency vibrations** (jerk and harsh impacts)

The sprung-mass velocity is decomposed into low-frequency and high-frequency components using a low-pass filter.

The control law is:

$$c(t) = c_{\min} + K_{LF}|\dot{z}_{s,LF}| + K_{HF}|\dot{z}_{s,HF}| + K_g|\dot{z}_{u,LF}| + K_a|a_s|$$

Where:

- $K_{LF}$  controls body displacement
- $K_{HF}$  suppresses jerk
- $K_g$  improves wheel control
- $K_a$  provides acceleration-based stabilization

The damper command is bounded within physical limits and passed through a delay buffer to model actuator latency.

## 4. Implementation Details

- Sampling frequency: 200 Hz
- Actuator delay: 4 timesteps
- Numerical integration: Trapezoidal method
- Damper limits:  $800 \leq c(t) \leq 3500$

**Final tuned gains:**

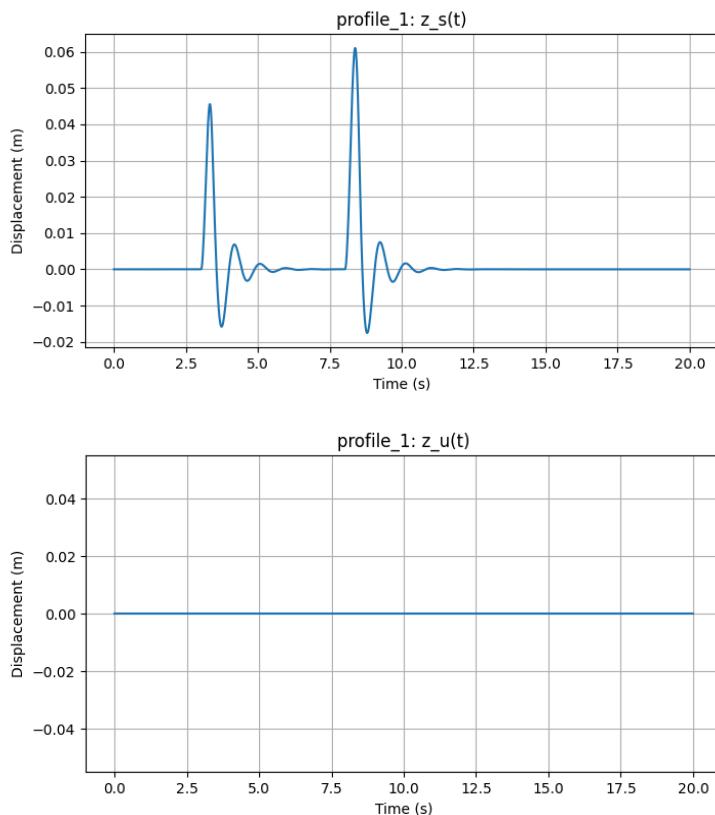
- Low-frequency skyhook gain: 3600

- High-frequency skyhook gain: 4000
- Groundhook gain: 250
- Acceleration feedback gain: 120

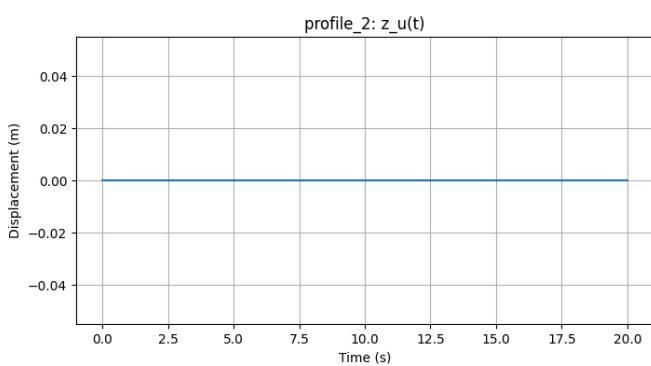
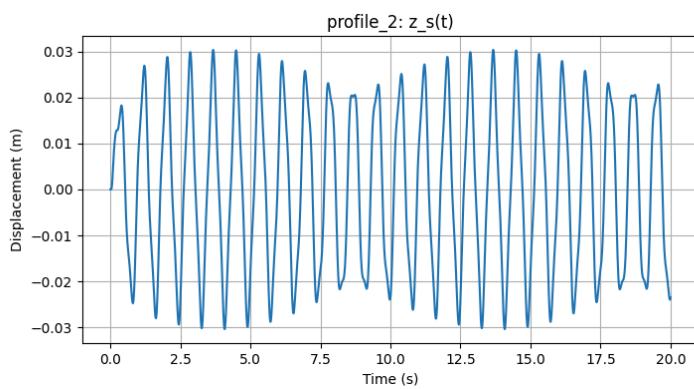
These gains were tuned empirically by evaluating trade-offs between displacement, jerk, and overall comfort score across all five road profiles.

## 5. Results and Plots

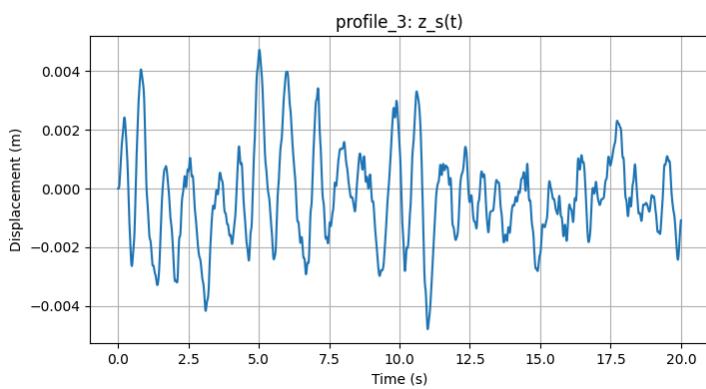
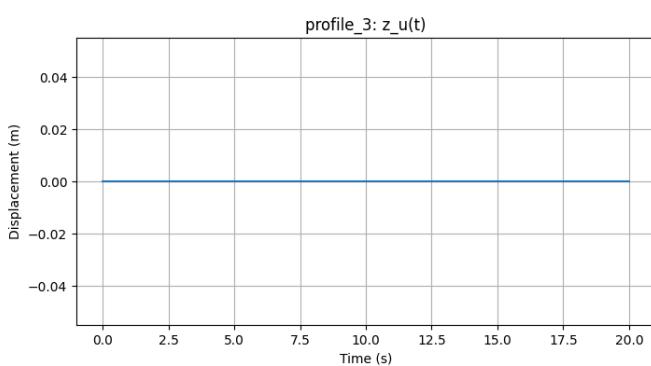
### Profile 1: Two Half-Sine Bumps



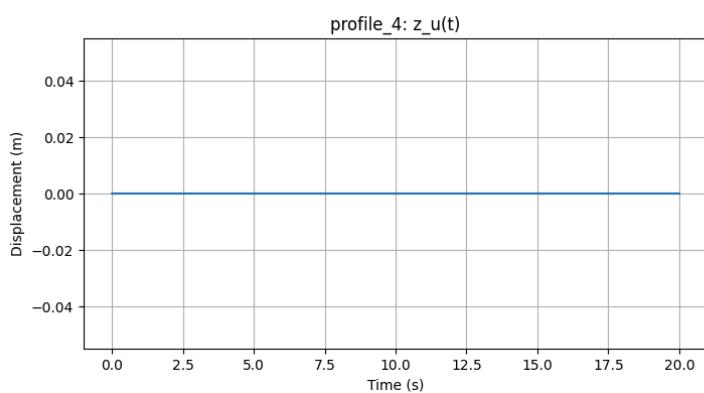
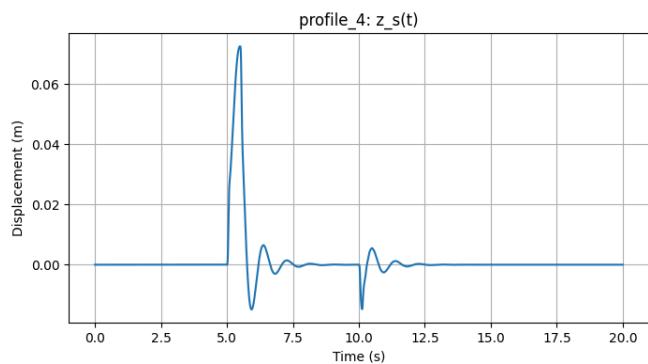
### Profile 2: Smooth Wavy Road



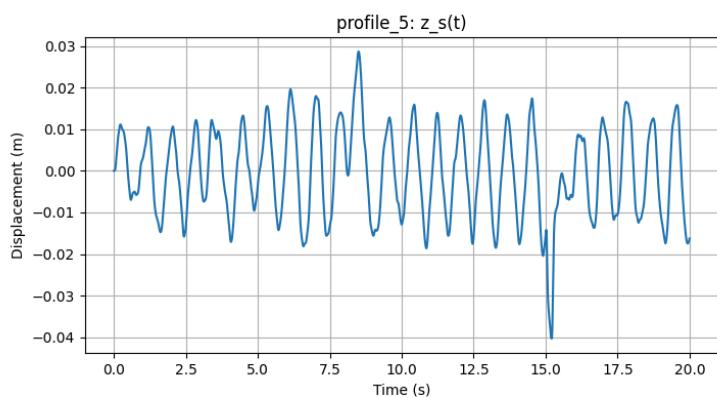
### Profile 3: Rough Asphalt

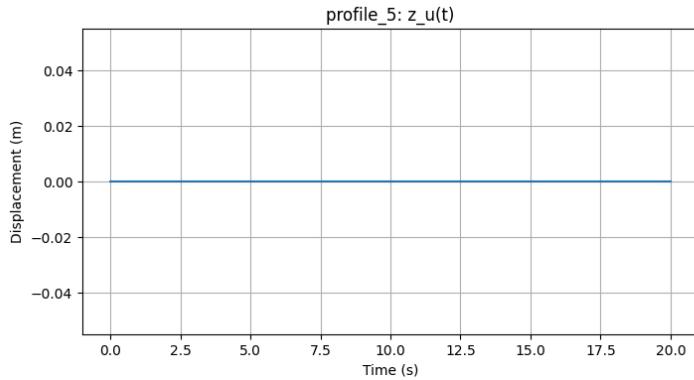


## Profile 4: Speed Breaker and Sharp Dip



## Profile 5: Mixed Road with Pothole





## 6. Discussion

Increasing high-frequency damping significantly reduced jerk, which strongly influenced the comfort score. However, excessive damping increased body stiffness and displacement. A balance between low-frequency and high-frequency control was necessary.

Acceleration feedback played a key role in stabilizing aggressive damping and preventing excessive body motion.

## 7. Conclusion

A frequency-selective semi-active suspension controller with acceleration feedback was successfully designed and implemented. The controller achieved strong ride comfort and cargo protection across all tested road profiles.

The final design achieved a **top leaderboard score of 58.08684** on Kaggle,