



```
In [108]: 1 import numpy as np
2 import matplotlib.pyplot as plt
3
4 # Define the custom function f(x)
5 def custom_function(x):
6     if 0 <= x <= np.pi:
7         return 1
8     elif -np.pi <= x < 0:
9         return -2 * x / np.pi
10
11 # Fourier series coefficients
12 def fourier_coefficients(f, n):
13     a = np.zeros(n)
14     b = np.zeros(n)
15
16     for i in range(n):
17         a[i] = (1 / np.pi) * np.trapz([f(x) * np.cos(i * x) for x in np.linspace(-np.pi, np.pi, 1000)], dx=2 * np.pi)
18         b[i] = (1 / np.pi) * np.trapz([f(x) * np.sin(i * x) for x in np.linspace(-np.pi, np.pi, 1000)], dx=2 * np.pi)
19
20     return a, b
21
22 # Fourier series approximation
23 def fourier_series(x, a, b, n):
24     series = a[0] / 2
25     for i in range(1, n):
26         series += a[i] * np.cos(i * x) + b[i] * np.sin(i * x)
27     return series
28
29 # Find the lowest peak value to the left and the highest peak value to the right of x=0
30 def find_peaks(x_values, y_values, x_range):
31     # Determine the range of indices within the specified x_range
32     x_min, x_max = x_range
33     x_min_idx = np.argmax(x_values >= x_min)
34     x_max_idx = np.argmax(x_values >= x_max)
35
36     # Find the peak within the specified range
37     x_peak = x_values[x_min_idx:x_max_idx]
38     y_peak = y_values[x_min_idx:x_max_idx]
39
40     # Find the lowest peak to the left
41     left_half_idx = len(y_peak) // 2
42     x_peak_left = x_peak[:left_half_idx][np.argmin(y_peak[:left_half_idx])]
43     y_peak_left = min(y_peak[:left_half_idx])
44
45     # Find the highest peak to the right
46     right_half_idx = len(y_peak) // 2
47     x_peak_right = x_peak[right_half_idx:][np.argmax(y_peak[right_half_idx:])]
48     y_peak_right = max(y_peak[right_half_idx:])
```