Assignment 1

Financial Engineering

Option price in Matlab

Price a European Call Option with the following characteristics:

Strike price: 1.05 Euro

value date: 31st of January 2023

time-to-maturity (ttm): 4 months (consider a yearfrac 1/3)

volatility: 21% (per year)

ttm-zero-rate: 2.5%

Underlying: equity stock

Dividend Yield: 2%

Settlement: physical delivery

Number of contracts: 1 Mln Underlying price 1 Euro

Questions

a. Price the option,

considering an underlying price equal to 1 Euro (i.e a derivative Notional of 1 Mln Euro):

- i) via blkprice Matlab function;
- ii) with a CRR tree approach;
- iii) with a Monte-Carlo (MC) approach.
- b. Consider M, as the number of intervals in CRR and as the number of simulations in the MC. Focus on a call. Select M according to the criteria mentioned in the class.

[Hint1: As error for the CRR consider the difference in absolute value w.r.t. to the exact value, while as error for the MC an estimation of the unbiased standard deviation of the MC price]

[Hint2: Option bid/ask for these equity options is 1bp (0.01%).]

c. Show that the numerical errors for a call rescale with M approximately as 1/M for CRR and as $1/\sqrt{M}$ for MC.

[Hint3: Show, for a call, the error for CRR and MC varying M in a log-log scale.]

- d. Price also a European Call Option with <u>European barrier</u> at €1.4 (up&out) and same parameters with the two numerical techniques (tree & MC). Does it exist a closed formula also in this case? If yes, compare the results.
- e. For this barrier option, plot the Vega (possibly using both the closed formula and a numerical estimate) with the underlying price in the range 0.65 Euro and 1.45 Euro. Comment the results.
- f. [Facultative]. Does antithetic variables technique (Hull 2009, Ch.19.7) reduce MC error of point b.?
- g. [Facultative] Price also -with the Tree- a Bermudan option, where the holder has also the right to exercise the option at the end of every month, obtaining the stock at the strike price K. Does it significantly differ from a Call Option Price?

h. [Facultative] Pricing the Bermudan option, vary the dividend yield between 0% and 5% and compare with the corresponding European price. Discuss the results.

Function signatures

- a. optionPrice=EuropeanOptionClosed(F0,K,B,T,sigma,flag), flag 1 call, -1 put.
- b. optionPrice=EuropeanOptionMC(F0,K,B,T,sigma,N,flag)
- c. optionPrice=EuropeanOptionCRR(F0,K,B,T,sigma,N,flag)
- d. [M,errorCRR]=PlotErrorCRR(F0,K,B,T,sigma); M=2^m with m=1:10; (return row vectors)
- e. [M,stdEstim]=PlotErrorMC(F0,K,B,T,sigma); M=2^m with m=1:20; (return row vectors)
- f. optionPrice=EuropeanOptionKOMC(F0,K, KO,B,T,sigma,N)
- g. optionPrice=EuropeanOptionKOCRR(F0,K, KO,B,T,sigma,N)
- h. gamma= VegaKO(F0,K,KO,B,T,sigma,N,flagNum), flagNum=1 CRR, flagNum=2 MC, flagNum=3 Exact.

Comment codes, use explicative variable names and divide into sections. It's IMPORTANT to use **exactly the same** signatures provided above.

<u>Delivery Date:</u> Friday 11:59 a.m. the 21th of February. <u>Pay attention to the delivery address</u> below.

Email Subject: Follow rules instructions