Problem G. Rectangular City

Time limit 1000 ms

Mem limit 1048576 kB

OS Linux

The festive season is coming and Rectangular City is going to organize N different events for N consecutive days. Rectangular City, as its name suggests, consists of $R \times C$ blocks. Each event will be hosted on a rectangular area within the city. In order to lighten-up the events, the mayor decides to spend some of the budgets to decorate K blocks on the condition that every decorated block must be used in all N events.

The city council is interested in the number of different ways to organize all N events such that it is possible to choose K different blocks to decorate. Two ways are considered different if there exists a day in which the corresponding event is hosted on a different area. Since the answer can be very large, modulo the output by $1\,000\,000\,007$.

Input

The input contains a line with four integers N, R, C, and K ($1 \le N \le 10^6$; $1 \le R$, $C \le 5\,000$; $1 \le K \le R \cdot C$).

Output

The output contains an integer representing the total number of different ways to organize all events, modulo $1\,000\,000\,007$.

Explanation

In the Sample Input, the city has 2×3 blocks, and the mayor decides to decorate 4 blocks for 2 different events (days). There are a total of 7 ways to organize the events.

```
#1
                                     Decorated: **.
     Day 1: 00.
                      Day 2: 00.
             00.
                             00.
#2
     Day 1: oo.
                      Day 2: 000
                                     Decorated: **.
                             000
             00.
                                     Decorated: .**
#3
     Day 1: .oo
                      Day 2: .oo
             . 00
                              . 00
#4
     Day 1: .oo
                      Day 2: 000
                                     Decorated: .**
                             000
             .00
#5
     Day 1: 000
                      Day 2: 00.
                                     Decorated: **.
```

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Note that, in the example above, configuration #7 uses the whole city for both events, thus, the decorated blocks can be any K blocks in the city. The shown decorated blocks are only given as examples.

Sample 1

Input	Output
2 2 3 4	7