

- 1) Take Data2 and split it into a Training Set of 210 randomly selected data points. Use the remaining 100 data points as the Testing Set. Train a linear support vector machine (kernel_function = linear) to build a classifier model. Use this model to predict the classes for the data in the Testing Set.

```
import numpy as np
from sklearn.utils import shuffle
import pandas as pd
from sklearn.tree import DecisionTreeClassifier
from sklearn.metrics import accuracy_score
from sklearn import tree
from sklearn.metrics import precision_recall_fscore_support
from IPython.display import Image
from sklearn.tree import export_graphviz
import pydotplus
import collections
import matplotlib.pyplot as plt

data1=pd.read_csv('G:\Masters materials\Spring\IDA\Assignment2\Biomechanical_Data_
column_2C_weka.csv')
list(data1.keys()) //lists column name of datasets.
```

- **OUTPUT**

```
['pelvic_incidence',
'pelvic_tilt numeric',
'lumbar_lordosis_angle',
'sacral_slope',
'pelvic_radius',
'degree_spondylolisthesis',
'class']
```

- **Split it into a Training Set of 210 randomly selected data points**

```
data1=shuffle(data1);
X = data1.loc[:, 'pelvic_incidence': 'degree_spondylolisthesis'];
y= data1.loc[:, 'class'];
X_train,X_test,y_train,y_test = X[:210] , X[210:], y[:210] , y[210:];
```

- **Train a linear support vector machine (kernel_function = linear) to build a classifier model, Use this model to predict the classes for the data in the Testing Set.**

```
from sklearn.svm import SVC
clf = SVC(kernel='linear')
clf.fit(X_train,y_train)
predict=clf.predict(X_test)
```

In above code,

SVC() function is equivalent to **svmtrain** function of matlab.

fit() function is used to train the classifier with given **X_train,y_train** train dataset.

predict() function predicts the output given a test dataset

1a) List all the support vectors of the data set. Examine the number of support vectors for each class and their attribute values and comment on what can be inferred from these values.

- **List all the support vectors of the data set. Examine the number of support vectors for each class**

```
print(clf.support_vectors_)
print("support vector for Abnormal class="+str(clf.n_support_[0])+ " support vector for Normal
class="+str(clf.n_support_[1]))
print("Indices of support vectors are\n"+str(clf.support_))
```

support_vectors_ attribute displays the support vectors for a SVM classifier.

n_support attribute displays support vectors for each class.

support_ attribute displays the indices of the support vectors.

Output:

Support Vectors for linear svm:

```
[ [ 68.83202098 22.21848205 50.09219357 46.61353893 105.9851355 -3.53031731]
[ 41.72996308 12.25407408 30.12258646 29.475889 116.5857056 -1.24440249]
[ 69.78100617 13.77746531 57.99999999 56.00354085 118.9306656 17.91456046]
[ 44.31890674 12.53799164 36.098763 31.78091509 124.1158358 5.41582514]
[ 41.35250407 16.57736351 30.70619135 24.77514057 113.2666746 -4.49795756]
[ 70.25043628 10.34012252 76.37007032 59.91031376 119.2370072 32.66650243]
[ 40.55735663 17.97778407 34. 22.57957256 121.0462458 -1.53738307]
[ 48.10923638 14.93072472 35.56468278 33.17851166 124.0564518 7.94790486]
[ 38.69791243 13.44474904 31. 25.25316339 123.1592507 1.42918576]
[ 78.40125389 14.04225971 79.69426258 64.35899418 104.7312342 12.39285327]
[ 45.54078988 13.06959759 30.29832059 32.47119229 117.9808303 -4.98712962]
[ 42.02138603 -6.55494835 67.89999999 48.57633437 111.5857819 27.33867086]
[ 53.85479842 19.23064334 32.77905978 34.62415508 121.6709148 5.3298432 ]
[ 43.20318499 19.66314572 35. 23.54003927 124.8461088 -2.91907595]
[ 65.53600255 24.15748726 45.77516991 41.3785153 136.4403015 16.37808564]
[ 52.41938511 19.01156052 35.87265953 33.40782459 116.5597709 1.6947051 ]
[ 46.85578065 15.35151393 38. 31.50426672 116.2509174 1.66270559]
[ 31.27601184 3.14466948 32.56299592 28.13134236 129.0114183 3.62302007]
[ 66.28539377 26.32784484 47.49999999 39.95754893 121.2196839 -0.79962447]
[ 53.43292815 15.86433612 37.16593387 37.56859203 120.5675233 5.9885507 ]
[ 63.83498162 20.36250706 54.55243367 43.47247456 112.3094915 -0.62252664]
[ 43.34960621 7.46746896 28.06548279 35.88213725 112.7761866 5.75327746]
[ 45.44374959 9.9060718 44.99999999 35.53767779 163.0710405 20.31531532]
[ 32.09098679 6.98937808 35.99819848 25.10160871 132.264735 6.41342771]
[ 46.44207842 8.39503589 29.0372302 38.04704253 115.4814047 2.0454758 ]
[ 35.70345781 19.44325311 20.7 16.26020471 137.5406125 -0.26348965]
[ 54.60031622 21.48897426 29.36021618 33.11134196 118.3433212 -1.47106726]
[ 37.7319919 9.38629828 41.99999999 28.34569362 135.740926 13.68304672]
[ 54.92085752 18.96842952 51.60145541 35.952428 125.8466462 2.00164247]
[ 51.07983294 14.20993529 35.95122893 36.86989765 115.8037111 6.90508996]
[ 63.79242525 21.34532339 65.99999999 42.44710185 119.5503909 12.38260373]
[ 33.84164075 5.07399141 36.64123294 28.76764934 123.9452436 -0.19924909]
[ 49.82813487 16.73643493 28. 33.09169994 121.4355585 1.91330704]
[ 42.51727249 14.37567126 25.32356538 28.14160123 128.9056892 0.75702014]
[ 53.68337998 13.44702168 41.58429713 40.23635831 113.9137026 2.73703529]
[ 51.62467183 15.96934373 35. 35.6553281 129.385308 1.00922834]
[ 67.80469442 16.55066167 43.25680184 51.25403274 119.6856451 4.86753994]
[ 46.63786363 15.85371711 39.99999999 30.78414653 119.3776026 9.06458168]
[ 64.26150724 14.49786554 43.90250363 49.76364169 115.3882683 5.95145437]
[ 40.34929637 10.19474845 37.96774659 30.15454792 128.0099272 0.45890137]
[ 48.3189305 17.45212105 47.99999999 30.86680945 128.9803079 -0.91094057]
[ 57.1458515 16.48909145 42.84214764 40.65676005 113.8061775 5.0151857 ]
```

```
[ 47.31964755    8.5736803   35.56025198   38.74596726 120.5769719    1.63066351]
[ 33.04168754   -0.32467846   19.0710746   33.366366   120.3886112    9.35436493]
[ 38.04655072    8.30166942   26.23683004   29.7448813   123.8034132    3.88577349]
[ 69.3988184    18.89840693   75.96636144   50.50041147 103.5825398   -0.44366081]
[ 89.01487529   26.07598143   69.02125897   62.93889386 111.4810746    6.0615084 ]
[ 47.90356517   13.61668819   36.          34.28687698 117.4490622   -4.24539542]
[ 42.51561014   16.54121618   41.99999999   25.97439396 120.631941    7.87673069]
[ 56.10377352   13.10630665   62.63701952   42.99746687 116.2285032   31.17276727]
[ 61.54059876   19.67695713   52.89222856   41.86364163 118.6862678    4.81503108]
[ 38.50527283   16.96429691   35.11281407   21.54097592 127.6328747    7.98668323]
[ 43.11795103   13.81574355   40.34738779   29.30220748 128.5177217    0.97092641]]
```

support vector for Abnormal class=26 support vector for Normal class=27

Indices of support vectors are

```
[ 2  9 24 28 31 41 42 46 47 48 50 52 56 69 89 94 96 102
109 151 160 181 187 193 194 204  8 15 29 32 58 64 67 76 78 84
 85 101 113 118 131 141 143 147 162 164 171 176 195 198 199 200 205]
```

- **Examine the number of support vectors for each class and their attribute values and comment on what can be inferred from these values.**

From above output it can be seen that number of support vectors for the abnormal class are 26 and support vector for Normal class= 27.

It can be inferred from above output that, Support vectors are the data points that lie on the margin of the SVM classifier. Compared to other data points, support vectors of both the classes at minimum distances i.e. these points decide to which class a new data instance belongs to.

- **Code for accuracy precision and recall**

```
accuracy = clf.score(X_test,y_test)
result = precision_recall_fscore_support(y_test, predict, pos_label='Normal', average='binary')
print(" Accuracy " +str(accuracy) + "\t\t Precision " +str(result[0])
      +"\n Recall " +str(result[1]))
```

- **Output**

```
Accuracy 0.86 Precision 0.8529411764705882
Recall 0.7631578947368421
```

1b) Run the training and testing five times, each time selecting a different randomly selected set of training instances. Create the confusion matrix for this classifier using average number of true positives, false positives etc.

CODE:

```
clf = SVC(kernel='linear')
Precision = []
Recall = []
FScore = []
Accuracy = []
tp=0
tn=0
fp=0
fn=0
from sklearn.metrics import confusion_matrix
for x in range(0, 5):
    data1=shuffle(data1);
    X = data1.loc[:, 'pelvic_incidence': 'degree_spondylolisthesis'];
    y = data1.loc[:, 'class'];
    X_train, X_test, y_train, y_test = X[:210], X[210:], y[:210], y[210:];
    clf.fit(X_train, y_train)
    predict=clf.predict(X_test)
    accuracy = accuracy = clf.score(X_test, y_test)
    result = precision_recall_fscore_support(y_test, predict, pos_label='Normal', average='binary')
    Precision.append(result[0])
    Recall.append(result[1])
    Accuracy.append(accuracy)
    conf_mat = confusion_matrix(y_test, predict)
    print(conf_mat)
    tp= tp + conf_mat[0][0]
    tn= tn + conf_mat[1][1]
    fn= fn + conf_mat[0][1]
    fp= fp + conf_mat[1][0]
avg_conf=np.matrix([[tp/5, fn/5], [fp/5, tn/5]])
print("confusion matrix for this classifier using average number of true positives, false positives etc. =\n"
      "+str(avg_conf))
```

In above code, precision_recall_fscore_support() function calculate precision, recall, f1 score and support given the predicted output, actual output and positive class.

OUTPUT:

```
confusion matrix for this classifier using average number of true
positives,    false positives etc. =
[[62.  8.]
 [ 6. 24.]]
```

1c) Compute the accuracy, precision and recall values.

CODE:

```
avg_acc = np.mean(Accuracy)
avg_pre = np.mean(Precision)
avg_rec = np.mean(Recall)
print("Average Accuracy " +str(avg_acc) + "\t\t Average Precision " +str(avg_pre)
      +"\nAverage Recall " +str(avg_rec))
```

OUTPUT:

```
Average Accuracy 0.8559999999999999    Average Precision 0.8001843317972351
Average Recall 0.760881690904377
```

2) Repeat Q#1 above with the only difference that this time train a non-linear SVM using rbf (radial basis function) for kernel function

- Split it into a Training Set of 210 randomly selected data points
- Train a linear support vector machine (kernel_function = linear) to build a classifier model, Use this model to predict the classes for the data in the Testing Set.

```
data1=shuffle(data1);
X = data1.loc[:, 'pelvic_incidence': 'degree_spondylolisthesis'];
y= data1.loc[:, 'class'];
X_train,X_test,y_train,y_test = X[:210] , X[210:], y[:210] , y[210:];
from sklearn.svm import SVC
clf = SVC(C = 50, kernel = 'rbf', gamma = 0.0001)
clf.fit(X_train,y_train)
predict=clf.predict(X_test)
```

In above code,

SVC() function is equivalent to svmtrain function of matlab.

fit() function is used to train the classifier with given X_train,y_train train dataset.

predict() function predicts the output given a test dataset.

2a) List all the support vectors of the data set. Examine the number of support vectors for each class and their attribute values and comment on what can be inferred from these values.

- List all the support vectors of the data set. Examine the number of support vectors for each class

CODE:

```
print(clf.support_vectors_)
print("support vector for Abnormal class="+str(clf.n_support_[0])+ " support vector for Normal class="+str(clf.n_support_[1]))
print("Indices of support vectors are\n"+str(clf.support_))
```

OUTPUT:

SUPPORT VECTORS ARE:

```
[[ 66.28539377  26.32784484  47.49999999  39.95754893 121.2196839 -0.79962447]
 [ 72.64385013  18.92911726  67.99999999  53.71473287 116.9634162  25.38424676]
 [ 76.1472121  21.93618556  82.96150249  54.21102654 123.9320096  10.43197194]
 [ 72.07627839  18.94617604  50.99999999  53.13010236 114.2130126  1.01004051]
 [ 73.63596236  9.71131795  62.99999999  63.92464442  98.72792982  26.97578722]
 [ 45.36675362  10.75561143  29.03834896  34.61114218 117.2700675 -10.67587083]
 [ 43.34960621  7.46746896  28.06548279  35.88213725 112.7761866  5.75327746]
 [ 54.91944259  21.06233245  42.19999999  33.85711014 125.2127163  2.43256144]
 [ 43.79019026  13.5337531  42.69081398  30.25643716 125.0028927  13.28901817]
 [ 47.74467877  12.08935067  38.99999999  35.6553281  117.5120039  21.68240136]
 [ 41.72996308  12.25407408  30.12258646  29.475889  116.5857056 -1.24440249]
 [ 32.09098679  6.98937808  35.99819848  25.10160871 132.264735  6.41342771]
 [ 44.93667457  17.44383762  27.78057555  27.49283695 117.9803245  5.56961959]
 [ 48.10923638  14.93072472  35.56468278  33.17851166 124.0564518  7.94790486]
 [ 43.20318499  19.66314572  35.      23.54003927 124.8461088 -2.91907595]
 [ 41.17167989  17.32120599  33.46940277  23.85047391 116.3778894 -9.56924986]
 [ 65.53600255  24.15748726  45.77516991  41.3785153 136.4403015  16.37808564]
 [ 66.87921138  24.89199889  49.27859673  41.9872125 113.4770183 -2.00589175]
 [ 35.70345781  19.44325311  20.7      16.26020471 137.5406125 -0.26348965]
 [ 38.66325708  12.98644139  39.99999999  25.67681568 124.914118  2.70300805]
```

[46.85578065 15.35151393 38. 31.50426672 116.2509174 1.66270559]
 [41.35250407 16.57736351 30.70619135 24.77514057 113.2666746 -4.49795756]
 [42.02138603 -6.55494835 67.89999999 48.57633437 111.5857819 27.33867086]
 [45.54078988 13.06959759 30.29832059 32.47119229 117.9808303 -4.98712962]
 [49.70660953 13.04097405 31.33450009 36.66563548 108.6482654 -7.82598575]
 [53.43292815 15.86433612 37.16593387 37.56859203 120.5675233 5.9885507]
 [53.85479842 19.23064334 32.77905978 34.62415508 121.6709148 5.3298432]
 [63.83498162 20.36250706 54.55243367 43.47247456 112.3094915 -0.62252664]
 [65.00796426 27.60260762 50.94751899 37.40535663 116.5811088 7.01597788]
 [41.76773173 17.89940172 20.0308863 23.86833001 118.3633889 2.06296255]
 [31.27601184 3.14466948 32.56299592 28.13134236 129.0114183 3.62302007]
 [55.08076562 -3.75992987 55.99999999 58.84069549 109.9153669 31.77358318]
 [45.44374959 9.9060718 44.99999999 35.53767779 163.0710405 20.31531532]
 [52.41938511 19.01156052 35.87265953 33.40782459 116.5597709 1.6947051]
 [55.28585178 20.44011836 34. 34.84573342 115.8770174 3.55837236]
 [43.1919153 9.9766638 28.93814927 33.21525149 123.4674001 1.74101758]
 [44.48927476 21.78643263 31.47415392 22.70284212 113.7784936 -0.28412937]
 [33.84164075 5.07399141 36.64123294 28.76764934 123.9452436 -0.19924909]
 [48.90290434 5.58758866 55.49999999 43.31531568 137.1082886 19.85475919]
 [47.90356517 13.61668819 36. 34.28687698 117.4490622 -4.24539542]
 [51.07983294 14.20993529 35.95122893 36.86989765 115.8037111 6.90508996]
 [39.65690201 16.20883944 36.67485694 23.44806258 131.922009 -4.96897988]
 [67.53818154 14.65504222 58.00142908 52.88313932 123.6322597 25.9702063]
 [41.6469159 8.8355491 36.03197484 32.8113668 116.5551679 -6.05453796]
 [63.92947003 19.97109671 40.17704963 43.95837332 113.0659387 -11.05817866]
 [66.50717865 20.89767207 31.72747138 45.60950658 128.9029049 1.51720336]
 [48.80190855 18.01776202 51.99999999 30.78414653 139.1504066 10.44286169]
 [61.44659663 22.6949683 46.17034732 38.75162833 125.6707246 -2.70787952]
 [34.64992241 7.51478278 42.99999999 27.13513962 123.9877408 -4.0829376]
 [65.61180231 23.13791922 62.58217893 42.47388309 124.1280012 -4.08329841]
 [53.91105429 12.93931796 38.99999999 40.97173633 118.1930354 5.07435318]
 [57.1458515 16.48909145 42.84214764 40.65676005 113.8061775 5.0151857]
 [53.68337998 13.44702168 41.58429713 40.23635831 113.9137026 2.73703529]
 [33.04168754 -0.32467846 19.0710746 33.366366 120.3886112 9.35436493]
 [50.75329025 20.23505957 37. 30.51823068 122.343516 2.28848775]
 [89.83467631 22.63921678 90.56346144 67.19545953 100.5011917 3.04097326]
 [54.60031622 21.48897426 29.36021618 33.11134196 118.3433212 -1.47106726]
 [53.93674778 20.72149628 29.22053381 33.21525149 114.365845 -0.42101039]
 [42.51561014 16.54121618 41.99999999 25.97439396 120.631941 7.87673069]
 [36.42248549 13.87942449 20.24256187 22.543061 126.0768612 0.17971708]
 [45.57548229 18.75913544 33.77414297 26.81634684 116.7970069 3.13190992]
 [50.08615264 13.43004422 34.45754051 36.65610842 119.1346221 3.08948446]
 [49.82813487 16.73643493 28. 33.09169994 121.4355585 1.91330704]
 [64.31186727 26.32836901 50.95896417 37.98349826 106.1777511 3.11822129]
 [89.01487529 26.07598143 69.02125897 62.93889386 111.4810746 6.0615084]
 [37.14014978 16.48123972 24. 20.65891006 125.0143609 7.3664254]
 [63.79242525 21.34532339 65.99999999 42.44710185 119.5503909 12.38260373]
 [46.63786363 15.85371711 39.99999999 30.78414653 119.3776026 9.06458168]
 [43.11795103 13.81574355 40.34738779 29.30220748 128.5177217 0.97092641]
 [42.51727249 14.37567126 25.32356538 28.14160123 128.9056892 0.75702014]]

Support vector for Abnormal class=35, support vector for Normal class=35
 Indices of support vectors are

[4, 11, 21, 37, 39, 44, 50, 55, 71, 78, 80, 81, 86,
 87, 92, 104, 106, 116, 119, 120, 126, 128, 133, 134, 143, 144,
 149, 151, 168, 175, 194, 196, 200, 206, 207, 2, 7, 12, 43,
 49, 51, 56, 57, 59, 66, 72, 82, 95, 99, 100, 101, 107,
 108, 109, 110, 121, 123, 125, 129, 137, 148, 150, 157, 183, 185,
 187, 199, 205, 208, 209]

- **Examine the number of support vectors for each class and their attribute values and comment on what can be inferred from these values.**

From above output it can be seen that number of support vectors for the abnormal class are 35 and support vector for Normal class= 35.

It can be inferred from above output that, Support vectors are the data points that lie on the margin of the SVM classifier. Compared to other data points, support vectors of both the classes at minimum distances i.e. these points decide to which class a new data instance belongs to.

- **Code for accuracy precision and recall**

```
accuracy = clf.score(X_test,y_test)
result = precision_recall_fscore_support(y_test, predict, pos_label='Normal', average='binary')
print(" Accuracy " +str(accuracy) + "\t\t Precision " +str(result[0])
      +"\n Recall " +str(result[1]))
```

- **Output**

```
Accuracy 0.87          Precision 0.7714285714285715
Recall 0.84375
```

2b) Run the training and testing five times, each time selecting a different randomly selected set of training instances. Create the confusion matrix for this classifier using average number of true positives, false positives etc.

```
Precision = []
Recall = []
FScore = []
Accuracy = []
tp=0
tn=0
fp=0
fn=0
for x in range(0, 5):
    data1=shuffle(data1);
    X = data1.loc[:, 'pelvic_incidence':'degree_spondylolisthesis'];
    y= data1.loc[:, 'class'];
    X_train,X_test,y_train,y_test = X[:210] , X[210:], y[:210] , y[210:];
    clf = SVC(C = 50, kernel = 'rbf', gamma = 0.0001)
    clf.fit(X_train,y_train)
    predict=clf.predict(X_test)
    accuracy = clf.score(X_test,y_test)
    result = precision_recall_fscore_support(y_test, predict, pos_label='Normal', average='binary')
    Precision.append(result[0])
    Recall.append(result[1])
    Accuracy.append(accuracy)
    conf_mat = confusion_matrix(y_test, predict)
    print(conf_mat)
    tp= tp + conf_mat[0][0]
    tn= tn + conf_mat[1][1]
    fn= fn + conf_mat[0][1]
    fp= fp + conf_mat[1][0]
avg_conf=np.matrix([[tp/5, fn/5], [fp/5, tn/5]])
print("confusion matrix for this classifier using average number of true positives, false positives etc. =\n
      "+str(avg_conf))
```

In above code, **precision_recall_fscore_support()** function calculate precision, recall, f1 score and support given the predicted output, actual output and positive class.

OUTPUT:

```

confusion matrix for this classifier using average number of true positives, false positives etc. =
[[62.  10.4]
 [ 5.2 22.4]]

```

2c) Compute the accuracy, precision and recall values.**CODE:**

```

avg_acc = np.mean(Accuracy)
avg_pre = np.mean(Precision)
avg_rec = np.mean(Recall)
print("Average Accuracy " +str(avg_acc) + "\t\t Average Precision " +str(avg_pre)
      +"\nAverage Recall " +str(avg_rec))

```

OUTPUT:

```

Average Accuracy 0.8619999999999999 Average Precision 0.783041283041231
Average Recall 0.8324346405228757

```

3) Compare the performance values obtained in 1c and 2c above with the ones you received for the same data in Problem 1(c) of Homework#1. Comment on the differences and you observe and their possible causes/consequences.

FOR 1C(Linear kernel SVM),

```

Average Accuracy 0.8559999999999999 Average Precision 0.800184331797235
Average Recall 0.760881690904377

```

FOR 2C(RBF kernel SVM),

```

Average Accuracy 0.8619999999999999 Average Precision 0.78304128304123
Average Recall 0.8324346405228757

```

FOR 1(c) of Homework#1(Decision tree),

```

average of accuracy = 0.810000 average of precision = 0.665102
average of recall = 0.548387

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As can be seen from above values, the accuracy is higher for SVM with rbf kernel than linear kernel SVM and decision tree. Also, the precision and recall values are higher for SVM classifier than decision tree classifier.

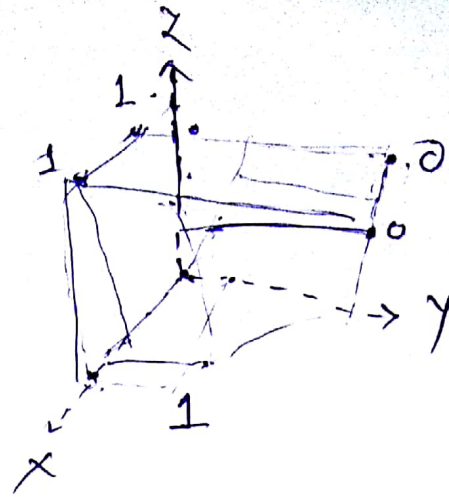
Decision trees can't split further if the attribute values are not separable, whereas SVM finds support vector using complex optimization method.

SVM uses the kernel trick to turn a linearly non-separable problem into a linearly separable one, whereas decision tree split input space into hyper-rectangles according to target.

If data is not separable with hyper-rectangles then decision tree won't perform efficiently, whereas complex kernel function can be used to transform data so that it can be classified with SVM classifier.

4

x	y	z	class
5	2	8	1
-2	9	3	0
0	10	4	0
6	1	4	1
8	-3	9	1



append $x_0 = 1$

x	y	z	x_0	class
5	2	8	1	1
-2	9	3	1	0
0	10	4	1	0
6	1	4	1	1

Initial weight vector:
[1 2 3 4]

①

\vec{x}				\vec{w}				$\vec{x} \cdot \vec{w}$ $\vec{x} \cdot \vec{w}^T$	error	\vec{w}_{t+1} $\vec{w}_t = (\vec{w}_t \pm \alpha)$
x	y	z	x_0	w_1	w_2	w_3	w_4			
5	2	8	1	1	2	3	4	37	N	1 2 3 4
-2	9	3	1	1	2	3	4	29	Y	3 -7 0 3
0	10	4	1	3	-7	0	3	-67	N	3 -7 0 3
6	1	4	1	3	-7	0	3	14	N	3 -7 0 3
8	-3	9	1	3	-7	0	3	48	N	3 -7 0 3
5	2	8	1	3	-7	0	3	4	N	3 -7 0 3
-2	9	3	1	3	-7	0	3	-66	N	3 -7 0 3
all ok										

Hence, final weight vector

$$= [3 -7 0 3]$$

$3x - 7y + 0z + 3 = 0$ is the hyperplane.

ii] As the number of misclassified ~~data~~ training vector only one which is $[-2 \ 9 \ 3 \ 1]$

So, for first epoch

$$J(w) = \sum_{x \in Y} (\delta_x w^T x)$$

where, Y is set of misclassified datapoints
& δ_x is +1 as the misclassified point ~~also~~ belongs to negative class.

$$\therefore J(w) = 1 [1 \ 2 \ 3 \ 4] \begin{bmatrix} -2 \\ 9 \\ 3 \\ 1 \end{bmatrix} = -2 + 18 + 9 + 4 = 29$$

$$\therefore \text{for 1st epoch } \underline{J(w) = 29}.$$

For, second epoch

As there are no misclassification in second epoch

$$\underline{\underline{J(w) = 0}}$$