

# Math 115A: Problem set 2

Sections 1 and 3. Instructor: James Freitag

Due 10/2

## Problem 1 Showing finite dimensionality

Let  $V$  be a vector space and suppose that  $V = \text{span}(\{x_1, \dots, x_n\})$ . Show that  $V$  is finite dimensional.

## Problem 2 Functions without restrictions

Recall that  $\mathcal{F}(\mathbb{R}, \mathbb{R})$  denotes the space of functions  $f : \mathbb{R} \rightarrow \mathbb{R}$ . Show that  $\mathcal{F}(\mathbb{R}, \mathbb{R})$  is infinite dimensional.

## Problem 3 Intermediate subspace

Let  $m, n \in \mathbb{N}$  such that  $m < n - 1$ . Suppose  $V$  is a vector space of dimension  $n$  and  $W$  is a subspace of dimension  $m$ . Show that for each  $k$  with  $m < k < n$  there is a subspace  $U$  such that  $W \leq U \leq V$ .

## Problem 4 Interpolation

Given an example of a polynomial  $p$  which has degree at most 2 such that  $p(x) = 3^x$  for  $x = 1, 2, 3$ .

## Problem 5 Exercises from the book

Do the following exercises from book:

- 1 from section 1.6.
- 3 from section 1.6.