## # Kinematics

Quantity	Unit	Definition	
Displacement	m	$\Delta ec{r} = ec{r}_f - ec{r}_i$	
Instantaneous velocity	$\mathrm{m/s}$	$ec{v}=rac{dec{r}}{dt}$	
Instantaneous acceleration	$ m m/s^2$	$ec{a}=rac{dec{v}}{dt}=rac{d^2ec{x}}{dt^2}$	

Description	Equations
Kinematics equations at constant acceleration	$egin{aligned} x &= x_0 + v_0 t + rac{1}{2} a t^2 \ v &= v_0 + a t \ v_f^2 &= v_i^2 + 2 a \Delta x \end{aligned}$
Relative velocity	$ec{v}_{P/A} = ec{v}_{P/B} + ec{v}_{B/A}$
Centripetal acceleration	$a_{ m rad}=rac{v^2}{R}=rac{4\pi^2R}{T^2}$

# # Dynamics

Quantity	Unit	Definition	
Spring force (Hooke's law)	N	$F_s = -k\Delta x$	
Static friction	N	$egin{aligned} f_s & \leq (f_s)_{ ext{max}} = \mu_s F_N \ \mu_s & =  an( heta) \end{aligned}$	
Kinetic friction	N	$f_k = \mu_k F_N$	
Gravitational force near Earth surface	N	$ec{F}_g = m ec{g} \ g = 9.81 \mathrm{m/s^2}$	

Description	Equations
Newton's first law moving at constant velocity	$\sum {ec F}_{ m ext} = ec 0$
Newton's second law	$\sum {ec F}_{ m ext} = m ec a$
Newton's third law	${ec F}_{AB} = - {ec F}_{BA}$
Acceleration on an inclined plane	$a=g\sin heta$

## # Energy

Quantity	Unit	Definition
Work	J	$W = ec{F} \cdot ec{x} = Fx \cos  heta \ W = \int_{x_1}^{x_2} F \ dx$

Quantity	Unit	Definition
Kinetic energy	J	$K=rac{1}{2}mv^2$
Power	W	$P = rac{dW}{dt} = rac{dE}{dt} \ P = ec{F} \cdot ec{v}$
Gravitational potential energy	J	$U=mgh \ W_{ m grav}=-\Delta U_{ m grav}$
Elastic potential energy	J	$egin{aligned} U &= rac{1}{2}kx^2 \ W_{ ext{el}} &= -\Delta U_{ ext{el}} \end{aligned}$
Reduced mass	kg	$\mu=\frac{m_1m_2}{m_1+m_2}$
Coefficient of restitution	-	$e = -\frac{v_{12,f}}{v_{12,i}}$

Description	Equations
Work-energy theorem	$W_{ m total} = \Delta K$
Conservation of mechanical energy	$K_i + U_i = K_f + U_f$
Energy of system with external force (non-isolated system)	$K_i + U_i + W = K_f + U_f$
Conservation of energy	$\Delta K + \Delta U + \Delta U_{int} = 0$
Force as a function of potential energy	$ec{F} = -ec{ abla} U \ F = -rac{dU}{dx}$

#### **# Momentum**

Quantity	Un	it	Definition
Momentum	kg · ı	m/s	$ec{p}=mec{v} \ \sum ec{F}_{ m ext} = rac{dec{p}}{dt}$
Impulse	${ m kg} \cdot { m i}$	m/s	$ec{J} = \sum_{} ec{F} \Delta t \ ec{J} = \int_{t_1}^{t_2} \sum_{} ec{F} \; dt$
Center of mass	m	1	$ec{r}_{ ext{cm}} = rac{\sum\limits_{i} m_i ec{r}_i}{\sum\limits_{i} m_i}$
	Description	Equations	
Impulse-momen	tum theorem	$ec{J}=\Deltaec{p}$	
Conservation of momentum (clo	osed system)	$ec{p}_i = ec{p}_f \ \sum ec{F}_{ m ext} = rac{dec{p}}{dt}$	

 $\sum ec{F}_{
m ext} = m ec{a}_{
m cm}$ 

## # Rotational Kinematics

Force on extended body

Quantity	Unit	Definition
Angular displacement	$\operatorname{rad}$	$\Delta  heta =  heta_f -  heta_i$
Angular velocity	$\mathrm{rad/s}$	$\omega_z=rac{d heta}{dt}$
Angular acceleration	$ m rad/s^2$	$lpha_z=rac{d\omega_z}{dt}=rac{d^2 heta}{dt^2}$
Rotational Inertia of particle	${ m kg\cdot m^2}$	$I = \sum_i m_i r_i^2$
Rotational kinetic energy	J	$K=rac{1}{2}I\omega^2$

Description	Equations
Rotational kinematics equation with constant angular acceleration	$egin{aligned}  heta &=  heta_0 + \omega_{0z} t + rac{1}{2}lpha_z t^2 \ \omega_z &= \omega_{0z} + lpha_z t \ \omega_{fz}^2 &= \omega_{iz}^2 + 2lpha_z \Delta  heta \end{aligned}$
Relationship between linear kinematics and rotational kinematics	$egin{aligned} s &= r  heta \ v &= r \omega \ a_{ an} &= r lpha \ a_{ ext{rad}} &= rac{v^2}{r} = \omega^2 r \end{aligned}$
Parallel-axis theorem	$I_{ m parallel} = I_{ m cm} + m d^2$

# # Rotational Dynamics

Quantity	Unit	Definition
Torque	${ m N}\cdot{ m m}$	$ec{ au}=ec{r} imesec{F}=Fr\sin heta \ \sumec{ au}=rac{dec{L}}{dt}$
Angular momentum of a particle	${ m kg\cdot m^2/s}$	$ec{L}=ec{r} imesec{p}=mvr\sin heta$
Angular momentum of rotating body	${ m kg\cdot m^2/s}$	$ec{L} = I ec{\omega}$

Description	Equations
Rotational Newton's second law	$\sum  au = I lpha_z$
Condition of mechanical equilibrium	$\sum {ec F}_{ m ext} = m ec a \ \sum  au = I lpha_z$
Total kinetic energy of rotating and translating object	$K=rac{1}{2}mv_{ m cm}^2+rac{1}{2}I_{ m cm}\omega^2$
Rolling without slipping	$v_{ m cm}=R\omega$
Slipping (only rolling)	$v_{ m cm} < R \omega$
Skidding (only translating)	$v_{ m cm} > R \omega$
Rotational Work	$egin{aligned} W &=  au_z \Delta  heta \ W &= \int_{ heta_1}^{ heta_2}  au_z \; d heta \ W &= \Delta K_{ ext{rot}} \end{aligned}$

Description	Equations
Power	$P=rac{dW}{dt} \ P= au_z\omega_z$
Conservation of angular momentum (closed system)	$ec{L}_i = ec{L}_f \ \sum ec{ au} = rac{dec{L}}{dt}$

## # Universal Gravitation

Quantity	Unit	Definition	
Gravitational force	N	$F_g=Grac{m_1m_2}{r^2}$	
Gravitational acceleration	$ m m/s^2$	$g=Grac{m_E}{r^2}$	
Gravitational potential energy	J	$U=-Grac{m_E m}{r}$	

Description	Equations
Escape velocity	$v_{ m escape} = \sqrt{rac{2Gm_E}{R}}$
Velocity in circular orbit	$v_{ m circ} = \sqrt{rac{Gm_E}{R}} = rac{2\pi R}{T}$
Period in circular orbit	$T=rac{2\pi R}{v}=2\pi R\sqrt{rac{R}{Gm_E}}=rac{2\pi r^{3/2}}{\sqrt{Gm_E}}$